Improved vertical gradients in an ocean temperature and salinity climatology

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Generalized Digital Environmental Model (GDEM)



Vertical Gradient Issues

Case I: small observed gradients



Vertical Gradient Issues

Case II: large observed gradients



Vertical Gradient Issues

Vertical gradients are important for ocean acoustics.



Presentation Outline

- (1) Ocean observations (1.7 million XBTs)
- (2) XBTs are important
- (3) Gridding techniques (vertical gradient constraints)
- (4) Results: preservation of the observed vertical

gradients of temperature and salinity

Observations



Observations



The number of observed temperature (blue circles) and salinity (red squares) profiles for each year starting in 1930. The last partial year is 2007 and extends only through October.

Observations

Sources: MOODS, WOD05, and Argo

Data Type	Number of profiles
Raw Total	8,302,197
Editing	-3,621,099 (-2,237,379 MBTs removed)
Short profile in deep water	-268,644
Total remaining T	4,412,454 (approx. 1,742,000 XBTs)
Total remaining S	1,969,081

For the XBT drop rate corrections were applied to WOD05 data based on the secondary header # 54 as directed in the WOD05 database documentation (Johnson et al. 2006).

T: good proxy for sound speed



9

Vertical Resolution



10

Vertical Resolution



11

Vertical Resolution



Horizontal Gridding, 1/4°

Cost function: minimize the squared slope and data misfit

$$J = \sum_{m} \sum_{n} \left\{ \left(\frac{T_{n+1,m} - T_{n,m}}{\Delta x} \right)^2 + \left(\frac{T_{n,m+1} - T_{n,m}}{\Delta y} \right)^2 + \sum_{k} \left(T_{m,n} - \theta_{m,n,k} \right)^2 \right\}$$

 $T_{m,n}$ Field solution T or S being sought at grid points m, n that are not over land.

 $\theta_{m,n,k}$ Data for each month are selected to be within 45 days of the center of the month.

• Zero-gradient boundary conditions were applied at land boundaries.

 Solution is system of Poisson diffusion equations solved using the Gauss-Seidel method.

Vertical Gradient Constraints

Minimize:

(1) different between analysis and observed vertical gradients(2) difference between the original and corrected gridded profile:

$$J = \sum_{k=2}^{N} \left(\frac{\hat{T}_{k} - \hat{T}_{k-1} - D_{k}}{\delta_{k}} \right)^{2} + \sum_{k=1}^{N} \left(\frac{\hat{T}_{k} - T_{k}}{\sigma_{k}} \right)^{2}$$

 $\begin{aligned} \hat{T}_{k}, k &= 1, N \\ T_{k}, k &= 1, N \\ D_{k}, k &= 1, N \end{aligned} \ \ \begin{array}{l} \text{The T or S solution being sought} \\ \text{The T or S from the $2D$ gridding} \\ \text{The gridded $observed$ vertical differences} \end{aligned}$

The adjusted \hat{T} or \hat{S} is determined by the minimization of the cost function in a tridiagonal system of N equations.

Vertical Stability Constraints

Potential temperature and density is referenced to pressure midway between layers.

$$\theta_{i-1} = \theta \left(S_{i-1}, T_{i-1}, p_{i-1}, pr \right)$$

$$\theta_{i} = \theta \left(S_{i}, T_{i}, p_{i}, pr \right)$$

$$\rho_{i-1} = \rho \left(S_{i-1}, \theta_{i-1}, pr \right)$$

$$\rho_{i} = \rho \left(S_{i}, \theta_{i}, pr \right)$$

$$N^{2} = -\frac{g}{\left(\rho_{i-1} + \rho_{i} \right) / 2} \frac{\left(\rho_{i} - \rho_{i-1} \right)}{\left(z_{i} - z_{i-1} \right)}$$

A stabilizing salinity difference is incrementally increase until:

$$N^2 = 1.5 \times 10^{-7} \, s^{-2}$$

Case I

Impact of vertical gradient constraint

Bering Sea shelf east of Bristol Bay along 58 N



Impact of vertical gradient constraint

Case I

Bering Sea shelf east of Bristol Bay along 58 N



Case I

Impact of vertical gradient constraint

Before (Colorfilled) and **After** (Black Line Contours) Vertical Gradient Correction

Temperature (Deg C) January Uncorrected - Colorfilled, Corrected - Line Contours Vertical Section along Latitude = 33.25 N 0 10 20 30 40 Depth (m) 50 U.S. 60 east coast 70 80 90 100 291 285 282 283 284 Longitude (Degrees) 75°W 79°W

Uncorrected and **corrected** mean temperature profiles computed from local **observations**.







Conclusions

•XBTs provide vertical gradients for acoustic applications.

•Vertical gradient constraints correct for: Case I: small observed gradients Sampling irregularities near shelf breaks

Case II: large observed gradients small improvement on mixed layer depth representation

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