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1 **Identifying and Estimating Biases between XBT**
2 **and Argo Observations Using Satellite Altimetry**

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16 **Abstract**

17 A methodology is developed to identify and estimate systematic biases between
18 expendable BathyThermograph (XBT) and Argo observations using satellite altimetry.
19 Pseudo-climatological fields of isotherm depth are computed by least squares adjustment
20 of in-situ XBT and Argo data to altimetry-derived sea height anomaly (SHA) data. In
21 regions where the correlations between isotherm depth and SHA are high, this method
22 reduces sampling biases in the *in situ* observations by taking advantage of the high
23 temporal and spatial resolution of satellite observations. In this study we consider
24 temperature profiles from *deep* XBTs corrected for a bias identified and adopted during
25 the 1990s. Our analysis shows that the pseudo-climatological isotherm depths derived
26 from these corrected XBTs are predominantly deeper than the Argo-derived estimates
27 during the 2000–2007 period. The XBT minus Argo differences increase with depth
28 consistent with hypothesized problems in the XBT fall rate equations. The depth-
29 dependent XBT minus Argo differences suggest a global positive bias of 3% of the XBT
30 depths. The fact that this 3% error is robust among the different ocean basins provides
31 evidence for changes in the instrumentation, such as changes in the terminal velocity of
32 the XBTs. The value of this error is about the inverse of the correction to the XBT fall-
33 rate equation (FRE) implemented in 1995, suggesting that this correction, while adequate
34 during the 1990s, is no longer appropriate, and could be the source of the 3% error. This
35 result suggests that for 2000-2007, the XBT dataset can be brought to consistency with
36 Argo by using the original FRE coefficients without the 1995 correction.

37 **Introduction**

38 expendable BathyThermographs (XBT) are widely used to observe the thermal
39 structure of the upper ocean and constitute a large fraction of the archived ocean thermal
40 data during the 70s, 80s and 90s. Until the advent of the Argo array, XBTs dominated
41 the global ocean thermal observations, currently; XBTs represent approximately 25% of
42 current ocean temperature profile observations, being a valuable complement for the
43 Argo array. Unlike Argo observations, XBTs determine the depth of the temperature
44 observations indirectly. The time in seconds elapsed since the XBT hits the ocean
45 surface is converted into depth, z_{xbt} , using a fall-rate equation (FRE):

$$46 \quad z_{xbt} = bt - at^2 \quad (1),$$

47 where the a and b coefficients are empirical constants related to the physics of the probe
48 descent.

49 This FRE results from a simple dynamical model of the descent of the XBT with
50 the net buoyant force being balanced by hydrodynamic drag proportional to the square of
51 the probe speed (Green 1984; Hallock and Teague 1992). The linear term bt in (1) results
52 from this balance neglecting the acceleration of the probe d^2z/dt^2 . As a result the fall
53 speed is virtually equal to the terminal velocity, a reasonable assumption for depths larger
54 than 10 m. The b coefficient represents the value of this terminal velocity and is, to first-
55 order, determined by the drag coefficient and the mass of the probe in the water. The
56 deceleration term $-at^2$ accounts for the both the reduction of probe mass as the wire pays
57 out and the increasing drag with depth, where the later is more important. The depth

58 dependence of the fall-rate due to changes in sea water density is one order of magnitude
59 smaller than the temperature dependence of the drag or the mass loss due to wire payout
60 (Green 1984).

61 The bulk of XBT temperature profiles are collected using probes manufactured by
62 Sippican Incorporated (now Lockheed Martin Sippican, hereinafter Sippican). Even
63 though these coefficients are based on physical parameters of the probe (Green 1984),
64 they are empirically determined by the manufacturer with standard values for $b = 6.472$
65 m s^{-1} and $a = 216 \times 10^{-5} \text{ m s}^{-2}$. The processes involved in the descent of an XBT probe are
66 certainly more complex than the first-order dynamics implied in equation (1). As a
67 result, the determination of the XBT depth is the most important source of error in XBT
68 temperature profiles with reported values of 17 m, (McDowell 1977; Seaver and
69 Kuleshov 1982) and 19 m (Fedorov et al. 1978) at 750 m depths. Systematic errors in the
70 computed XBT depths have been identified since the mid 1970s: Comparison studies
71 between simultaneous XBTs and Conductivity Temperature Depth (CTD) casts found a
72 small positive bias above the thermocline and a much larger negative bias for depths
73 below (Fedorov 1978; Flierl and Robinson 1977; McDowell 1977; Seaver and Kuleshov
74 1982). Evidence of surface offsets associated with initial transients has also been found
75 (e.g. Singer 1990), pointing at the limitations of (1) in the determination of XBT depths.
76 Nonetheless, XBT temperature profiles have been shown to be accurate enough to
77 characterize mesoscale phenomena (Seaver and Kuleshov 1982; Flierl and Robinson
78 1977).

79 It was not until the 1990s when the impact of these systematic errors on climate
80 applications was recognized. Sippican adopted a correction factor after a comprehensive
81 analysis of research-quality CTD and XBT data by Hanawa et al. (1995 - hereinafter
82 H95). This study showed that the Sippican coefficients in the FRE resulted in depths that
83 were too shallow, producing a cold temperature bias in most of the water column. A
84 stretching factor $f_{H95} = 1.0336$ was recommended to correct this bias, and later applied to
85 the Sippican original FRE as follows:

$$86 \quad z_{H95} = f_{H95}(bt - at^2). \quad (2)$$

87 Recent studies suggest time-varying biases between XBT and CTD observations
88 that are consistent with changes in the b coefficient, i.e. the probe's terminal velocity
89 (Gouretski and Koltermann 2007; Wijffels et al. 2008; Ishii and Kimoto 2009). The
90 time-varying errors found by these studies represent up to 10% changes in the b
91 coefficient of the FRE, leading to commensurate changes in z_{xbt} . The implied changes in
92 the FRE exceed the 2% error specified by Sippican and are likely to be responsible for
93 spurious decadal signals in global mean heat storage time series (Wijffels et al. 2008;
94 Levitus et al. 2009).

95 Starting in 2000, the rapidly expanding Argo array (Gould et al. 2004) provides
96 global and highly quality controlled ocean temperature and salinity data with CTD
97 accuracy. Nonetheless, XBT profiles make up to 25% of the current global temperature
98 profile observations during the period of study. Therefore, assessing and correcting this
99 bias is key to monitoring changes of global ocean heat content. Moreover, systematic

100 biases between observing systems with disparate quality capabilities, such as Argo and
101 XBTs, can also introduce spurious climatic signals in heat storage as the ratio of the
102 number of observations collected with each platform changes (e.g. Willis et al. 2009).
103 Argo and CTD profiles also have uncertainties in the determination of pressure/depth.
104 For instance, profiles from Argo floats are often corrected for drifts in the pressure sensor
105 (http://www.argo.ucsd.edu/Acpres_drift_apex.html). Most of the Argo pressure drifts are
106 less than 2 db with very rare cases as large as 10 db. These large drifts are unlikely to
107 have a global impact compared with the hypothesized XBT bias, which if detected,
108 should exhibit a global extent. Moreover, the magnitude of the hypothesized XBT bias,
109 about 20 m at 700 m depth (e.g. Wijffels et al. 2008, Figure 6), is substantially larger than
110 the Argo drifts in addition to having very different depth dependence. Ideally, XBT data
111 should be evaluated against CTD data in order to obtain an absolute correction (e.g.
112 Hanawa et al. 1995). However, the sparse coverage provided by CTDs during the 2000-
113 2007 period does not permit a global comparison. For these reasons, in this study we
114 evaluate XBTs relative to Argo data. This should be kept in mind if the correction
115 derived here is applied to XBT data.

116 Most intercomparisons have focused on localized concurrent CTD and XBT casts,
117 which have limited temporal and spatial scope. On the other hand, very few studies have
118 analyzed the spatial dependence of these errors (e.g. Schmid 2005; Wijffels et al. 2008).
119 In this study we use temperature profiles obtained from XBT and Argo combined with
120 satellite altimetry observations to investigate the spatial dependence of potential XBT
121 errors globally. Simultaneously, a methodology is developed to estimate the uncertainty

122 of these errors. This methodology takes advantage of the high correlation between
123 satellite altimeter sea height observations and the thermal structure of the upper ocean to
124 reduce uncertainty associated with sampling by *in situ* observations. This methodology is
125 shown to produce statistically significant (1-sigma) estimates of the XBT bias over
126 relatively short periods compared with conventional climatologies, thus becoming a
127 viable procedure to correct future XBT observations on an operational basis.
128 Furthermore, in this study we characterize the spatial extent of this bias¹ and provide
129 more evidence for a FRE problem.

130 **Data**

131 Temperature profiles obtained from XBTs, profiling floats, and CTD casts are
132 used in this study. The XBT data are obtained from Global Temperature-Salinity Profile
133 Program (GTSP; <http://www.nodc.noaa.gov/GTSP>). The profiling float data are
134 available from the GTSP and from the Argo Global Data Assembly Centers (GDAC;
135 <http://www.usgodae.org/argo/argo.html> and <http://www.coriolis.eu.org/cdc/argo.htm>).
136 CTD data are also obtained from the GTSP. Temperature profiles in the GTSP and
137 GDACs are typically quality controlled with different standards. All profiles analyzed
138 here, including XBTs, are quality controlled following an additional procedure based on

¹ The term bias and error used indistinguishably throughout this paper to refer to those errors that are systematic.

139 the standard procedures that are approved by the international Argo data management
140 team consisting of removal of duplicates, spike detection, pressure increasing test, and a
141 vertical gradient test (Schmid 2005). In addition, the profiles were compared with
142 climatology (Conkright et al. 2002). For the Argo data, only pressure and temperature
143 values with quality control flags equal to 1 are used in addition to “adjusted” fields when
144 available. Since 50% of the Argo profiles collected during the 2000-2007 are available in
145 delayed-mode, real-time profiles were used to complete the Argo data. After the
146 additional quality control and duplicates removal are performed, the majority (85%) of
147 the non-XBT profiles used in our study are profiling floats obtained from the Argo
148 GDAC. The remaining profiles are profiling float profiles obtained from the GTSP (5%)
149 and CTDs (10%). Approximately 120,000 XBT temperature profiles and 380,000 Argo
150 and CTD temperature profiles that passed the quality control were included in this study.

151 All XBT-derived profiles analyzed here correspond to “deep” XBTs, such as
152 Sippican models T7 and DeepBlue. These XBTs are designed to reach depths of about
153 750 m and represent the bulk of the XBT observations since 2000. Profiles shorter than
154 550 m were not considered to avoid including *shallow* XBTs, which have different FRE
155 coefficients. The transition from the original Sippican coefficients to the H95 correction
156 has resulted in profiles submitted to the GTSP with the original FRE during a period
157 after the H95 correction was recommended (Wijffels et al. 2008). Some profiles were
158 submitted to the GTSP without any information on the coefficients used in the FRE.
159 However, from 2000 to 2007 virtually all profiles include information indicating the FRE
160 coefficients, with the majority including the H95 correction. In this study, we only

161 consider XBT profiles with FRE coefficients unambiguously indicated in the profile.
162 The H95 correction was applied whenever the metadata unambiguously indicated that it
163 was not applied in the data submitted to the GTSP. About 20% of the XBT profiles
164 required this adjustment. No profiles with ambiguous FRE coefficients were found for
165 the period of study. As a result, all XBT profiles considered in this study have the H95
166 FRE coefficients applied. A pressure offset has been recently found in a group of Argo
167 profiling floats. All temperature profiles obtained by floats with this problem have not
168 been considered in this study following the recommendation of the Argo project
169 (http://www-argo.ucsd.edu/Acpres_offset2.html).

170 Altimetry-derived sea surface height observations are used in this study for two
171 reasons: first, to avoid potential biases in climatological estimates of isotherm depth that
172 arise from the relatively inhomogeneous sampling inherent to *in situ* hydrography;
173 second, to reduce the uncertainty of the climatological estimates of isotherm depth in
174 regions where the thermal structure of the upper ocean is correlated with the sea surface
175 height. The altimetry data used here are the delayed-mode optimally interpolated gridded
176 sea surface height (SHA) fields produced by AVISO according to the methodology of Le
177 Traon et al. (1998), with spatial resolution of 0.25 degrees, and with temporal resolution
178 of 1 week. The altimetric observations used to produce these gridded fields were
179 obtained from two or three satellites throughout the period from January 2000 to
180 December 2007. The AVISO SHA fields are anomalies computed with respect to the
181 1993 – 1999 mean from the direct altimetry observations. Therefore, the time-mean field
182 for the 2000-2007 period is not necessarily zero. To apply our methodology we removed

183 the time-mean SHA corresponding to the 2000-2007 period on every grid point. This
184 simplifies the interpretation of the isotherm depth estimates obtained results from our
185 methodology as climatological mean estimates.

186 **Methods**

187 The methodology to identify and quantify biases between XBT and Argo
188 observations presented here consists of the following steps:

- 189 1. The climatological isotherm depths and their uncertainty are estimated from H95-
190 corrected XBTs and from Argo profiles separately. Due to the short duration of the
191 Argo dataset, correlations with altimetry-derived SHA fields are used to reduce the
192 uncertainty of the isotherm depth estimates.
- 193 2. The geographical distribution of the differences between XBT minus Argo isotherm
194 depths is analyzed. Systematic biases between the two observing systems are
195 expected to affect the mean climatological estimates. Only differences with non-
196 overlapping 1-sigma confidence intervals are considered.
- 197 3. The depth dependence of the XBT minus Argo differences are analyzed to confirm a
198 problem in the XBT FRE. The depth dependent biases in the XBTs are estimated
199 globally, and in different regions, to infer other potential sources of error than the
200 FRE.

201 Potential biases in the XBT observations are explored here by comparing
202 estimates of the mean-climatological isotherm depth derived from XBTs with estimates

203 derived from Argo profiling-floats and CTDs. Throughout the analysis, Argo and CTD
204 observations, are collectively referred to as Argo due to the prevalence of this platform
205 during the period of study. Unlike XBTs, Argo and CTD casts measure the pressure at
206 each temperature observation directly. Thus, the depth of these temperature profiles is
207 determined with higher accuracy than the XBT FRE. For Argo and CTD profiles the
208 pressure is converted into depth following a methodology that accounts for the variation
209 of gravity with latitude and depth, and the effect of pressure on density (Saunders 1981).
210 This methodology neglects the small influence of salinity and temperature on density
211 with an error less than 0.25 m, which is at least one order of magnitude smaller than the
212 hypothesized biases in the FRE equation we seek to identify and quantify. For these
213 reasons, in this study we evaluate the depth of isotherms derived from XBT data relative
214 to Argo data, since the latter are expected to have smaller systematic biases.

215 Several studies have shown that observations of sea surface height are strongly
216 correlated with the thermal structure of the upper ocean (Goni et al. 1996; Gilson et al.
217 1998; Mayer et al. 2001; Willis et al. 2004). Based in this virtually ubiquitous
218 relationship, we propose a methodology that combines altimetry-derived SHA fields with
219 *in situ* temperature profiles to produce climatologies capable of quantifying potential
220 biases in the XBT observations. The depths of the 5°C to 28°C isotherms, every 1°C, are
221 estimated for each XBT and Argo temperature profile. The SHA fields are interpolated
222 into the location and day of the temperature profiles using a Gaussian filter in space and
223 linear interpolation in time. The pairs of interpolated SHA values and *in situ* isotherm
224 depths are binned into 3°×3° bins globally, with XBT and Argo profiles separately. On

225 each $3^\circ \times 3^\circ$ bin, the isotherm depth values are linearly regressed on the interpolated SHA
226 estimating a correlation coefficient, regression gain, and a y-intercept.

227 Results for the depth of the 10°C and 20°C isotherms are highlighted because
228 these isotherms lie in thermocline waters in subtropical and equatorial oceans
229 respectively. The spatial distribution of the correlation coefficients obtained for the depth
230 of the 10°C isotherm (h_{10}) are similar between estimates using Argo (Figure 1a) and XBT
231 (Figure 1b) observations. High correlations ($r > 0.6$) are found in regions where this
232 isotherm is within thermocline waters, such as in the subtropical gyres, with the
233 exception of the South Atlantic subtropical gyre where observations are scarce. The
234 correlation coefficients obtained for the depth of the 20°C isotherm (h_{20}) show high
235 values in the equatorial oceans both for Argo (Figure 1c) and XBT (Figure 1d)
236 observations. The correlation coefficients between the Argo-derived isotherm depth and
237 altimetry-derived SHA are statistically significant over most of the global ocean with a
238 67% confidence level (1-sigma) based on a chi-squared distribution. The correlation
239 coefficients between XBT-derived isotherm depth and altimetry-derived SHA are
240 statistically significant (1-sigma) over regions covered by XBT transects, where the
241 density of observations is largest. We assume that all observations are independent in the
242 estimation of the statistical uncertainty. This is a reasonable assumption for the Argo
243 profiles, which could show some correlation between successive 10-day profiles, but are
244 generally decoupled between casts in Ekman layer. In contrast, multiple XBT casts
245 sampling one single mesoscale feature are more common along high-density transects
246 (Roemmich and Gilson 2001). In these cases, the uncertainty of the correlations will be

247 underestimated. However, the conclusions presented are robust because our estimation
 248 of the depth-dependent XBT error is performed using estimates of isotherm depth
 249 resulting from regions with very high correlations ($r > 0.8$) with the SHA fields. We
 250 tested the robustness of our results by considering the case of three XBTs sampling the
 251 same eddy, resulting in factor of $\sqrt{3}$ increase in the confidence interval, but without
 252 impact on the estimate of the XBT minus Argo bias.

253 Global fields of regression gain and y-intercept are obtained by least-squares
 254 fitting of a straight line to the pairs of interpolated SHA values, η' , and the *in situ*
 255 isotherm depth observations, h , on each $3^\circ \times 3^\circ$ bin:

$$256 \quad \hat{h} = \varepsilon^{-1} \cdot \eta' + \tilde{h}, \quad (3)$$

257 where \hat{h} is the isotherm depth estimated by this statistical model for each altimetry-
 258 derived η' value, ε^{-1} is the regression gain, and \tilde{h} is the y-intercept. For each isotherm,
 259 the regression slope, ε^{-1} , is related to the reduced gravity of a two-layer model, thus
 260 representing a measure of the local stratification. Conversely, since the time-mean value
 261 of η' at each location is zero, the y-intercept, \tilde{h} , represents the time-mean isotherm
 262 depth predicted by this statistical two-layer model. We refer to \tilde{h} as pseudo-climatology,
 263 to distinguish it from the climatology obtained from averaging the Argo or XBT
 264 observations directly:

$$265 \quad \bar{h} = \sum h_i / N \quad (4).$$

266 The pseudo-climatologies, \tilde{h} , obtained from (3) weight the *in situ* observations
267 with the satellite-derived η' fields in a least-squares sense. This procedure avoids biases
268 due to inhomogeneous sampling and reduces the statistical uncertainty of the pseudo-
269 climatologies. In the following subsections we discuss these two key features of the
270 methodology that allow identification and estimation of potential biases in the XBT
271 observations.

272 *a. Reduced Sampling Bias*

273 Throughout this study we compare the parameters obtained from the regression
274 (3) between the satellite-derived η' and h obtained from each platform. Any statistical
275 significant difference between the regression parameters may be indicative of problems
276 in either or both platforms. Argo floats have high accuracy in depth and temperature but
277 may have spatial and temporal sampling problems inherent of a Lagrangian observing
278 platform. XBTs are also prone to sampling problems, however, their most important
279 source of error is in the determination of depth, which are much larger than errors in the
280 temperature sensor. As discussed in the introduction, there is evidence suggesting that
281 XBTs suffer from systematic biases associated with changes in the coefficients of the
282 FRE (1). In regions of high correlations, the methodology proposed here reduces the
283 sampling bias using high resolution SHA fields, allowing us to identify other systematic
284 errors, such as those associated with the FRE. Thus, discrepancies in the regression
285 parameters will point to problems related to XBT depth estimates.

286 Both climatology estimators \tilde{h} and \bar{h} are related through the correlation
 287 coefficient, r , and mean SHA, $\bar{\eta}'$, according to basic properties of the least-squares
 288 method (Lawson and Hanson, 1974):

$$289 \quad \tilde{h} = \bar{h} - r \frac{\sigma_h}{\sigma_\eta} \bar{\eta}', \quad (5)$$

290 where σ_h and σ_η are the standard deviation of the h and η' observations
 291 respectively. Note that while the time-mean η' is zero, the mean η' corresponding to the
 292 *in situ* observations, $\bar{\eta}'$, is not necessarily zero due to the inhomogeneous temporal and
 293 spatial sampling of XBT and Argo observations at each location. For instance, when *in*
 294 *situ* observations are predominantly collected in anti-cyclonic eddies, which are
 295 characterized by positive η' values and isotherms deeper than the background flow; the
 296 \bar{h} will be biased towards large values. In this case, the $r \sigma_h / \sigma_\eta \bar{\eta}'$ term in (5) represents
 297 a correction to this bias. If observations are biased towards anti-cyclonic eddies, then $\bar{\eta}'$
 298 > 0 and according to (5) the \tilde{h} estimate will be lower than \bar{h} .

299 For example, 82 Argo and 36 XBT quality controlled observations are analyzed in
 300 a $3^\circ \times 3^\circ$ bin centered in 169°W 4°S . The mean depths of the 20°C isotherm estimated
 301 from Argo and XBTs are $\bar{h}_{20} = 179.4 \pm 1.3$ (Argo) and $\bar{h}_{20} = 182.9 \pm 2.4$ (XBT), where the
 302 uncertainty is given by the standard error of the sample. The 1-sigma confidence
 303 intervals overlap, therefore the two estimates are statistically indistinguishable with a
 304 67% probability. A scatter plot of the observed isotherm depths from each platform and
 305 their corresponding η' values (Figure 2a), suggests that 66 out of 82 Argo observations

306 were collected over positive η' values. In other words, most of the Argo observations
307 were collected over anticyclonic features; therefore the \bar{h} estimate must be deeper than
308 that derived from XBTs, which were obtained at locations with evenly distributed
309 positive and negative η' values. However, the \bar{h} estimates do not show a significant
310 difference, this raises an apparent contradiction that could be explained by a systematic
311 deep bias in the XBT observations.

312 This apparent contradiction may be elucidated with the analysis of the results
313 from the linear regression. The correlation coefficients are 0.6 and 0.5 for Argo and
314 XBT, respectively. The regression gains obtained from each platform are statistically
315 indistinguishable within 1-sigma confidence levels. On the other hand, the y-intercepts
316 or pseudo-climatology estimates are statistically distinct within 1-sigma confidence
317 levels, with values of $\tilde{h}_{20} = 172.1 \pm 1.4$ (Argo) and $\tilde{h}_{20} = 181.2 \pm 2.1$ (XBT). These
318 estimates suggest that XBTs overestimate the depth of the 20°C isotherm by about 10 m.
319 This difference between the estimates is statistically significant based on the 1-sigma
320 confidence intervals of the y-intercept resulting from the linear regressions, \tilde{h} .

321 The previous example illustrates how in regions of high correlations, this
322 methodology takes advantage of the homogenous sampling of satellite altimetry to
323 correct biases in the estimates of isotherm depth. On the other hand, when the sampling
324 is homogeneous and in the absence of systematic biases, \bar{h} and \tilde{h} converge to the same
325 value. Thus, in regions with high density of observations the \bar{h} and \tilde{h} estimates are
326 expected to converge. For instance, in the $3^\circ \times 3^\circ$ bin centered in 175°E 25°S the number

327 of XBT and Argo observations is large and the *in situ* observations are evenly distributed
328 between positive and negative η' values (Figure 2b). This example shows how the
329 climatological estimates converge when the sampling is homogeneous in each platform.
330 This is shown by the overlapping between the \bar{h} and \tilde{h} estimates obtained from each
331 platform respectively (Figure 2b). However, the \bar{h} and \tilde{h} estimates show a difference of
332 about 30 m between Argo and XBT, which cannot be explained as a sampling bias and
333 could result from biases in either observing platforms.

334 *b. Reduced Statistical Uncertainty*

335 As already discussed in the introduction, several studies have provided evidence
336 for a systematic bias in the XBT observations consistent with a FRE problem. Any
337 problem in the FRE equation leading to a systematic bias in the determination of the XBT
338 depth could be identified by analyzing the differences between climatologies \bar{h} , derived
339 from XBTs and Argo. This methodology has been applied to identify XBT biases over
340 long periods of time (Gouretski and Koltermann 2007; Wijffels et al. 2008). Argo
341 observations do not allow the estimation of climatologies with uncertainties required to
342 identify systematic biases with a magnitude of less than 20 m found by the previous
343 studies mentioned in the introduction. This limitation becomes more important for
344 characterization of the spatial extent of this bias during the relatively short 2000-2007
345 period. However, any systematic bias in the XBT observations could also be identified in
346 the pseudo-climatologies \tilde{h} . According to the least-squares method (e.g. Lawson and

347 Hanson, 1974) the standard error of \tilde{h} is related to the standard error of the climatological
 348 isotherm depth, \bar{h} , through the correlation coefficient, r :

$$349 \quad S(\tilde{h}) = \sqrt{(1-r^2) \left(1 + \frac{\overline{\eta'}}{\sigma_\eta}\right)} S(\bar{h}), \quad (6)$$

350 where $S(\)$ represents the standard error estimator, $\overline{\eta'}$ is the mean value of the η'
 351 observations, and σ_η is their standard deviation. This equation shows that the statistical
 352 uncertainty of the \tilde{h} estimates is reduced in the limit of $\overline{\eta'} \sim 0$, which corresponds to
 353 homogenous sampling. In other words, the standard errors are related by the $\sqrt{(1-r^2)}$
 354 factor, which is always less than 1, when the *in situ* observations are equally distributed
 355 between positive and negative values of SHA (i.e. $\overline{\eta'}=0$). Therefore, when correlations
 356 are high and sampling is homogeneous, the uncertainty of the pseudo-climatology \tilde{h} , is
 357 reduced with respect to the climatological isotherm depth \bar{h} . This feature of the
 358 methodology becomes more important in regions where the variability of the thermal
 359 structure of the upper ocean is large because σ_h is large. To conclude, in the limit of no
 360 correlation between h and η' , \tilde{h} converges to \bar{h} (5) and so do the standard errors (6),
 361 thus the methodology defaults to a conventional climatology.

362 **Results**

363 Global maps of \tilde{h} are estimated for isotherms from 5°C to 28°C (every 1°C) for
 364 XBT and Argo observations separately. In this section we describe the spatial features of
 365 the pseudo-climatologies and the differences between XBT and Argo estimates, focusing

366 on the 10°C and 20°C isotherms. The estimates of \tilde{h}_{10} obtained from XBTs and Argo
367 show similar spatial patterns consistent with large scale ocean features, such as gyres,
368 currents, and fronts (Figure 3). For example, the pseudo-climatologies capture the
369 deepening of the 10°C isotherm towards the centers of subtropical gyres. The largest
370 values of \tilde{h}_{10} are found in the North Atlantic, where the thermocline is deeper compared
371 with other basins. Frontal regions, such as the Gulf Stream and the North Atlantic
372 Current can also be identified from these fields. The XBT- and Argo-derived estimates
373 of \tilde{h}_{20} also show similar spatial patterns (Figure 4). Both XBT and Argo estimates
374 capture the location of the subtropical gyres in the Pacific and South Atlantic and the
375 east-west gradient of the depth of the 20°C isotherm in the equatorial oceans as well. The
376 Argo-derived \tilde{h} estimates are statistically significant over most of the global ocean. The
377 XBT-derived \tilde{h} are statistically significant in most regions, with the exception of
378 subpolar oceans, the northeastern tropical Pacific and south Atlantic subtropical gyre
379 where the density of observations is low.

380 Subtle differences are identified between the XBT- and Argo-derived pseudo-
381 climatologies for the 10°C and 20°C isotherm depth. For instance, the pseudo-
382 climatological 20°C isotherm is deeper in the center of the North Pacific subtropical gyre
383 in the XBT-derived estimates (Figure 4). These differences are revealed when the
384 respective climatologies are subtracted (Figure 5). A large fraction of the observed
385 regions of the ocean show differences that are not statistically significant, especially in
386 the Atlantic and Indian oceans. In regions where the difference can be estimated with 1-

387 sigma confidence, the differences between the estimates are mostly positive. This
388 suggests a systematic depth bias in the XBTs compared with the Argo estimates, as Argo
389 floats are assumed not to have systematic bias due to their higher accuracy in measuring
390 depths. The differences are considered statistically significant when the 1-sigma
391 confidence intervals of the XBT and Argo estimates do not overlap. The confidence
392 intervals are obtained from the standard error of the \tilde{h} estimator, which amplitude is
393 given by (6). The differences between estimates are not significant over large regions,
394 such as the North Pacific and North Atlantic subtropical gyres. This could be related to
395 larger variability in these regions and highlights the difficulty in identifying biases from
396 the highly energetic mesoscale field. Nonetheless, the number of bins where the implied
397 differences are statistically significant greatly exceeds the spatial coverage of previous
398 studies (e.g. Hanawa et al. 1995; Gouretski and Koltermann 2007; Wijffels et al. 2008).

399 Differences in the values of ε^{-1} , a parameter related to the stratification, are also
400 possible, but possibly restricted to higher order problems in the XBT FRE. Our analysis
401 shows very few bins with statistically significant differences in the correlation gain
402 (Figure 6). This is consistent with a FRE problem, since this type of error should not
403 introduce changes in the stratification. However, other systematic errors, such a
404 temperature bias, should not introduce biases in the estimation of the stratification as
405 well.

406 Furthermore, the differences between the XBT minus Argo isotherm depths are
407 larger for the 10°C isotherm (Figure 5a) compared with the 20°C isotherm (Figure 5b).
408 Differences increasing with depth could be linked with a depth dependent bias between

409 the two observing platforms. Globally, this depth dependence is clearly observed for all
 410 isotherms when the XBT minus Argo differences are analyzed as a function of isotherm
 411 depth (Figure 7). Most of the statistically significant differences are positive (red dots in
 412 Figure 7), indicating that XBT-derived pseudo climatologies are deeper than the Argo-
 413 derived estimates. Surprisingly, those differences that are not statistically significant
 414 (gray dots in Figure 7) fall inside the 2% errors bounds specified by Sippican (dashed-dot
 415 line in Figure 7). These XBT minus Argo differences (Figure 7) correspond to pseudo-
 416 climatology estimates obtained from regressions with correlation coefficients larger than
 417 0.8, and that do not differ by more 0.1 between XBT and Argo. The depth dependent
 418 bias implied by the XBT minus Argo differences is independent of the correlations
 419 between isotherm depth and SHA; however, the differences between pseudo-
 420 climatologies from these high correlations show reduced scatter.

421 The following linear fits are obtained when the global depth dependent XBT
 422 minus Argo differences, Δh , are adjusted using a least-squares best-fit line with no offset
 423 at the ocean surface:

$$424 \quad \Delta h_{XBT-Argo} = (0.030 \pm 0.002) \cdot h \quad (7),$$

425 or with an offset at the surface:

$$426 \quad \Delta h_{XBT-Argo} = (0.020 \pm 0.004)h + (4.7 \pm 1.3)m \quad (8).$$

427 The slope of these straight lines (solid and dashed lines in Figure 7, respectively)
 428 represents an estimate of a depth dependent error expressed as a percentage of the depth.

429 For instance, (7) indicates that XBTs overestimate the depths of the isotherms with
 430 respect to Argo depths by $(3.0 \pm 0.2)\%$ in the global ocean. The offset in (8) indicates that
 431 XBTs overestimate the isotherm depths by (4.7 ± 1.3) m plus a $(2.0 \pm 0.4)\%$ of the Argo
 432 depths. The uncertainty in the coefficients corresponds to the 1-sigma confidence
 433 intervals obtained from the least-squares fit. The implications of these results for detecting
 434 problems in the FRE are discussed in the following section. The slope and offset for the
 435 least-squares lines show values ranging from 0.1 % to 3.7% and from 0.1 m to 11.4 m
 436 respectively in different ocean basins and depending on the type of equation used to fit
 437 the differences (Table 1; Figure 8). Both lines fall outside the 2% error envelope
 438 specified by Sippican in all ocean basins (dashed-dot line in Figures 7 and 8).

439 **Discussion**

440 Our analysis of XBT and Argo observations for the 2000-2007 period provides
 441 evidence for a depth dependent bias consistent with an error in the FRE equation. The
 442 positive XBT minus Argo differences indicate that XBTs are actually falling slower than
 443 the specified terminal velocity in the H95-corrected FRE equation. The implied bias
 444 results in XBT depths that are too deep, therefore producing a warm temperature bias that
 445 increases with depths throughout most of the water column. The error associated with
 446 this bias is estimated from the slope of the least-squares fit of the XBT minus Argo
 447 differences (7):

$$448 \quad \gamma_1 = \frac{z_{H95} - z_{Argo}}{z_{Argo}} = 0.030 \pm 0.002, \quad (9)$$

449 where z_{H95} is the H95-corrected XBT depth, and z_{Argo} is considered here to be the true
450 depth. This depth-dependent error allows correction of z_{H95} as follows:

451
$$z_{Argo} = \frac{1}{(1 + \gamma_1)} z_{H95} \quad (10).$$

452 The global correction factor $(1 + \gamma_1)^{-1}$ of 0.97 in (10) is approximately the inverse of the
453 stretching factor $f_{H95} = 1.0336$, implemented after the H95 study. This strongly suggests
454 that the H95 correction could have introduced the bias during the 2000-2007 period.

455 The conclusion presented above is consistent with the analysis of Wijffels et al.
456 (2008), which showed that since 2000, XBTs are falling with a terminal velocity close to
457 the original Sippican values. Their comparison of CTD and XBT data showed that the
458 H95 study was done at a time when the terminal velocity (represented by the b coefficient
459 in the FRE) was faster than at any other time. This return of the terminal velocity values
460 back to the original Sippican values has been independently confirmed by field
461 intercomparisons (D. Snowden, personal communication). Our study not only confirms
462 the value of the FRE bias, but also provides evidence of its global extent, since we
463 identify approximately the same error in the H95-corrected XBT depths in all ocean
464 basins, with the exception of the North Pacific (Table 1). The apparent global extent of
465 the bias points to problems in the XBT instruments rather than the influence of regional
466 differences in ocean conditions, such as the effect of temperature on the hydrodynamic
467 drag.

468 Additionally, an offset at the surface is identified when the XBT minus Argo
 469 differences are fitted using a straight line with a constant term (8). Both XBT and Argo
 470 are unable to observe the upper few meters of the water column with precision. However
 471 surface offsets are still detectable because any systematic bias introduced in the initial
 472 seconds of the XBT descent results in a vertical shift of the entire temperature profile.
 473 The depth-dependent error, γ_2 , and offset, δ_2 , obtained from the least-squares fit allows to
 474 correct z_{H95} as follows:

$$475 \quad z_{Argo} = \frac{1}{(1 + \gamma_2)} (z_{H95} - \delta_2) \quad (11).$$

476 The values obtained for the γ_2 and δ_2 coefficients show more disparity between the
 477 different ocean basins (Table 1) compared with the γ_1 coefficient in correction (10).
 478 Overall, the values of the δ_2 offset are consistent with values reported by previous studies
 479 of 3.7 m (Bailey et al. 1989;), 4.2 m (Singer 1990), 2 to 10m (Kizu and Hanawa 2002), 2
 480 m (Reseghetti et al. 2007), and 4.5 m (D. Snowden, personal communication).

481 Surface offsets have received a great deal of attention and have been attributed to
 482 a wide range of transients resulting from the thermistor response, the recording system, or
 483 the hydrodynamics of the descent of the probe (Green 1984; Roemmich and Cornuelle
 484 1987; Hallock and Teague 1992; Kizu and Hanawa 2002; Reseghetti et al. 2007).
 485 Sippican recommends launching XBTs from a height H , of about 2.5 m to ensure that the
 486 entry speed is $\sqrt{2gH} \sim 6.5ms^{-1}$, equal to the terminal speed, and thus avoid
 487 hydrodynamical transients. In other words, the FRE assumes that the probe starts the
 488 descent with the terminal velocity implied by the b coefficient. The entry speed is

489 expected to be much larger for XBTs launched from cargo ships, because they are
490 typically dropped from the stern or the bridge, which are several meters above the ocean
491 surface. An initial velocity larger than the terminal velocity represents a faster b
492 coefficient during the initial descent and results in a negative offset at the surface. In
493 contrast, the *positive* 4.7 m offset suggested by our analysis is consistent with a probe
494 descending with an initial velocity closer to zero (Hallock and Teague 1992, Table 1),
495 thus unlikely to result from hydrodynamic transients.

496 A positive offset could also result from the finite time response of the temperature
497 sensor to sudden changes in temperature, which typically occur when the probe enters the
498 ocean and when it crosses the base of the mixed layer (e.g. Roemmich and Cornuelle
499 1987; Kizu and Hanawa 2002; Reseghetti et al. 2007). Different recording systems are
500 used in the different ocean basins, thus explaining why we find different values.
501 However, a comparison of the different acquisition systems (SEAS2000, Devil, Sippican)
502 indicates that they exhibit approximately the same offset (D. Snowden, personal
503 communication). In contrast, our analysis shows that considering a surface offset in the
504 least-squares fit of the XBT minus Argo differences leads to less robust estimates of
505 depth error, γ , and surface offset, δ (Table 1, columns 3 and 4). Briefly stated, the only
506 robust bias detected from our analysis is a 3% depth dependent error, with no evidence
507 for a robust surface offset. Addressing this problem is important because this surface
508 offset could introduce biases of up to 10% when estimating the depth of shallow mixed
509 layers becoming an important source of error. More research is needed to determine its

510 origin, and whether it is introduced when probe enters the ocean or when the probe
511 crosses the mixed layer.

512 **Conclusions**

513 A methodology is proposed to estimate climatologies of isotherm depths using a
514 combination of *in situ* and satellite observations. The methodology allows the estimation
515 of climatologies for relatively short periods reducing sampling problems by using
516 correlations with satellite-derived SHA fields. This represents an important advantage
517 compared with the analysis of nearby XBT/CTD, which is difficult to perform on a
518 global scale, and that has been the main methodology for identifying and characterizing
519 these biases up to date. Moreover, this methodology overcomes limitations in comparing
520 XBTs with in-situ hydrography directly, which require very large amounts of data to be
521 able to detect biases obscured by the highly energetic mesoscale field. The methodology
522 presented here avoids these limitations by taking advantage of the high temporal and
523 spatial resolution of satellite altimetry observations.

524 Comparison of XBT and Argo estimates of isotherm depth suggests a depth
525 dependent bias in XBT observations in all regions of the world ocean, which confirms the
526 global extent of a depth dependent error in the XBTs reported in previous studies
527 (Gouretski and Koltermann 2007; Wijffels et al. 2008). Moreover, our results show that
528 this error can be identified with 1-sigma statistical significance despite the
529 inhomogeneous sampling of the eddy variability by Argo and XBTs. The 3% depth error
530 identified here is also suggestive of a time-dependent bias in the XBTs, since it appears

531 that the H95 correction is no longer appropriate for current XBTs. This indicates that the
532 original FRE coefficients specified by Sippican would be adequate for the 2000-2007
533 period. The source of the time-dependent FRE bias remains unclear. However, the
534 global extent of the implied bias points to problems in the instrumentation, such as
535 changes in the terminal velocity of the XBTs, which are likely to result from variations in
536 the drag characteristics of the probes. The robust global extent of the bias points to
537 problems in the XBT instruments rather than the influence of regional differences in
538 ocean conditions. While there are several potential sources of near-surface errors due to
539 transients in the descent of the probe, our study shows that surface offsets are different
540 among ocean basins, thus unable to be explained by a systematic problem in the XBT
541 FRE. According to our results, returning to the original FRE coefficients is the only
542 correction that seems to be robust. This correction could bring the XBT dataset to
543 consistency with Argo during the 2000-2007 period.

544 XBTs remain the second most important source of upper ocean thermal data and
545 the most important source of temperature along transects. The FRE coefficients need to
546 be monitored on a continuous basis to identify future changes in the terminal velocity of
547 the XBT, which may avoid introducing spurious decadal signals in global heat storage.
548 The methodology presented here is especially well suited for this purpose because it
549 allows the comparison of XBT and Argo data over relatively short periods. High-density
550 transects, which are run four times per year, could provide the number of observations to
551 perform this type analysis over one or two year periods. Additionally, these transects

552 must coincide with regions of high density of Argo observations, such as the North
553 Pacific or the North Atlantic.

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632 **Figure list**

633 Figure 1 – Correlation coefficient between the altimetry-derived SHA and the depth of
634 the 10°C isotherm (h_{10}) from (a) Argo and (b) XBT profiles. Correlation coefficient
635 between the altimetry-derived SHA and the depth of the 20°C isotherm (h_{20}) from
636 (c) Argo and (d) XBT profiles. Stippling indicates regions where the correlation
637 coefficients are not significant with 67% confidence based on a chi-squared test. The
638 correlation coefficients between the Argo-derived isotherm depth and altimetry-derived
639 SHA are significant over most of the global ocean. The correlation coefficients between
640 XBT-derived isotherm depth and altimetry-derived SHA are significant over the major
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643 (h_{20}) and concurrent estimates of satellite-derived sea height anomaly (η') in a 3°×3° bin
644 centered at 169°W 4°S. (b) Dispersion diagram between in-situ observations of the depth of
645 the 10°C isotherm (h_{10}) and concurrent estimates of satellite-derived sea height anomaly (η')
646 in a 3°×3° bin centered at 175°W 25°S. Gray diamonds and black circles correspond to the
647 XBT-derived and Argo-derived estimates of isotherm depth respectively. The blue and the
648 red lines are the least-squares best-fit line between the satellite-derived sea height anomaly
649 and the XBT-derived and Argo-derived isotherm depth estimates respectively. Note that the
650 y-axis is inverted so deeper isotherm depths appear on the bottom of the scatter plot.....38

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653 \tilde{h}_{10} estimates are computed on 3°×3° bins using XBT or Argo data from 2000 to 2007

654 combined with altimetry-derived sea height anomaly fields. Stippling indicates regions
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 658 methodology described in the text using (a) Argo and (b) XBT temperature profiles
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 66040

661 Figure 5 – XBT minus Argo difference of the pseudo climatologies of the depth of the (a) 10°C
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 663 depths. The pseudo-climatologies correspond to the 2000 to 2007 period and are computed
 664 using XBT or Argo data combined with altimetry-derived sea height anomalies as described
 665 in the text. Stippling indicates regions where the difference between the estimates is not
 666 significant with 67% confidence.41

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 672 pseudo-climatological isotherm depth derived from Argo. Positive $h_{XBT} - h_{Argo}$ differences
 673 indicate that the XBT estimates result in deeper isotherms for the period 2000–2007. Only
 674 pseudo-climatologies obtained from regressions with correlation coefficients larger than 0.8
 675 and with a difference of less than 0.1 between XBTs and Argo are shown. Red dots

676 correspond to 1-sigma significant biases while gray dots are not significant with the same
677 confidence level. The dashed-dot lines indicate the 2% error bounds specified by the
678 manufacturer. The solid dashed line corresponds to the least-squares fit allowing for an
679 offset at the surface while the solid line is adjusted with no offset at the surface.43

680 Figure 8 – Scatter plot of the differences between the pseudo-climatological isotherm depth
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682 (c) North Pacific, (d) South Pacific, (e) Tropical Pacific, and (f) Indian oceans. See Figure 8
683 for more details.44

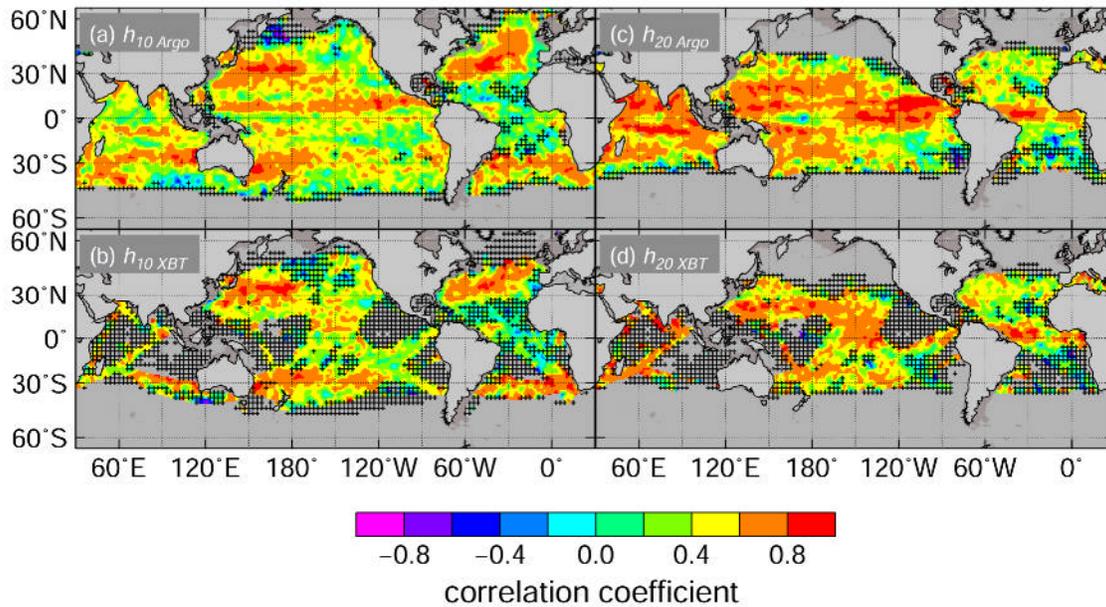
684 **Table list**

	$\Delta h_{\text{XBT-Argo}} = \gamma_1 z$	$\Delta h_{\text{XBT-Argo}} = \gamma_2 z + \delta_2$	
	γ_1 (%)	γ_2 (%)	δ_2 (m)
Global	3.0 ± 0.2	2.0 ± 0.4	4.7 ± 1.3
North Atlantic	2.6 ± 0.2	2.6 ± 0.5	0.1 ± 1.1
South Atlantic	3.7 ± 0.3	1.1 ± 0.6	11.4 ± 1.6
North Pacific	2.2 ± 0.3	1.7 ± 0.5	2.3 ± 1.3
South Pacific	3.2 ± 0.3	2.4 ± 0.6	2.6 ± 1.9
Tropical Pacific	3.6 ± 0.5	0.1 ± 1.0	8.1 ± 1.5
Indian Ocean	3.0 ± 0.3	2.0 ± 0.7	4.8 ± 2.9

685 **Table 1** – Corrections to the fall-rate equation obtained from least-squares fitting of the XBT
 686 minus Argo differences as a function of depth obtained in this study. The uncertainty in the
 687 coefficients corresponds to the 1-sigma confidence intervals obtained from the least-squares fit.

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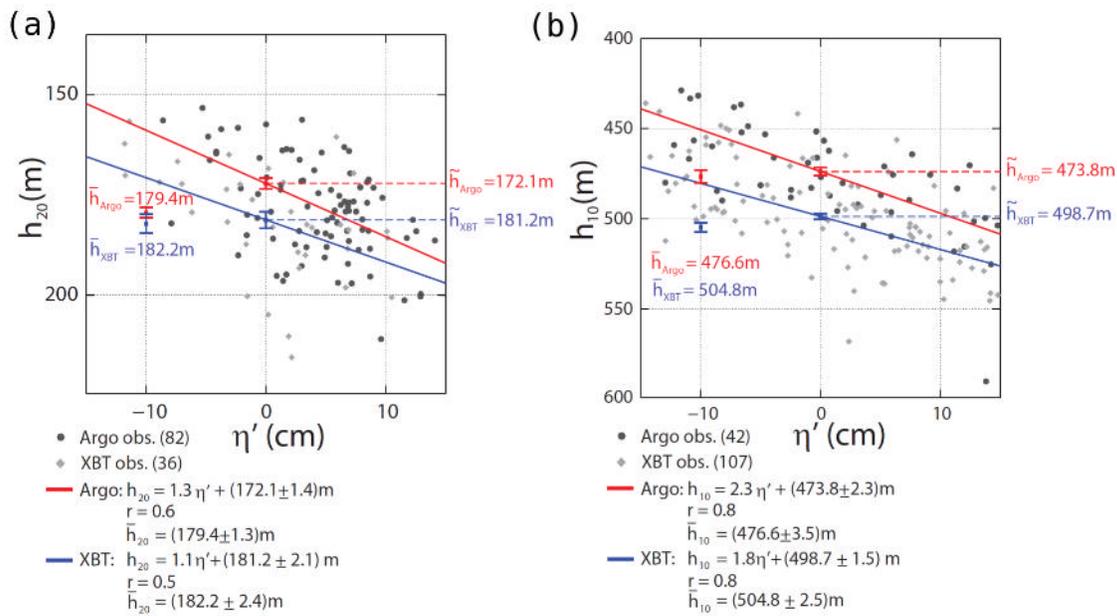
689 **Figures**



690

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699 of observations is largest.

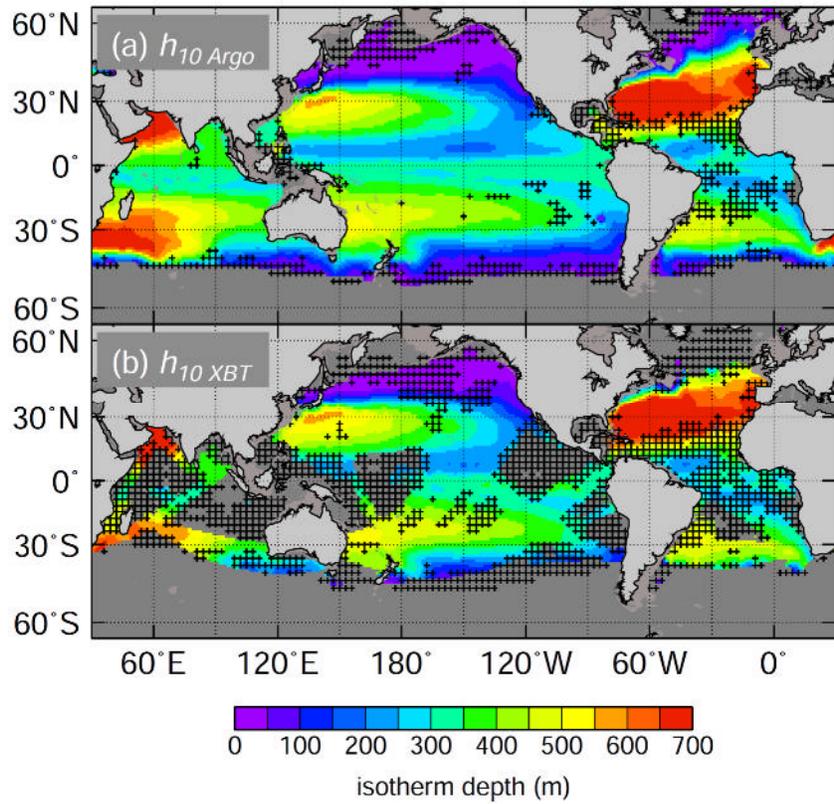
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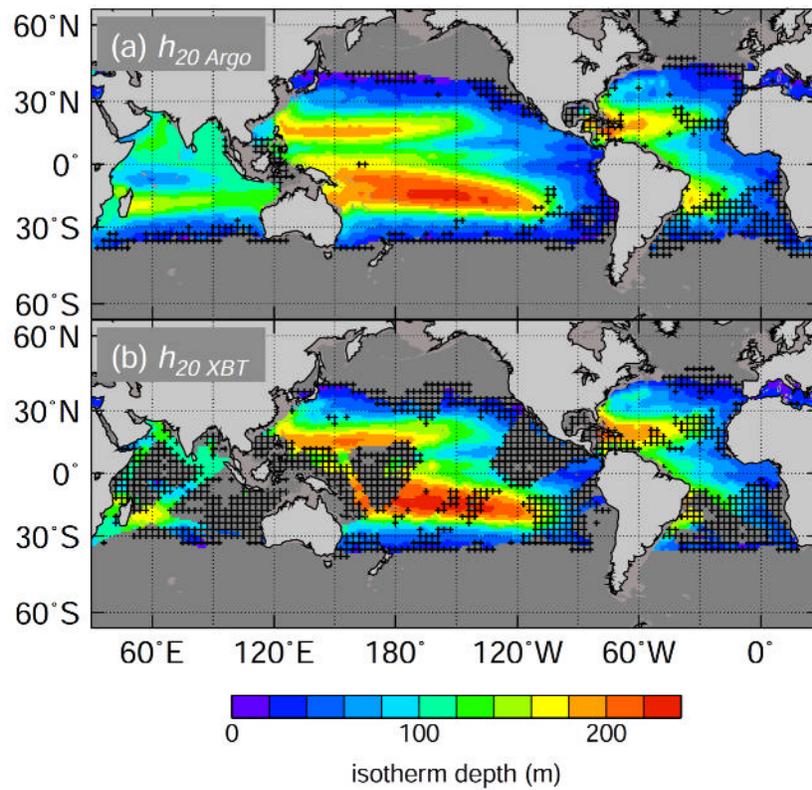
702 Figure 2 – (a) Dispersion diagram between in-situ observations of the depth of the 20°C isotherm
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 706 centered at $175^\circ \text{W } 25^\circ \text{S}$. Gray diamonds and black circles correspond to the XBT-derived and
 707 Argo-derived estimates of isotherm depth respectively. The blue and the red lines are the least-
 708 squares best-fit line between the satellite-derived sea height anomaly and the XBT-derived and
 709 Argo-derived isotherm depth estimates respectively. Note that the y-axis is inverted so deeper
 710 isotherm depths appear on the bottom of the scatter plot.

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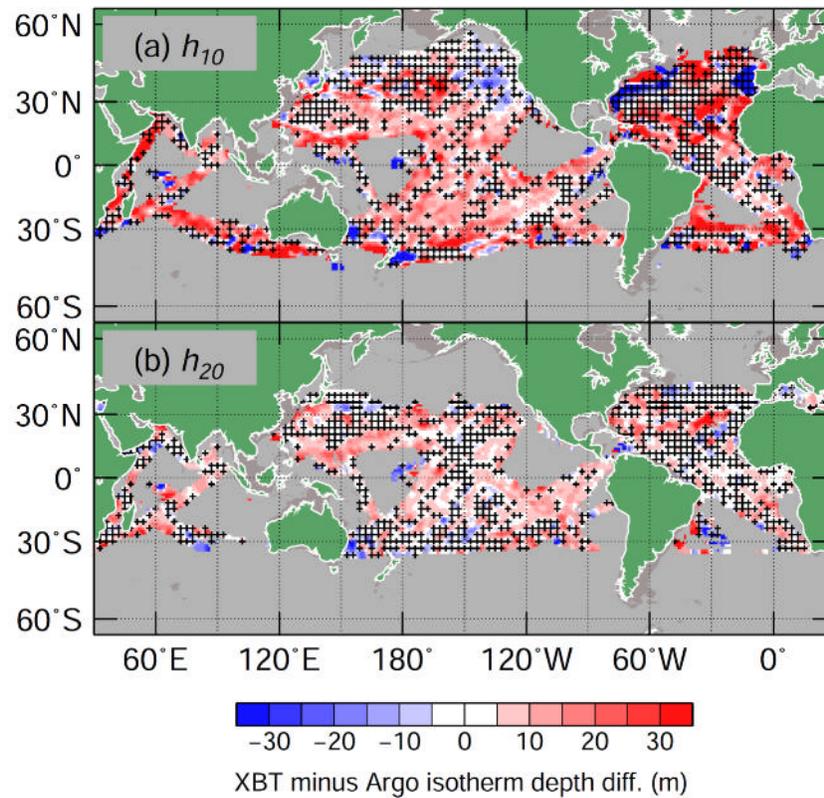
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718 observations is low.



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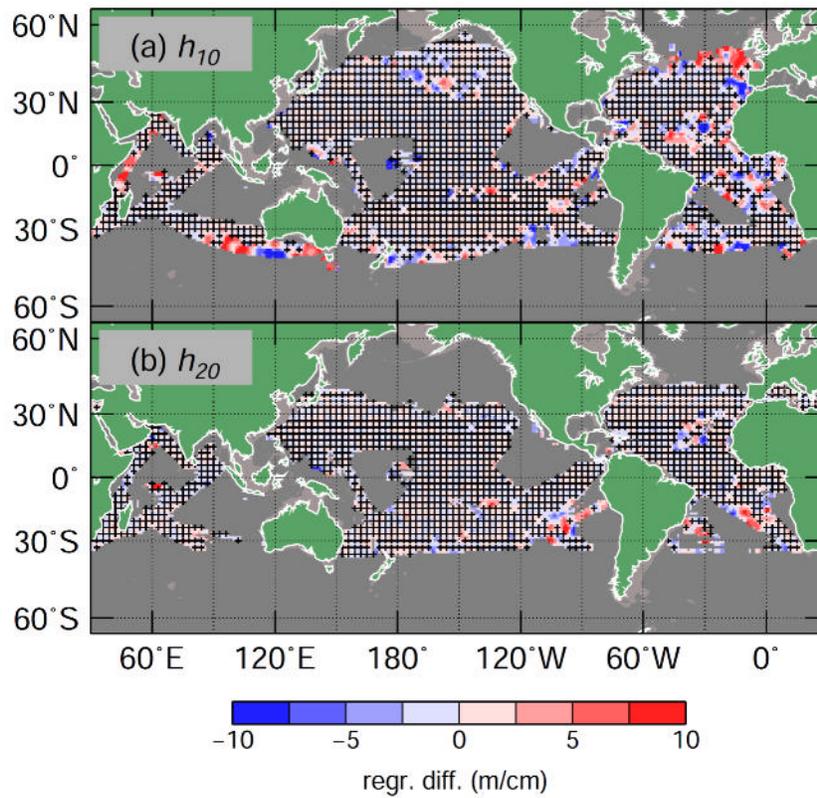
721 Figure 4 – Pseudo-climatologies corresponding to the 20°C isotherm computed following the
722 methodology described in the text using (a) Argo and (b) XBT temperature profiles combined
723 with altimetry-derived sea height anomaly fields. See Figure 3 for more details.



725

726 Figure 5 – XBT minus Argo difference of the pseudo climatologies of the depth of the (a) 10°C
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 728 depths. The pseudo-climatologies correspond to the 2000 to 2007 period and are computed using
 729 XBT or Argo data combined with altimetry-derived sea height anomalies as described in the text.
 730 Stippling indicates regions where the difference between the estimates is not significant with 67%
 731 confidence.

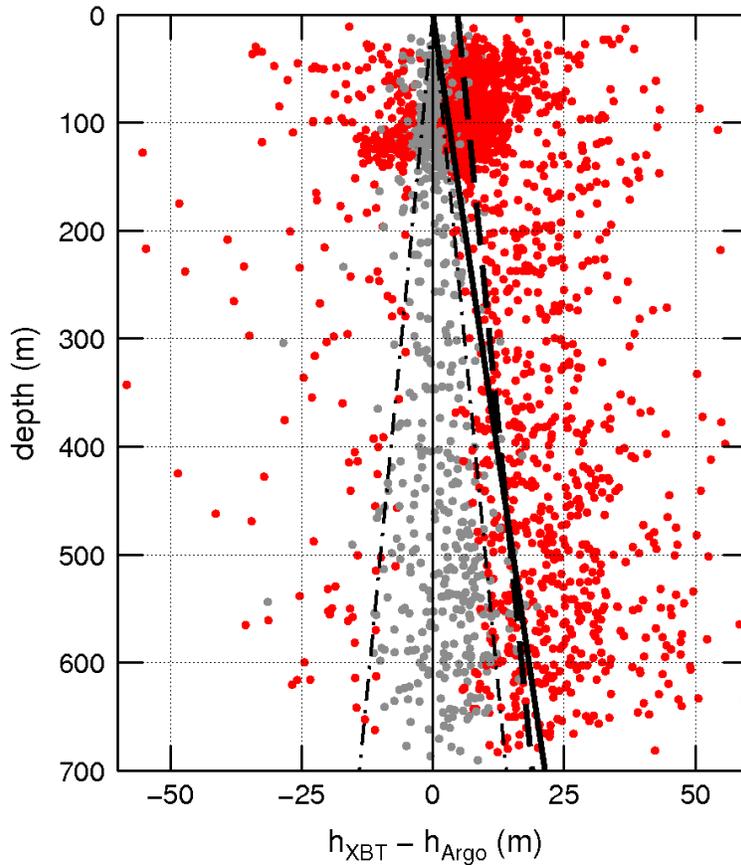
732



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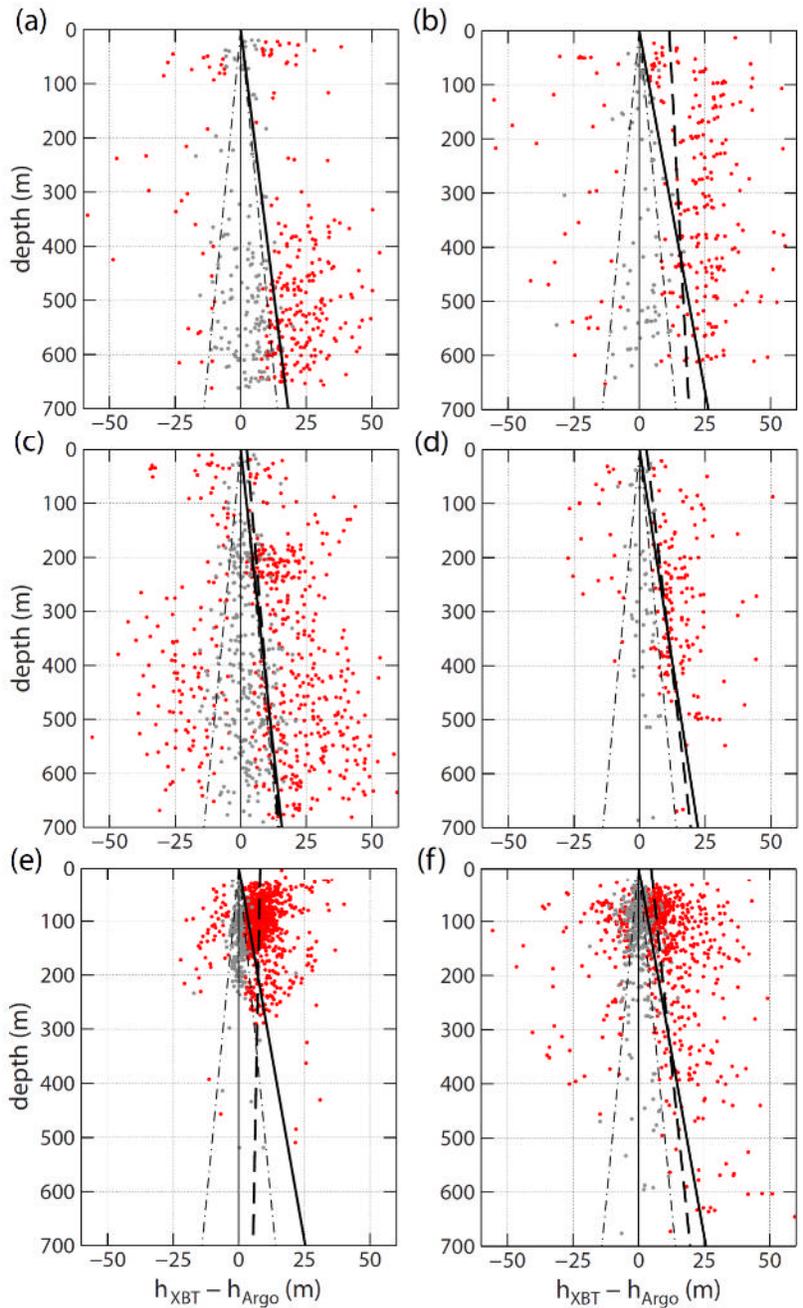
734 Figure 6 – XBT minus Argo difference in regression gain of the depth of the (a) 10°C and the (b)
735 20°C isotherms. Stippling indicates regions where the difference between the estimates is not
736 significant with 67% confidence.

737



738

739 Figure 7 – Scatter plot of the differences between the pseudo-climatological isotherm depth
 740 estimates as a function of depth for the global ocean. The depth axis corresponds to the pseudo-
 741 climatological isotherm depth derived from Argo. Positive $h_{XBT} - h_{Argo}$ differences indicate that
 742 the XBT estimates result in deeper isotherms for the period 2000–2007. Only pseudo-
 743 climatologies obtained from regressions with correlation coefficients larger than 0.8 and with a
 744 difference of less than 0.1 between XBTs and Argo are shown. Red dots correspond to 1-sigma
 745 significant biases while gray dots are not significant with the same confidence level. The dashed-
 746 dot lines indicate the 2% error bounds specified by the manufacturer. The solid dashed line
 747 corresponds to the least-squares fit allowing for an offset at the surface while the solid line is
 748 adjusted with no offset at the surface.



749

750 Figure 8 – Scatter plot of the differences between the pseudo-climatological isotherm depth
 751 estimates as a function of depth for different regions: (a) North Atlantic, (b) South Atlantic, (c)
 752 North Pacific, (d) South Pacific, (e) Tropical Pacific, and (f) Indian oceans. See Figure 8 for
 753 more details.