

## A climate sensitivity estimate using Bayesian fusion of instrumental observations and an Earth System model

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[1] Current climate model projections are uncertain. This uncertainty is partly driven by the uncertainty in key model parameters such as climate sensitivity ( $CS$ ), vertical ocean diffusivity ( $K_v$ ), and strength of anthropogenic sulfate aerosol forcing. These parameters are commonly estimated using ensembles of model runs constrained by observations. Here we obtain a probability density function (pdf) of these parameters using the University of Victoria Earth System Climate Model (UVic ESCM) - an intermediate complexity model with a dynamic three-dimensional ocean. Specifically, we run an ensemble of UVic ESCM runs varying parameters that affect  $CS$ , ocean vertical diffusion, and the effects of anthropogenic sulfate aerosols. We use a statistical emulator that interpolates the UVic ESCM output to parameter settings where the model was not evaluated. We adopt a Bayesian approach to constrain the model output with instrumental surface temperature and ocean heat observations. Our approach accounts for the uncertainties in the properties of model-data residuals. We use a Markov chain Monte Carlo method to obtain a posterior pdf of these parameters. The mode of the climate sensitivity estimate is 2.8°C, with the corresponding 95% credible interval ranging from 1.8 to 4.9°C. These results are generally consistent with previous studies. The  $CS$  pdf is sensitive to the assumptions about the priors, to the effects of anthropogenic sulfate aerosols, and to the background vertical ocean diffusivity. Our method can be used with more complex climate models.

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### 1. Introduction

[2] Climate hindcasts and projections are strongly affected by two key climate model parameters: climate sensitivity ( $CS$ ) and vertical ocean diffusivity. Meridional overturning circulation, global temperature, and ocean heat accumulation

that produces thermosteric sea level rise are good examples of climate variables that depend on these parameters [Goes *et al.*, 2010; Knutti *et al.*, 2002]. Better characterization of the uncertainty in these parameters is thus critical for future climate prediction.

[3] Climate sensitivity is defined as the equilibrium near-surface temperature response to a doubling of atmospheric CO<sub>2</sub>.  $CS$  is a measure of climate feedbacks that amplify or dampen the direct response of near-surface temperature to radiative forcings [Andronova *et al.*, 2007]. Vertical ocean diffusivity is a parameter that influences heat uptake by the ocean. It parameterizes mixing processes below the grid scale of climate models. For the same climate sensitivity, at higher diffusivities the atmosphere will reach the equilibrium temperature specified by  $CS$  more slowly, due to more heat flux into the deep ocean [National Academy of Sciences, 1979].

[4] In order to estimate these parameters from climate models and observations, one needs to know past climate forcings. Both parameter estimation studies and simple theoretical considerations show that assumptions about these forcings influence climate sensitivity estimates and the uncertainty surrounding them [Andreae *et al.*, 2005; Tanaka

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*et al.*, 2009; *Urban and Keller*, 2010]. For example, *Andreae et al.* [2005] use a zero-dimensional climate model to illustrate that when they assume no aerosol effects, a climate sensitivity of just 1.3°C is needed to explain the observed 1940–2000 warming. On the other hand, aerosol forcing of  $-1.7 \text{ Wm}^{-2}$  (a value that is within the IPCC range [Forster *et al.*, 2007]) requires a climate sensitivity of more than 10°C [Andreae *et al.*, 2005]. Out of the main climate forcings, the forcings due to aerosols are especially uncertain. A large part of this uncertainty is due to anthropogenic sulfate aerosols [Forster *et al.*, 2007].

[5] Parameters controlling climate sensitivity, vertical diffusion in the ocean, and strength of anthropogenic sulfate aerosols are commonly estimated using model runs and observations [Knutti *et al.*, 2002, 2003; Forest *et al.*, 2002, 2006; Drignei *et al.*, 2008; Tomassini *et al.*, 2007; Edwards *et al.*, 2007; Sanso and Forest, 2009]. Typically, an ensemble of model runs is used where the key parameters are systematically varied. The outputs from these runs are then compared with the observations, and the posterior probability distribution functions (pdfs) for model parameters are derived.

[6] One conceptually simple methodology selects only the model runs that are consistent with the observations using a broad, heuristic approach [Knutti *et al.*, 2003]. In this framework all parameter combinations that pass the consistency criterion are assigned a uniform probability, while those that do not pass it receive a zero probability. These probabilities are then used to construct the posterior pdfs.

[7] A more complex approach uses Bayesian statistics. This approach requires: (1) a model ensemble, (2) observations, (3) a statistical model that relates climate model output to the observations, and (4) prior information about the model parameters (priors). In this framework, each parameter combination is associated with a likelihood that depends on how well the corresponding model output matches the observations [Tomassini *et al.*, 2007; Sanso and Forest, 2009]. The likelihood,  $L(Y|\Theta)$ , describes the degree of belief that the physical observations  $Y$  came from a climate model and a statistical model (describing the properties of data-model residuals) with unknown parameters  $\Theta$ . Once the statistical model is defined, the likelihood  $L(Y|\Theta)$  can be calculated from the residuals between the model output and the observations. In the Bayesian framework, the posterior probability of the unknown parameters given the observations is proportional to  $L(Y|\Theta)$ , and to the prior probability of the parameters:

$$p(\Theta|Y) \propto L(Y|\Theta) \times p(\Theta). \quad (1)$$

[8] While the posterior probability  $p(\Theta|Y)$  can be evaluated on a grid of parameter values, this can become too computationally expensive if the parameter space is multi-dimensional. In such cases Markov Chain Monte Carlo (MCMC) methods [Metropolis *et al.*, 1953; Hastings, 1970] can be used. The MCMC generates a sequence of parameter values (a Markov chain) which may be treated approximately as samples from the posterior distribution. Hence, virtually any property of the posterior distribution can be approximated by a corresponding sample property of this sequence.

[9] Intermediate Complexity Earth System models are frequently used for this analysis [Forest *et al.*, 2002, 2006; Knutti *et al.*, 2003; Tomassini *et al.*, 2007; Sanso and Forest, 2009]. The appeal of these models is that they can be run at many parameter settings with relative ease. At the same time these models still represent many relevant physical processes. While the models can be run hundreds of times, many more runs at arbitrary parameter values are needed for the MCMC sampling. To approximate model output at these values, emulators (statistical approximators of climate models) can be used [e.g., Drignei *et al.*, 2008; Holden *et al.*, 2010; Edwards *et al.*, 2011]. The emulators draw on information about model outputs at known parameter settings to interpolate the output to any desired parameter setting.

[10] In this study, we use the University of Victoria Earth System Climate Model (UVic ESCM) to estimate these important climate parameters. We constrain the ensemble of model runs with atmospheric surface temperature and ocean heat content observations to present probability distribution functions for key model parameters controlling the processes described above: climate sensitivity  $CS$ , background vertical ocean diffusivity  $K_{bg}$ , and a scaling parameter for the direct effects of anthropogenic sulfate aerosols  $A_{sc}$ . The use of the full 3D ocean allows for the representation of the non-linear effects of  $K_{bg}$  on ocean dynamics and currents (e.g., on the Meridional Overturning Circulation). We present posterior joint and marginal pdfs for the parameters, and explore the sensitivity of the results to prior assumptions.

## 2. Earth System Model, Its Emulator, and Observational Constraints

### 2.1. Model Description

[11] We use the University of Victoria Earth System Climate Model (UVic ESCM) [Weaver *et al.*, 2001] for our analysis. The atmospheric component is a one-layer energy-moisture balance model, with winds prescribed using the NCAR/NCEP climatology. The oceanic component is a three-dimensional model MOM2 [Pacanowski, 1995]. Both the atmospheric and the oceanic components have horizontal resolution of  $1.8^\circ$  (lat)  $\times$   $3.6^\circ$  (lon). The ocean has 19 depth levels. The model also includes terrestrial vegetation and carbon cycle [Cox, 2001], oceanic biogeochemistry based on work by Schmittner *et al.* [2005], and thermodynamic sea ice. We use the modified 2.8 version of the model. Specifically, we use a newer solar forcing, and include new transient forcings. The new forcings are described in section 2.3.

### 2.2. Model Parameters

#### 2.2.1. Climate Sensitivity (CS)

[12] Climate sensitivity is defined as the equilibrium response of global average near-surface temperature to a doubling of atmospheric  $\text{CO}_2$ . Climate sensitivity is a diagnosed parameter in the UVic ESCM. We vary  $CS$  through an additional parameter  $f^*$  that perturbs local outgoing longwave radiation:

$$Q_{PLW}^* = Q_{PLW} + f^*(T_t - T_0). \quad (2)$$

[13] Here  $T_0$  is temperature at equilibrium (i.e. at the start of the transient run),  $T_t$  is a temperature at time  $t$ ,  $Q_{PLW}$  is the planetary outgoing longwave radiation as calculated in the

**Table 1.** Prior Ranges for the Parameters Used in the NON-UNIF Experiment<sup>a</sup>

Parameter	Units	Lower Bound	Upper Bound	Prior Form
$K_{bg}$	$\text{cm}^2 \text{s}^{-1}$	0.1	0.5	Lognormal(−1.55, 0.59)
$CS$	$^{\circ}\text{C}$ per $\text{CO}_2$ doubling	1.1	11.2	$NIG(\alpha = 1.8, \delta = 2.3, \beta = 1.2, \mu = 1.7) \times$ $NIG(\alpha = 1.9, \delta = 3.3, \beta = 1.0, \mu = 1.3)$
$A_{sc}$	unitless	0	3	uniform
$\sigma_T$	$^{\circ}\text{C}$	0.01	inf	uniform
$\sigma_{OHC}$	$1 \times 10^{22} \text{ J}$	0.01	inf	uniform
$\rho_T$	unitless	0.01	0.99	uniform
$\rho_{OHC}$	unitless	0.01	0.99	uniform
$b_T$	$^{\circ}\text{C}$	−0.51	0.50	uniform

<sup>a</sup>Subscript  $T$  refers to the temperature data, and  $OHC$  refers to the ocean heat content data.

standard 2.8 version of the model and  $Q^*_{PLW}$  represents the modified outgoing longwave radiation. This approach is similar to that of *Matthews and Caldeira* [2007] and *Zickfeld et al.* [2009], but here the temperature terms are functions of latitude and longitude.

[14] While  $f^*$  is the input parameter to the model, we want to know the  $CS$  values for each ensemble model run (section 2.3). We determine the relationship between  $f^*$  and  $CS$  using a small number of  $\text{CO}_2$  doubling experiments with varying  $f^*$  values at  $K_{bg} = 0.1 \text{ cm}^2 \text{ s}^{-1}$ . The runs continue for 2250 years to capture the equilibrium response of the model to  $\text{CO}_2$ . The  $CS$  is diagnosed as the average global temperature during the last 50 years of the runs minus the 50 year average prior to doubling. This mapping neglects a potential dependency of  $CS$  on  $K_{bg}$  at the same value of  $f^*$ . We adopt a prior range for  $CS$  from 1.1 to 11.2 (Table 1).

### 2.2.2. Background Vertical Ocean Diffusivity ( $K_{bg}$ )

[15] The rate at which surface temperatures adjust to radiative forcings is controlled by the rate at which heat is absorbed by the ocean. The vertical mixing of heat in the ocean is parameterized in UVic ESCM by a vertical diffusivity parameter  $K_v$ , which has contributions from tidal and background diffusivities [*Schmittner et al.*, 2009]:

$$K_v = K_{tidal} + K_{bg}. \quad (3)$$

$K_{tidal}$  uses the parameterization of *St. Laurent et al.* [2002] following the methodology of *Simmons et al.* [2004]. The background diffusivity  $K_{bg}$  is assumed to be globally uniform. We vary  $K_{bg}$  to obtain different vertical ocean diffusivities ( $K_v$ ), while keeping standard parameters for  $K_{tidal}$ . In our model,  $K_{bg}$  largely determines the total diffusivity in most areas of the pelagic pycnocline since the tidal component is small in those areas [*St. Laurent et al.*, 2002; *Schmittner et al.*, 2009]. As in work by *Schmittner et al.* [2009] and *Goes et al.* [2010], the model is modified to limit  $K_v$  to  $\geq 1 \text{ cm}^2 \text{ s}^{-1}$  in the Southern Ocean below 500 m for better agreement with observations. Following *Goes et al.* [2010], we adopt the prior range for  $K_{bg}$  from 0.1 to  $0.5 \text{ cm}^2 \text{ s}^{-1}$  (Table 1).

### 2.2.3. Anthropogenic Aerosol Scaling Factor ( $A_{sc}$ )

[16] Direct anthropogenic sulfate effects are modeled through spatially resolved sulfate albedos  $\Delta a_s$  following *Matthews et al.* [2004] and *Charlson et al.* [1991] according to:

$$\Delta a_s = A_{sc} \frac{\beta \tau (1 - \alpha_s)^2}{\cos(Z_{eff})}. \quad (4)$$

Here  $\beta = 0.29$  is the upward scattering parameter,  $\tau$  is the aerosol optical depth field,  $\alpha_s$  is surface albedo, and  $Z_{eff}$  is the effective solar zenith angle. The strength of anthropogenic sulfate aerosol effects is modulated via the scaling parameter ( $A_{sc}$ ). This parameterization does not account for the indirect effects of the sulfates on clouds. However, the indirect effects were found to be roughly proportional to the direct effects on major components of the Earth's radiation budget and climate on the global scale under idealized climate in a study by *Bauer et al.* [2008]. We use the prior range for  $A_{sc}$  from 0 to 3 (Table 1).

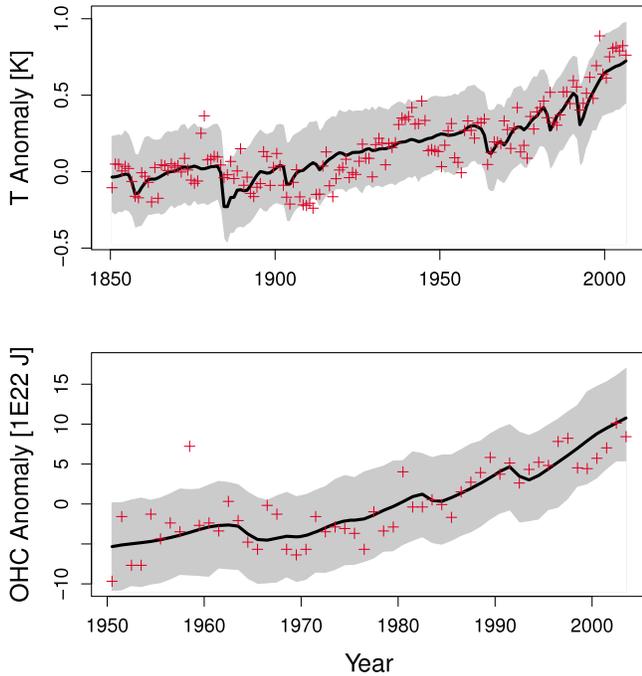
## 2.3. Hindcast Model Runs

[17] We run an ensemble of UVic ESCM model runs where we systematically vary the three parameters over their prior ranges. Specifically,  $K_{bg}$  is varied on a uniform grid with values of (0.1, 0.2, 0.3, 0.4, 0.5)  $\text{cm}^2 \text{ s}^{-1}$ . We sample  $CS$  at (1.14, 1.64, 2.15, 2.62, 3.11, 3.98, 5.36, 6.51, 8.20, 11.2)  $^{\circ}\text{C}$ . The samples for  $A_{sc}$  are (0, 0.75, 1.5, 2.25, 3). These values form a quasi-cubic grid.

[18] We spin the model up from observed data fields for 3,500 years with forcings set at year 1800 values. The transient runs continue from year 1800 to the present using historic radiative forcings. Volcanic aerosols, anthropogenic sulfate aerosols, changes in solar constant, and additional greenhouse gases such as  $\text{CH}_4$ ,  $\text{N}_2\text{O}$  and CFCs, are implemented following *Goes et al.* [2010]. Specifically, the volcanic radiative forcing anomalies are from *Crowley* [2000a, 2000b] for the period from 1800–1850, and from *GISS* [2007] and *Sato et al.* [1993] for years 1850 to 2000. We update the solar forcing using the data of *Krivova et al.* [2007]. The atmospheric  $\text{CO}_2$  concentration forcing is from *Etheridge et al.* [1998] and *Keeling et al.* [2004], complemented by the RCP8.5 scenario data after year 2002 [*Moss et al.*, 2010; *Riahi et al.*, 2007].

## 2.4. Observational Constraints

[19] We use two observational constraints. The first is global average atmospheric surface/ocean surface temperatures ( $T$ ) from the HadCRUT3 data set of the Hadley Center [*Brohan et al.*, 2006]. These observations are defined as anomalies with respect to the 1850–1899 period average. The observations cover the time period from 1850 to 2006 (Figure 1). The second constraint is global total ocean heat content ( $OHC$ ) in the 0–700 m layer [*Domingues et al.*, 2008]. These observations span the period from 1950 to 2003, and are calculated as anomalies with respect to the whole observation period (Figure 1). Modeled temperature



**Figure 1.** Probabilistic model hindcasts (grey shaded area), maximum posterior probability model output (‘best fit’, black line), and corresponding observations (red crosses) for the NON-UNIF assimilation experiment: (top) global average atmospheric surface temperature anomaly with respect to 1850–1899 mean [K] with corresponding observations of above surface/ocean surface temperatures from the HadCRUT3 data set [Brohan *et al.*, 2006]; (bottom) upper ocean (0–700 m) heat content anomaly with respect to 1950–2003 mean [ $1 \times 10^{22}$ J], and observations from Domingues *et al.* [2008]. The grey area denotes the 95% credible intervals for model output taken from a 1000-member subsampled MCMC chain, with corresponding AR1 error processes (and bias terms for temperature) added. For the AR1 process simulations, the  $\sigma$  and  $\rho$  parameters were taken from the corresponding chain member. For the best fit model output for temperature, the maximum posterior probability model output was combined with the corresponding bias term.

and ocean heat content are converted to anomalies to be consistent with the observational constraints.

## 2.5. Gaussian Process Emulator

[20] The MCMC sampling requires a large number of model runs (>10000) at arbitrary parameter values. Since it is computationally infeasible to run UVic ESCM at that many parameter settings, we use a statistical emulator that can approximate the model outputs at any parameter value. We adopt Gaussian Process (GP) emulation. This technique was previously used to approximate climate models by Bhat [2010], Sanso and Forest [2009] and Rougier *et al.* [2009]. We emulate model output as a function of climate parameters separately for temperature and for ocean heat content. For each tracer, we develop separate emulators for each time step during the years for which the observations are available (section 2.4). Thus, we build a total of 157 emulators for temperature, and 54 for the ocean heat content.

[21] We define model output of tracer  $k$  at time  $t$  as  $f_{t,k}(\theta)$  where  $\theta$  is a vector of model parameters ( $K_{bg}$ ,  $CS$ ,  $A_{sc}$ ). The  $f_{t,k}(\theta)$  is only defined on a discrete set of parameter values where the model was run. The purpose of the emulator is to estimate a function  $\tilde{f}_{t,k}(\theta)$  approximating model output on the continuous parameter ranges specified in Table 1. In the following discussion we will consider the emulator for atmospheric surface temperature at time  $t_0$ . The emulators for all other times and for the second tracer (ocean heat content) follow a similar statistical model. The indices  $t$  and  $k$  will thus be dropped from the rest of the emulator description.

[22] The emulator is developed in linearly rescaled coordinates with transformed parameters  $\theta' = (K'_{bg}, CS', A'_{sc})$  each taking on a range from zero to unity. The emulator approximates the climate model output as:

$$\tilde{f}(\theta') = P(\theta') + Z(\theta'), \quad (5)$$

where  $P$  is a quadratic polynomial in model parameters, and  $Z$  is a zero-mean Gaussian Process with an isotropic covariance function. Specifically, the covariance between  $Z$  at parameters  $\theta'_i$  and  $\theta'_j$  is modeled as  $mC(i, j)$  where  $m$  is a scale multiplier and  $C$  is defined by:

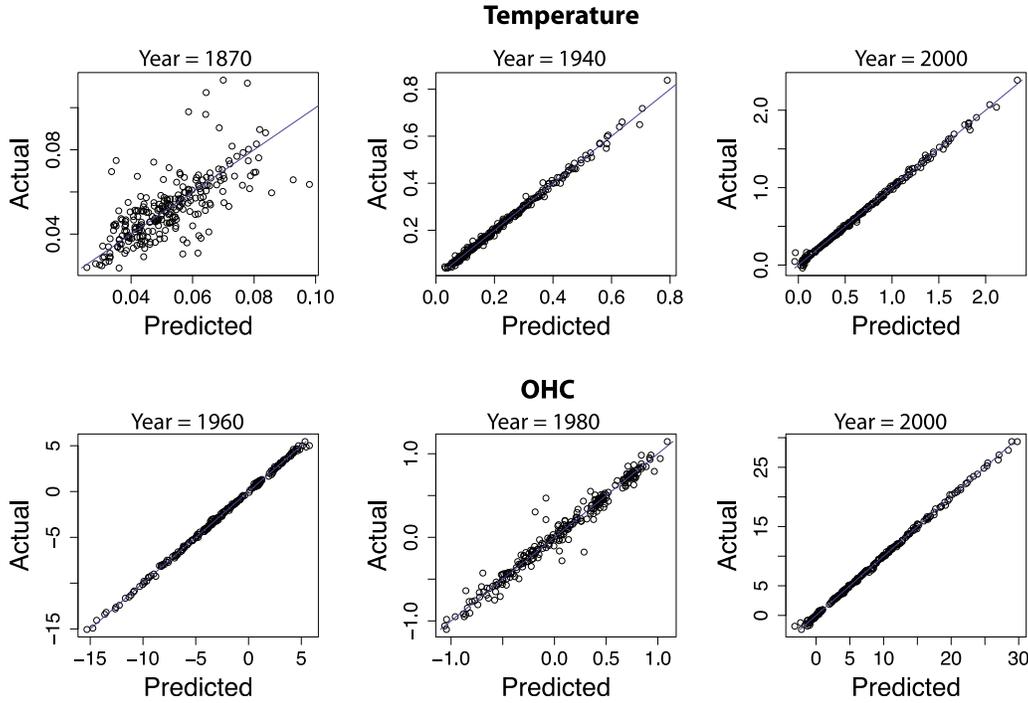
$$C(i, j) = \exp\left(\frac{-D_{ij}}{l}\right). \quad (6)$$

Here  $D_{ij}$  is the Euclidean distance between the two model parameter settings and  $l$  is a range parameter. Based on exploratory data analysis, we choose  $l = 0.6$ . This formulation ensures that model output at nearby parameter settings is highly correlated (i.e. model output is a smooth function of the parameters). We choose a nugget variance  $\sigma_\epsilon^2$  of zero. This implies that the emulator is equal to model output at the points of the ensemble design grid.

[23] We estimate the polynomial parameters and  $m$ . The polynomial parameters are the generalized linear squares estimates adjusting for the covariance function of the spatial process. They have a closed form solution that follows a standard formulation in Universal Kriging.  $m$  is likewise found by maximum likelihood given the parameter  $\lambda = \sigma_\epsilon^2/m = 0$ , and it has a closed form solution given  $\lambda$  as well (D. Nychka, personal communication, 2011). The optimized parameters provide the Best Linear Unbiased Estimate (BLUE) of  $\tilde{f}(\theta')$  (R. Furrer *et al.*, Package ‘fields’ manual, 2010, retrieved from <http://www.image.ucar.edu/Software/Fields/>).

[24] Emulators for other times and variables have different  $P$  and  $m$ . Henceforth all the emulators for all time steps and both tracers will be collectively referred to as the “emulator”.

[25] The emulator was extensively tested using the leave-one-out cross validation analysis. The emulator is found to perform adequately well (e.g., Figure 2) during the times when the variability of model output across the parameter space is high. The cross-validation errors are larger in the relative sense during the times close to the midpoints for the averaging periods for the anomalies (i.e. year 1870 for temperature, and 1980 for ocean heat content). At such times the signal is small and the model output is not a smooth function of the parameters, therefore it is impossible to accurately predict it based on the information from the



**Figure 2.** (top) Scatterplot of the temperature anomaly (with respect to the 1850–2006 mean, [K]) emulator predictions vs. actual model output values for years 1870, 1940, and 2000. Specifically, each of the parameter combinations of the ensemble was taken out one at a time, and the emulator was trained on the remaining 249 ensemble members. Then the emulator was used to predict the missing value. The 1:1 line is also shown. Note that Y axis limits are different for each subplot. (bottom) Same for the ocean heat content anomalies (with respect to the 1950–2003 mean, [ $1 \times 10^{22}$  J]), for years 1960, 1980, and 2000. The emulator performance, of course, will be different for other times not shown here.

remaining runs. We are unaware of any improvement in emulation techniques that could overcome this problem. We note that in this case the emulator errors are very low in the absolute sense and they are not expected to affect the estimation results. Overall, based on the cross-validation analysis, we are confident that the emulator provides a reasonable tool to interpolate model output.

### 3. Statistical Model and Markov Chain Monte Carlo

[26] We use a Bayesian parameter estimation method. In order to be able to evaluate the likelihood of observations given the unknown parameters  $L(Y|\Theta)$ , we need a statistical model that defines the relationship between the model (and the emulator) output and the observations. We refer to the emulator output by  $\tilde{f}_{t,k}(\theta)$  (for time  $t$ , tracer  $k$ , and parameter combination  $\theta$ ). The observations are denoted by  $y_{t,k}$ . We denote each observational time series by  $\mathbf{y}_k = y_{1,k}, \dots, y_{N_k,k}$  where  $N_k$  is the number of observations for tracer  $k$ . The set of all observations is referred to as  $Y = (\mathbf{y}_T, \mathbf{y}_{OHC})$ .

[27] We assume that the discrepancy between the emulator and the observations is due to the time constant bias  $b_k$  and time-varying error  $\epsilon_{t,k}$ . Thus, our statistical model is:

$$y_{t,k} = \tilde{f}_{t,k} + b_k + \epsilon_{t,k}. \quad (7)$$

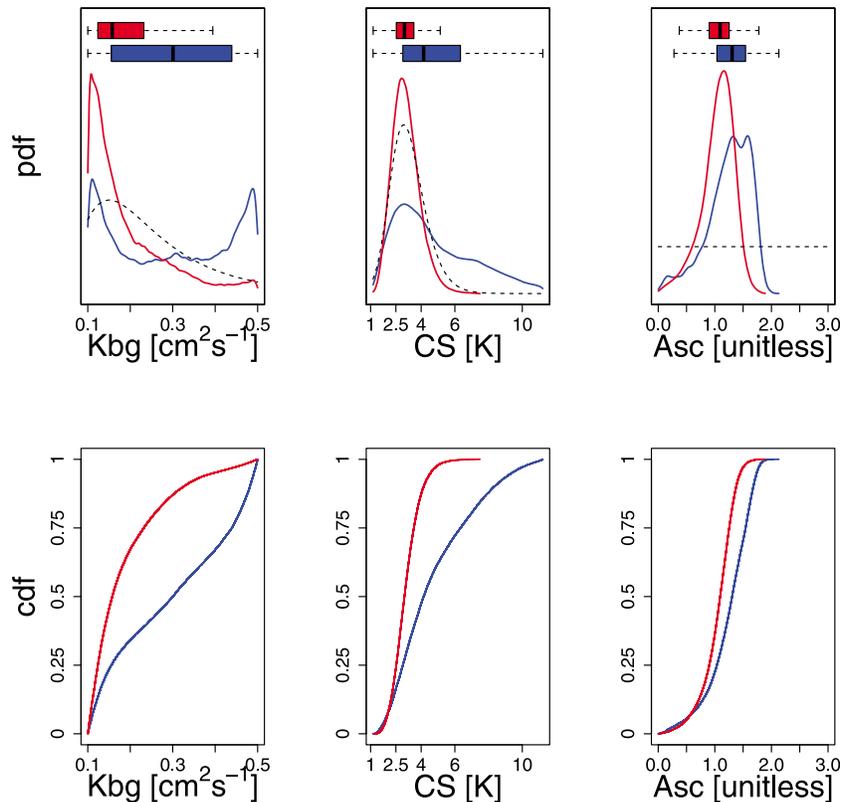
$\epsilon_{t,k}$  results from (1) model error, (2) natural climate variability, (3) emulator error, and (4) observational error. We

assume that  $\epsilon_{t,k}$  is an autoregressive process of order 1 (AR1) with unknown AR1 parameters  $\sigma_k^2$  and  $\rho_k$ .  $\sigma_k^2$  represents the variance of the AR(1) innovations while  $\rho_k$  represents the autocorrelation of lag1 (i.e. correlation of  $\epsilon_{t,k}$  with  $\epsilon_{t-1,k}$ ). This form is chosen both for its simplicity and the ability to account for the uncertain autocorrelation in the error terms. The bias term  $b_k$  represents time-independent biases. Note that for ocean heat content we use anomalies with respect to the entire observational period. As a result, the average modeled and observed  $OHC$  is 0 by definition and we set  $b_{OHC}$  to 0. Our statistical model is similar to that of *Urban and Keller* [2010], although they do not incorporate bias terms.

[28] For this statistical model, the likelihood of each observational time series  $\mathbf{y}_k$  given the UVic ESCM model output and the statistical parameters  $L(\mathbf{y}_k|\theta, \sigma_k, b_k, \rho_k)$  is given by *Bence* [1995] and is provided in Appendix A. We assume independence between the model-data residuals for different tracers. Under this assumption, the likelihood of both observations is equal to the product of the individual likelihoods:  $L(Y) = L(\mathbf{y}_1) \times L(\mathbf{y}_2)$ . Denote the set of all parameters by  $\Theta = (K_{bg}, CS, A_{sc}, \sigma_T, \rho_T, b_T, \sigma_{OHC}, \rho_{OHC})$ . Using Bayes Theorem, the posterior probability of the parameters can be calculated as:

$$p(\Theta|Y) \propto L(Y|\Theta) \times p(\Theta) \quad (8)$$

where  $p(\Theta)$  is the prior for the parameters (section 4).



**Figure 3.** Posterior (top) pdfs and (bottom) cdfs for model parameters obtained using both temperature and ocean heat content observations. Red: for the NON-UNIF experiment; blue: for the UNIF experiment. The dashed probability distribution lines represent the priors used in the NON-UNIF experiment. The dashed whiskers in the box-and-whisker plots extend to the most extreme data point which is no more than 1.5 interquartile ranges from the box.

[29] Two distinct approaches to estimate the properties of the error process  $\epsilon$  are (1) from the observations or models [Forest *et al.*, 2006; Tomassini *et al.*, 2007], or (2) directly from the model-data residuals together with the physical parameters [Urban and Keller, 2010; Goes *et al.*, 2010; Tonkonojenkov, 2010]. Here we use the second approach and estimate all parameters together in the MCMC step.

[30] We draw samples from the joint posterior  $p(\Theta|Y)$  using the MCMC algorithm [Metropolis *et al.*, 1953; Hastings, 1970] and generate the posterior probability distribution of  $\Theta$ . Our MCMC prechains are 50,000 members long, while the final chain has 300,000 members. We use information from previous chain covariance to construct the proposal distribution for each subsequent chain following Roberts and Rosenthal [2009]. We test the chains for convergence using the MCMC standard errors from the consistent batch means procedure [Flegal *et al.*, 2008; Jones *et al.*, 2006], and by repeating the assimilation with different starting values of the parameters for the final chain. Neither of these checks suggest any issues with convergence. Hence, we are satisfied that our MCMC-based inference provides reasonable estimates of the posterior pdfs.

#### 4. Priors

[31] We run two assimilation experiments. In the base case experiment we use non-uniform priors for climate sensitivity

and background vertical ocean diffusivity. We refer to this experiment as NON-UNIF. The priors for this experiment are listed in Table 1 and plotted in Figure 3. For  $K_{bg}$  the prior is Lognormal  $(-1.55, 0.59) \text{ cm}^2 \text{ s}^{-1}$  [Bhat, 2010]. This prior has a mode of  $0.15 \text{ cm}^2 \text{ s}^{-1}$  and a mean of  $0.24 \text{ cm}^2 \text{ s}^{-1}$ . The prior represents our prior belief that the values of  $0.1\text{--}0.2 \text{ cm}^2 \text{ s}^{-1}$  are more likely than  $0.4\text{--}0.5 \text{ cm}^2 \text{ s}^{-1}$  which is suggested by Goes *et al.* [2010] who use vertical oceanic tracer distributions to constrain  $K_{bg}$ . The climate sensitivity prior incorporates weak prior information derived from current mean climate and Last Glacial Maximum constraints. Specifically, we use a product of normal inverse Gaussian distributions (NIG) of  $NIG(\alpha = 1.8, \delta = 2.3, \beta = 1.2, \mu = 1.7)$  and  $NIG(\alpha = 1.9, \delta = 3.3, \beta = 1.0, \mu = 1.3)$ . We choose these distributions for their empirical ability to simultaneously fit the lower, upper, and best estimates from Knutti and Hegerl [2008], not because we have any theoretical motivation for the NIG distribution. While the central tendencies of the two NIG pdfs are generally compatible with past studies, the distributions are not based on any specific pdf from any of these studies. The combined prior distribution for CS is shown in Figure 3. It has a mean of  $3.25^\circ\text{C}$ , and the 90% interval from  $1.7$  to  $5.2^\circ\text{C}$ . We use uniform priors for  $A_{sc}$  and for all statistical parameters over the ranges specified in Table 1.

[32] To explore the sensitivity of the results to priors, we run a second assimilation experiment, where all priors are

**Table 2.** Properties of the Posterior pdfs of All Estimated Parameters

Parameter	Experiment	Mode	Mean	95% Credible Interval
$K_{bg}$	NON-UNIF	0.11	0.19	[0.10, 0.45]
	UNIF	0.11	0.30	[0.10, 0.50]
$CS$	NON-UNIF	2.8	3.1	[1.8, 4.9]
	UNIF	3.0	4.8	[1.6, 10.2]
$A_{sc}$	NON-UNIF	1.2	1.1	[0.35, 1.5]
	UNIF	1.6	1.2	[0.25, 1.8]
$\sigma_T$	NON-UNIF	0.10	0.10	[0.091, 0.11]
	UNIF	0.10	0.10	[0.091, 0.11]
$\sigma_{OHC}$	NON-UNIF	2.6	2.7	[2.2, 3.3]
	UNIF	2.6	2.7	[2.2, 3.3]
$\rho_T$	NON-UNIF	0.58	0.58	[0.44, 0.72]
	UNIF	0.58	0.58	[0.44, 0.72]
$\rho_{OHC}$	NON-UNIF	0.079	0.17	[0.018, 0.43]
	UNIF	0.091	0.17	[0.018, 0.42]
$b_T$	NON-UNIF	-0.031	-0.031	[-0.079, 0.021]
	UNIF	-0.034	-0.033	[-0.083, 0.022]

uniform over the ranges shown in Table 1. We refer to this experiment as UNIF.

## 5. Results

### 5.1. Probabilistic Hindcasts

[33] The probabilistic hindcasts capture the overall temporal structure of the observations (Figure 1). Specifically, the emulator is able to correctly represent the trend due to greenhouse warming (black line). We add an AR1 error process (representing model, observational, and emulator error, as well as the natural variability) to each emulator from the sub-sampled MCMC chain to produce the 95% credible intervals. In case of temperature, each emulator is corrected by adding a corresponding bias term from the chain. Overall, the method produces a reasonable surprise index (e.g., 1.9% of the ocean heat content and 5.1% of the temperature observations lie outside of the 95% hindcast range).

[34] The surface air temperature from the best fit emulator illustrates the effects of the stratospheric volcanic aerosols, with several prominent short-term coolings associated with the eruptions. For some of these eruptions, such as Agung (1963) and Mount Pinatubo (1991), the modeled response matches the observations relatively well, while for others, such as Krakatoa (1883), the model displays considerable cooling that is not present in the observations. Some of this discrepancy might be due to the unresolved climate variability, and due to the uncertainty in the past volcanic radiative effects [Ammann *et al.*, 2003] and temperature observations.

### 5.2. Parameter Estimates

[35] Under the baseline assumptions of non-uniform priors, posterior pdfs for climate sensitivity and vertical ocean diffusivity are broadly consistent with previous

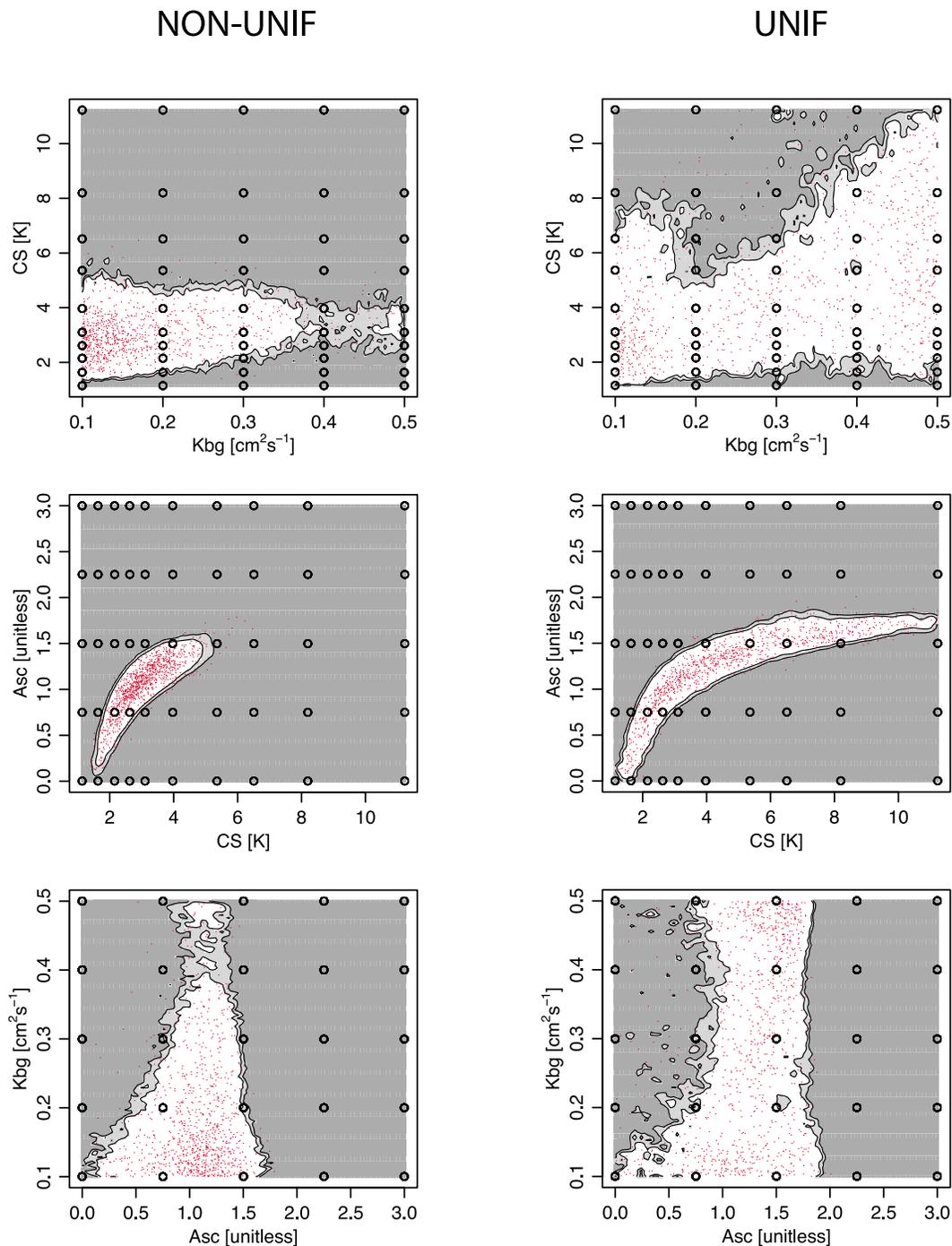
studies. The mode of the climate sensitivity pdf is 2.8°C, and the mean is 3.1°C. The 95% posterior credible interval ranges from 1.8°C to 4.9°C (Table 2). These values are broadly consistent with the likely range of 2 to 4.5°C, and the most likely value of 3°C given by the IPCC [Solomon *et al.*, 2007]. The mode is similar to results from Forest *et al.* [2006] and Knutti *et al.* [2003], and is slightly higher than those of Tomassini *et al.* [2007].

[36] For  $K_{bg}$ , we estimate a mode of 0.11 cm<sup>2</sup> s<sup>-1</sup>, and a mean of 0.19 cm<sup>2</sup> s<sup>-1</sup> (Table 2 and Figure 3). The pdf for  $K_{bg}$  was reported to depend on the tracers used to constrain this parameter [Schmittner *et al.*, 2009]. The mode of the  $K_{bg}$  matches results of Schmittner *et al.* [2009] based on global vertical ocean profiles of CFC11, and of  $\Delta^{14}C$ , and is slightly lower than 0.15 cm<sup>2</sup> s<sup>-1</sup> reported by Goes *et al.* [2010] based on profiles of three tracers. We stress that  $K_{bg}$  is not directly comparable with vertical diffusivities in other models [Tomassini *et al.*, 2007; Kriegler, 2005] because these parameters represent different processes. For example, our  $K_{bg}$  excludes tidally induced and Southern Ocean mixing, while the related  $K_v$  of Kriegler [2005] accounts for all vertical mixing processes. Therefore, our results should be interpreted as specific to our version of UVic ESCM.

[37] The estimated aerosol scaling factor has the most likely value of 1.2. This is broadly consistent with the default assumptions on the aerosol effects in the UVic ESCM (which imply the value of 1). Estimation of  $A_{sc}$  should be interpreted with caution because  $A_{sc}$  implicitly includes effects due to neglected forcings that might have emission or concentrations patterns similar to the anthropogenic sulfates. To better constrain  $A_{sc}$  it will be necessary to include these neglected forcings. Otherwise, one could interpret the value of  $A_{sc}$  as representing the combined effects of the aerosols as well as the neglected forcings. Similar to the case of  $K_{bg}$ ,  $A_{sc}$  is a model specific parameter and can not be readily compared to results from other models [e.g., Tanaka *et al.*, 2009].

[38] As in previous studies, the climate sensitivity pdf, and its upper tail in particular, are sensitive to the assumptions about the priors [e.g., Forest *et al.*, 2002, 2006; Sanso and Forest, 2009; Tomassini *et al.*, 2007; Annan and Hargreaves, 2011] (Figure 3). For example, replacing the expert prior with the uniform prior moves the upper bound of the 95% credible interval for  $CS$  to 10.2°C (Table 2). This is in agreement with the results from Forest *et al.* [2006], but considerably higher than those of Annan and Hargreaves [2011]. This discrepancy might be at least in part because Annan and Hargreaves [2011] consider a different type of constraint - Earth Radiation Budget Experiment (ERBE) data analyzed by Forster and Gregory [2006]. For the uniform prior, there is a considerable probability mass above the upper bound of the IPCC likely range of 4.5°C (Figure 3), similar to previous studies [e.g., Forest *et al.*, 2006; Knutti *et al.*, 2003].

[39] The use of uniform priors for climate sensitivity can be problematic as the posterior estimates are sensitive to the upper bound for the prior [Annan and Hargreaves, 2011]. In addition, such priors do not take independently collected evidence from other studies into account. High climate sensitivities become possible in this case because the flat prior assigns them high weight to begin with, while the



**Figure 4.** Bivariate joint pdfs for model parameters: (left) for the NON-UNIF experiment and (right) for the UNIF experiment. The contour lines delineate the 90% and 95% posterior credible intervals. A 1000-member thinned MCMC chain is plotted using red dots. Parameters used for the UVic ESCM ensemble are shown in thick black circles.

constraint provided by the observations can be relatively weak. This suggests that it is crucial to use independent prior information during  $CS$  estimation whenever possible.

[40] In addition, in the UNIF experiment the posterior pdf of  $K_{bg}$  is bimodal (Figure 3). Multimodal pdfs for  $K_{bg}$  have been previously reported by *Forest et al.* [2002] and *Tomassini et al.* [2007]. It is, thus far, unclear which physical mechanisms, if any, are driving this bimodality. Note

that here we withhold information on vertical tracer distributions that is needed to constrain  $K_{bg}$  and that the bimodality essentially disappears once that constraint is introduced as a prior in the NON-UNIF case.

[41] Joint bivariate pdfs for parameter pairs exhibit a complex structure (Figure 4), similar to the results from *Tomassini et al.* [2007]. Although this is not visibly evident, there is some correlation between  $K_{bg}$  and  $CS$ . Specifically,

the correlation is 0.24 in the NON-UNIF experiment, and 0.44 in the UNIF experiment. This is in agreement with 0.4 given by *Urban and Keller* [2010] even though the two studies differ in terms of climate models, observational constraints, and priors. It is difficult to compare these results with other studies [e.g., *Tomassini et al.*, 2007; *Forest et al.*, 2002, 2006] because they do not report the numerical value for the correlation coefficient while the pairs plots of the parameters can underestimate the correlation [*Urban and Keller*, 2010].

[42] Climate sensitivity is even more strongly correlated with  $A_{sc}$ , meaning that for higher climate sensitivity, higher aerosol effects are needed to explain historical climate change. This agrees with results from *Andreae et al.* [2005] and *Tanaka et al.* [2009] and implies that reducing uncertainty in  $A_{sc}$  will help reduce uncertainty in climate sensitivity. Ruling out high values of  $A_{sc}$  is especially important, because this is where climate sensitivity pdf appears to be most sensitive to  $A_{sc}$  (Figure 4).

[43] When the uniform priors on  $K_{bg}$  and  $CS$  are used, higher aerosol scaling values become possible, even though the prior on  $A_{sc}$  is the same in both cases. Because  $A_{sc}$  and  $CS$  are correlated, higher aerosol scalings are necessary to counteract higher warming due to larger climate sensitivities in the uniform prior case to match the observations.

[44] Climate parameter estimation using a model with a 3D ocean (GENIE-1) has been previously performed by *Holden et al.* [2010] so it might be interesting to compare our methodology and results with that study. *Holden et al.* [2010] vary a much larger set of parameters and derive a pdf for climate sensitivity using a Last Glacial Maximum (LGM) tropical Sea Surface Temperature (SST) anomaly as a main constraint. They also indirectly use information from several global climate metrics through a pre-calibration procedure. In our study we consider an orthogonal set of constraints that includes information about the time-resolved response of climate to modern forcings. We also provide a probabilistic estimate of vertical ocean diffusivity  $K_{bg}$ . In terms of the ocean models used, *Holden et al.* [2010] employ a coarse resolution frictional geostrophic model. On the other hand, the resolution of UVic ESCM is much higher and the dynamics is based on the Navier-Stokes equations, subject to the hydrostatic and Boussinesq approximations. The statistical methodologies are different as well. In particular, our approach is fully Bayesian and we use explicit priors for all model parameters. Also, the statistical properties of the error process are assumed by *Holden et al.* [2010], while here we estimate them together with the physical model parameters. The mode of climate sensitivity given by *Holden et al.* [2010] is 3.6°C under the favored set of assumptions, which is substantially higher than 2.8°C in our baseline case of non-uniform priors. We cannot attribute this gap with certainty to any specific factor due to the number of differences between the studies.

## 6. Caveats

[45] Our forthcoming conclusions are subject to several caveats. The first set of caveats deals with the Earth System model. Our model does not include all forcings (such as, sulfate effects on clouds or tropospheric ozone [*Forster*

*et al.*, 2007]). The patterns of some of excluded forcings might be similar to anthropogenic sulfates, thereby biasing the  $A_{sc}$  estimates. Including thus far neglected forcings is the subject of future research. Also, we only consider a subset of uncertain climate parameters. Our results would change if these additional uncertainties were considered. The model relies on a number of simplifications. The representation of open ocean mixing is highly parameterized and ignores, for example, effects of transient upper ocean mixing processes, such as tropical cyclones, that have been shown capable of influencing upper-ocean temperature patterns through mixing of heat [*Sriver et al.*, 2010]. We vary the longwave radiation feedbacks to change climate sensitivity. In reality, the uncertainty in shortwave radiative feedbacks also contributes to the  $CS$  uncertainty [*Bony et al.*, 2006]. Also, we only use a single model and neglect the uncertainty in model response to external forcings [*Stouffer et al.*, 2006]. Finally, we do not fully account for past climate forcings uncertainties.

[46] The second set of caveats is concerned with observations. When a short instrumental record is used, the results of our method can be influenced by natural climate variability and by observational errors comprising the residuals between the model and observations [*Tonkojenkov*, 2010]. Adding more observations can improve the parameter estimates, as could using spatially resolved information.

[47] Finally, limitations of the parameter estimation method deserve mentioning. We use a simplified likelihood function that does not account for the spectral complexity of the residuals, nor for the decrease of observational errors with time. Incorporating a more comprehensive likelihood function that captures a cross-correlation between the residuals for different tracers is the subject of future research.

## 7. Conclusions

[48] Using a Bayesian approach, we fuse the UVic ESCM model with global observations to estimate background vertical ocean diffusivity ( $K_{bg}$ ), climate sensitivity ( $CS$ ), and the scaling parameter for the effects of anthropogenic sulfate aerosols ( $A_{sc}$ ). Our methodology incorporates the effects of  $K_{bg}$  on 3D ocean dynamics. We use a Gaussian Process emulator to provide a fast surrogate for the climate model at arbitrary parameter combinations. The parameter estimates can be used to make climate projections using the UVic ESCM in future studies.

[49] The mode for  $K_{bg}$  is similar to previous results obtained using oceanic tracers such as CFC11, temperature, and  $\Delta^{14}C$  as constraints. The  $K_{bg}$  pdf is sensitive to the assumptions about the priors. If a uniform prior is used, then the results appear to show a bimodality, which is a potentially important result that might need further investigation.

[50] Under the default assumptions of informative priors, the mode of climate sensitivity is 2.8°C, with the 95% credible interval from 1.8°C to 4.9°C. This mode is consistent with many previous studies but lower than reported by *Holden et al.* [2010], who also use a 3D ocean model. As in previous studies, the upper tail of the  $CS$  pdf is sensitive to priors. The  $CS$  pdf depends critically on  $A_{sc}$ , with much higher climate sensitivities likely at high values of  $A_{sc}$ . The agreement with previous studies that use simpler climate

models gives more confidence to using these models to estimate climate sensitivity.

## Appendix A

[51] When the statistical model is defined as in section 3, the likelihood of observational time series  $\mathbf{y}_k$  coming from the model is given by [Bence, 1995]:

$$L(\mathbf{y}_k | \theta, \sigma_k, b_k, \rho_k) = \left(2\pi\sigma_{p,k}^2\right)^{-1/2} \exp\left(-\frac{1}{2} \frac{\epsilon_{1,k}^2}{\sigma_{p,k}^2}\right) \times \left(2\pi\sigma_k^2\right)^{-(N_k-1)/2} \times \exp\left(-\frac{1}{2\sigma_k^2} \sum_{j=2}^{N_k} w_{j,k}^2\right).$$

Here  $\sigma_{p,k}^2 = \sigma_k^2/(1 - \rho_k^2)$  is stationary process variance,  $N_k$  is the number of observational data points for tracer  $k$ , and  $w_{t,k} = \epsilon_{t,k} - \rho_k \epsilon_{t-1,k}$ ,  $t > 1$  are whitened errors.

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