

¹ **An optimal XBT-based monitoring system for the South Atlantic**
² **Meridional Overturning Circulation at 34°S**

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3 **Abstract.** The South Atlantic is an important pathway for the inter-basin
4 exchanges of heat and freshwater with strong influence on the global merid-
5 ional overturning stability and variability. Along the 34°S parallel, a quar-
6 terly, high resolution XBT transect (AX18) samples the temperature struc-
7 ture in the upper ocean. The AX18 transect has been shown to be a useful
8 component of a meridional overturning monitoring system of the region. How-
9 ever, a feasible, cost-effective design for an XBT-based system has not yet
10 been developed. Here we use a high-resolution ocean assimilation product
11 to simulate an XBT-based observational system across the South Atlantic.
12 The sensitivity of the meridional heat transport, meridional overturning cir-
13 culation, and geostrophic velocities to key observational and methodologi-
14 cal assumptions is studied. Key assumptions taken into account are horizon-
15 tal and temporal sampling of the transect, salinity and deep temperature in-
16 ference, as well as the level of reference for geostrophic velocities. With the
17 current sampling strategy, the largest errors in the meridional overturning
18 and heat transport estimations are the reference velocity for geostrophic cal-
19 culations and the western boundary resolution. We use the results obtained
20 by the state estimation under observational assumptions to make recommen-
21 dations for potential improvements in the AX18 transect implementation.

1. Introduction

22 The Atlantic Ocean circulation is well known for having a deep convection site at high
23 latitudes in the northern hemisphere, which drives to a large extent the Atlantic meridional
24 overturning circulation (AMOC) and, therefore, the northward heat transport to the
25 northern latitudes [*Marshall and Schott, 1999*]. The variability of the AMOC is partly
26 responsible for changes in the northern hemisphere climate, such as the North Atlantic
27 storm tracks [*Woollings et al., 2012*] and the North American and European precipitation
28 patterns [*Enfield et al., 2001; Sutton and Hodson, 2005*], sea level variability [*Levermann*
29 *et al., 2005; Hu et al., 2011*], uptake of ocean tracers such as CO₂ [*Sabine et al., 2004;*
30 *Goes et al., 2010*], tropical precipitation [*Zhang and Delworth, 2006*] and El Niño patterns
31 [*Dong and Sutton, 2007; Timmermann et al., 2007*].

32 Despite the fact that the AMOC strength and variability are highly determined by
33 changes within the North Atlantic Subpolar gyre [*Hatun et al., 2005; Lohmann et al.,*
34 *2009*], the deep convection regions between the Greenland-Iceland-Scotland seas are highly
35 sensitive to heat and freshwater transported from the South Atlantic [*Rahmstorf, 1996;*
36 *Donners and Drijfhout, 2004*], which is suggested to be one of the main drivers of two
37 stable states of the AMOC [*Weijer et al., 1999; Beal et al., 2011; Hawkings et al., 2011;*
38 *Garzoli et al., 2013*].

39 The South Atlantic is an important pathway for exchange of heat and water masses
40 from other basins through, for example, the Agulhas current region [*Goni et al., 1997*]
41 and the Brazil-Malvinas Confluence region [*Gordon, 1986; Wainer et al., 2000; Goni*
42 *and Wainer, 2001; Lentini et al., 2006; Goni et al., 2011*]. The South Atlantic Ocean

43 has been historically one of the least observed regions on the globe; however, several
44 efforts to measure long-term variability in the basin have been put forward in the last
45 decade. For instance, expendable bathythermograph (XBT) observations from the High-
46 Density XBT transect AX18 (Figure 1a) obtain temperature section in the upper 800
47 m of the ocean four times a year along 34°S. Studies based on the AX18 XBT data
48 have shown that the mean strength of AMOC and heat transport at 34°S are mostly
49 geostrophically driven, although the seasonal variability of the meridional transports are
50 equally determined by the geostrophic and the wind-driven Ekman components [*Dong*
51 *et al.*, 2009]. The compensation between the Ekman and geostrophic components may
52 translate into a small annual cycle of heat and volume transports [*Garzoli and Baringer*,
53 2007; *Dong et al.*, 2009], although models generally do not reproduce this characteristic
54 [*Dong et al.*, 2011a].

55 Currently, observational estimates rely on several assumptions to estimate the integral
56 flow in the South Atlantic. Thus far, only *Baringer and Garzoli* [2007] have estimated
57 some of the uncertainty resulting from the underlying XBT-based observational system
58 methodological assumptions to measure heat transport across 34°S. However, no sensi-
59 tivity tests have yet been performed to derive an optimal AX18 sampling strategy, i.e.,
60 a feasible strategy that maximizes the information content in a cost-effective manner,
61 and to assess the uncertainty in volume and heat transports associated with observational
62 and computational methodologies across 34°S. To accomplish this, current high resolution
63 ocean reanalyses can be useful to assess and investigate potential improvements in the
64 sampling strategy of the AX18 transect. Similar methodologies have been applied, for

65 example, in several studies in the North Atlantic [e.g. *Hirschi et al.*, 2003; *Baehr et al.*,
66 2004, 2008] to evaluate strategies for monitoring the MOC in the North Atlantic.

67 The goals of the present study is to assess how observational and computational method-
68 ologies affect the estimates of volume and heat transports across 34°S in Atlantic Ocean,
69 and to help improve the design of the AX18 XBT transect in order to reduce uncertainty
70 in its estimates. Therefore, this study will address four main objectives to reach these
71 goals:

- 72 i) The optimal spatial (longitudinal) resolution along the AX18;
- 73 ii) The optimal temporal sampling to capture the seasonal variability of the AMOC in
74 the region;
- 75 iii) The uncertainties derived from the salinity and deep temperature estimation;
- 76 iv) Potential improvements to the assumptions made regarding the level of reference to
77 resolve the barotropic mode.

78 To address these objectives, we will first describe the characteristics of the region of
79 study (Section 2). We will describe the high-resolution global assimilation model (Section
80 3) used in this study. We will define the methodology (Section 4) to calculate volume
81 and meridional heat transport (MHT) across 34°S, and perform controlled experiments in
82 the model framework to answer point-by-point the above questions (Section 5). Finally,
83 we will discuss the results and make recommendations for the improvement of the AX18
84 XBT transect measurements (Section 6).

2. Regional characteristics

85 The subtropical South Atlantic is characterized by a large scale anticyclonic feature,
86 the South Atlantic subtropical gyre [*Stramma and England*, 1999; *Garzoli and Matano*,

2011]. In the southwestern Atlantic, the surface dynamics are dominated by the Brazil-
Malvinas Confluence, which is characterized by the cold northward flow of the Malvinas
Current, and a southward flowing warm weak western boundary current, the Brazil Cur-
rent [Garzoli, 1993]. This region exhibits complex frontal motions [Goni *et al.*, 2011;
Goni and Wainer, 2001] and patterns with the simultaneous presence of warm and cold
rings and eddies [Lentini *et al.*, 2006] and, therefore, it is characterized by large values
of eddy kinetic energy (Figure 1a). In the southeastern Atlantic, the transfer of warm
waters from the Indian Ocean into the South Atlantic subtropical gyre largely takes place
in the form of rings and filaments formed when the Agulhas Current retroflects south of
Africa between 1°W and 25°E [Richardson and Garzoli, 2003; Goni *et al.*, 1997]. The
eastward flowing South Atlantic Current and the northward flowing Benguela Current
delimit the southern and eastern boundaries of the subtropical gyre, respectively. The
Brazil-Malvinas Confluence region and the Agulhas retroflection region represent the most
energetic areas contained in the South Atlantic. These two regions present similar values
of mean eddy kinetic energy, above $1000 \text{ cm}^2 \text{ s}^{-2}$ (Figure 1a), as revealed by altimetric sea
level anomalies [Ducet *et al.*, 2000] for the 2007-2012 time period. The Brazil-Malvinas
Confluence and Agulhas retroflection regions are both crossed by the XBT transect AX18
(Figure 1a).

3. The HYCOM-NCODA reanalysis

As suggested in previous studies, the strong mesoscale energy in the South Atlantic
region requires a minimum of eddy-permitting models to resolve its main features [Treguier
et al., 2007; Biastoch *et al.*, 2009]. In the present study we use data from the Hybrid
Coordinate Ocean Model (HYCOM)-Navy Coupled Ocean Data Assimilation (NCODA)

109 assimilative product [*Chassignet et al.*, 2009], which has been previously applied in several
110 studies in the South Atlantic [*Mello et al.*, 2013]. We use a total of nearly 6 years of model
111 simulation, from June 2007 to May 2013, sampled in a 7-day timestep using 7-day averages.

112 The HYCOM-NCODA is configured for the global ocean with HYCOM 2.2 as the dy-
113 namical model. Computations are carried out on a Mercator grid between 78°S and 47°N,
114 with an average of 1/12° (~ 7 km) horizontal spacing and 32 vertical layers. A bipolar
115 patch is used for regions north of 47°N. Bathymetry is derived from the U. S. Naval Re-
116 search Laboratory 2-minute DBDB2 (Digital Bathymetric Data Base) dataset. Surface
117 forcing is from the Navy Operational Global Atmospheric Prediction System (NOGAPS)
118 and includes 3-hourly and 0.5° wind stress, wind speed, heat flux (using bulk formula),
119 and precipitation. The NCODA methodology [*Cummings*, 2005] uses the model forecast
120 as a first guess in a multi-variate Optimal Interpolation (MVOI) scheme and assimi-
121 lates available along-track satellite sea height anomaly observations (obtained via the
122 Naval Oceanographic Office’s Altimeter Data Fusion Center), in-situ sea surface temper-
123 ature (SST), as well as available in-situ vertical temperature and salinity profiles from
124 XBTs, ARGO floats, and moored buoys. The Modular Ocean Data Assimilation Sys-
125 tem (MODAS) synthetic profiles are used by NCODA for downward projection of surface
126 information [*Fox et al.*, 2002].

127 Compared to altimetric observations, the eddy-resolving HYCOM-NCODA reanalysis
128 reproduces reasonably the main circulation features of the region (Figure 1b). The output
129 of this model, however, shows lower energy in the high EKE regions, such as the Brazil-
130 Malvinas Confluence and Agulhas retroflection regions, and higher energy in the low EKE
131 regions (Figure 1c). The negative energy biases are also observed in the comparison of the

132 sea level root-mean square variability of the AX18 transect boundaries (Figure 2a, b, c).
133 We select 18 realizations (Figure 2a) of the AX18 transect based on the criteria of being
134 zonally directed (median angle $< 10^\circ$, and with the mean section between 30° and 36° of
135 latitude) to compare the model thermohaline behavior with the actual XBT observations
136 along the nominal 34°S . Below 850 m, the maximum depth sampled by the XBTs, the
137 WOA05 annual climatology [*Locarnini et al.*, 2006] is used. The mean temperature section
138 retrieved by the AX18 along the nominal of 34°S shows an east-west gradient, with higher
139 upper ocean temperatures in the west (Figure 2d). The associated zonal density gradients
140 allow average geostrophic volume and heat transports to the north, as shown in previous
141 studies [e.g., *Ganachaud and Wunsch*, 2003; *Garzoli and Baringer*, 2007]. The model
142 shows generally negative temperature biases in the interior (1 to 2°C on average), which
143 indicates stronger stratification and shoaling of isothermal layers, and positive biases
144 on the boundaries (1 to 1.5°C on average) relative to the mean AX18 section above 850
145 m, and stronger ocean bottom stratification in comparison to the WOA05 climatology
146 (Figure 2g–i).

4. Methodology

147 This study focuses on the reconstruction of the AMOC streamfunction (Ψ_y) and the heat
148 transport (MHT) along 34°S by simulating XBT observations in the model framework.
149 For this, we use the temperature, salinity and velocity outputs of the model, distributed
150 over depth and longitude along the 34°S . This section describes how the AMOC and MHT
151 are defined through the paper.

4.1. AMOC

The AMOC streamfunction is defined as:

$$\Psi_y(z) = \int_{x_E}^{x_W} \int_z^{-H} v(x, z) dx dz, \quad (1)$$

i.e., the integral of the meridional velocity $v(x, z)$ from the bottom (H) to the depth (z) of the ocean and between the western (x_W) and the eastern (x_E) boundaries of the basin. The meridional velocity $v(x, z)$, and therefore its derived meridional streamfunction, can be decomposed into three dynamical components [Lee and Marotzke, 1998]:

$$v(x, z) = v_{sh}(x, z) + v_{bar}(x) + v_E(x, z), \quad (2)$$

where v_{sh} is the vertical shear component, which consists of the velocities calculated using the thermal wind relationship, minus a depth independent velocity:

$$v_{sh}(x, z) = \frac{g}{\rho_0 f} \frac{\partial \rho}{\partial x} - \frac{1}{H} \int_{-H}^0 v_{sh}(x, z) dz, \quad (3)$$

where $\rho_0 = 1025 \text{ kg m}^{-3}$ is the mean water density, f is the Coriolis parameter, and g is the local gravity. The depth independent velocity is known as the barotropic or gyre component v_{bar} , and is here defined as the local average of $v(x, z)$ over the depth H of the ocean:

$$v_{bar}(x) = \frac{1}{H} \int_{-H}^0 v(x, z) dz, \quad (4)$$

and the last term $v_E(x, z)$ is the Ekman component, derived from the local zonal wind stress (τ_x), compensated by a depth-independent flow underneath the Ekman layer:

$$v_E = -\frac{\tau_x}{\rho_0 f D_E} - \frac{1}{H} \int_{-H}^0 v_E(x, z) dz, \quad (5)$$

where D_E is the depth of the Ekman layer, which is arbitrarily assumed here to be $D_E = 50 \text{ m}$ [e.g., Pond and Pickard, 1983]. Therefore the Ekman velocity assumes only two different values in the water column, one in the Ekman layer, and another below the

Ekman layer [Baehr et al., 2004]. Other ageostrophic contributions rather than Ekman (frictional and non-linear) are not defined. The barotropic and vertical shear velocities combined constitute the absolute geostrophic velocity, which is estimated using the dynamic method assuming a reference level [Pond and Pickard, 1983]. Barotropic velocities have a strong contribution to the geostrophic flow at locations of sloping topography, and their projection on the AMOC can therefore be an important term in the AMOC reconstruction [Baehr et al., 2004]. To ensure zero mass transport, a correction is applied to the three components of the meridional velocity by subtracting a spatially constant term proportional to the weighted mean velocity across the section:

$$v(x, z) = v(x, z) - \frac{M_y}{\int_{-H}^0 \int_{x_E}^{x_W} dx dz}, \quad \text{for } M_y = \int_{-H}^0 \int_{x_E}^{x_W} v(x, z) dx dz \quad (6)$$

152 The AMOC strength (in Sv) is further defined as the value of the maximum amplitude
 153 of the AMOC streamfunction (Equation 1). Since the total velocity is decomposed into
 154 its physical components in Equation 2, an AMOC strength can also be defined for the
 155 individual components of the AMOC.

4.2. Meridional Heat Transport

The meridional heat transport is calculated as follows:

$$MHT = \rho_0 c_p \int_{-H}^0 \int_{x_E}^{x_W} v(x, z) \theta(x, z) dx dz - \rho_0 c_p M_y \langle \theta \rangle, \quad (7)$$

156 where $c_p = 4187 \text{ J kg}^{-1} \text{ K}^{-1}$ is the specific heat of sea water, and $\langle \theta \rangle$ is the averaged
 157 potential temperature θ along the section. The last term in Equation 7 is a constraint
 158 to allow zero mass transport across the section, which is necessary for heat transport
 159 calculations in free surface models, since they do not necessarily have zero mass transport
 160 at any given time period [Jayne and Marotzke, 2001; Griffies et al., 2004].

To reconstruct the MHT, Equation 7 is further decomposed into the same components as the meridional overturning, i.e., vertical shear, barotropic and Ekman, respectively, using the corresponding decomposition of the velocity (Equation 2). Following *Hall and Bryden* [1982]:

$$MHT = \rho_0 c_p \int_{-H}^0 \int_{x_E}^{x_W} \{v_{vs}[\theta - \theta_{bar}] + v_{bar}\theta_{bar} + v_{Ek}\theta_{Ek}\} dx dz \quad (8)$$

161 where θ_{bar} is the depth-averaged potential temperature, and θ_{ek} follows the Ekman velocity
 162 definition, i.e., θ_{ek} assumes only two values over depth, one as the average in the Ekman
 163 layer, and another in the layer below the Ekman layer. Each of the terms in Equation
 164 8 is meaningful as a heat transport, because the velocity components are designed to be
 165 compensated and allow zero net volume transport across the section [*Hirschi et al.*, 2003].
 166 Therefore, in the reconstruction, the last term in Equation 7 is not necessary. Otherwise,
 167 the calculated heat transport would be dependent on an arbitrary temperature reference
 168 [*Montgomery*, 1974].

5. Results

5.1. AMOC streamfunction reconstruction

169 The AMOC strength calculated from the model output velocities in a 7-day average is
 170 highly variable in time (Figure 3a; black line), with amplitude ranging from -5 to 35 Sv (1
 171 Sv = $10^6 \text{ m}^3\text{s}^{-1}$), and with strong high frequency variability as well as a defined annual
 172 cycle. The time-averaged AMOC streamfunction (Figure 3c) shows positive (northward)
 173 values in the upper 3500 m, negative (southward) values underneath, and a pronounced
 174 maximum at the depth of ~ 1500 m, which characterizes the AMOC strength. The time-
 175 mean AMOC strength in the model is 15.1 ± 6.8 Sv, lower than observational estimates

176 of 17.9 ± 2.2 Sv [*Dong et al.*, 2009], but within the uncertainty estimates. Results from
177 other high resolution models, e.g. [*Dong et al.*, 2011a] using the OFES model, show a
178 strong agreement with the AMOC strength value (15.0 ± 3.7 Sv) presented here.

179 We decompose the AMOC streamfunction into its vertical shear, Ekman, and barotropic
180 components using the methodology described in Section 4.1. Therefore, each component is
181 independently estimated, accordingly to *Lee and Marotzke* [1998] and *Baehr et al.* [2004],
182 but differently from the methodologies of *Perez et al.* [2011] and *Dong et al.* [2011a],
183 which estimate the geostrophic transport either unbalanced for mass transport or as the
184 residual between the total and Ekman transports. The absolute geostrophic component
185 (barotropic plus vertical shear) is calculated using a level of known motion at the bottom
186 of the ocean, assuming that velocities are perfectly known there. Individually, the vertical
187 shear component has the strongest contribution to the mean AMOC strength (Figure 3b),
188 with an average of 26.9 ± 3.6 Sv, and it is in great part compensated by the barotropic
189 contribution of the transport, which is negative (southward) with an average of $-16.3 \pm$
190 6.3 Sv. The resulting absolute geostrophic transport is 12.6 ± 3.2 Sv, smaller than the
191 observational value of 15.7 ± 2.6 Sv [*Dong et al.*, 2009], but similar to that obtained from
192 the OFES model (12.9 ± 2.1 Sv; *Dong et al.* [2011a]). It is worth mentioning that neither
193 the barotropic nor the vertical shear streamfunctions show a reversal in depth, as observed
194 on the total mean streamfunction, but that the addition of these two streamfunctions
195 produces the same reversal pattern at approximately 3500 m (magenta line in Figure
196 3c) as observed in the original model streamfunction. Strong interannual variability is
197 observed in the barotropic component, with positive anomalies in the austral summer of
198 2007 and 2008 and negative anomalies in the austral spring of 2009 and 2010. The Ekman

199 component has the lowest contribution to the mean AMOC strength, only 2.0 ± 4.0 Sv,
200 but its maximum amplitude (variability) can reach over 10 Sv, which is stronger than the
201 other components.

202 The MHT follows the same pattern as the AMOC (Figure 4). The mean MHT calculated
203 directly from the model fields is 0.33 ± 0.5 PW (1 PetaWatt = 10^{15} W), which is also
204 lower than the values calculated from observational studies (0.54 ± 0.14 PW; *Garzoli*
205 *et al.* [2013]). The barotropic MHT component (-0.60 ± 0.23 PW) compensates to a
206 large extent the vertical shear component (0.81 ± 0.35 PW), and the Ekman component
207 contributes about one third of the total MHT (0.12 ± 0.24 PW).

208 The annual variability of the AMOC and MHT components (Figure 5) shows that
209 the vertical shear component does not have a noticeable annual cycle. The Ekman and
210 barotropic components have stronger annual cycles, and are approximately in phase with
211 each other, with more positive/less negative values from March to August. Therefore, the
212 total geostrophic transport (vertical shear plus barotropic) and the Ekman components
213 have similar phases, a result that differs from previous observational studies [e.g., *Dong*
214 *et al.*, 2009] that show an out-of-phase relationship between the Ekman and geostrophic
215 AMOC annual cycle, which produces a much reduced annual cycle of the AMOC vari-
216 ability. However, other high-resolution models also show a similar annual cycle for the
217 total AMOC [e.g., *Dong et al.*, 2011a; *Perez et al.*, 2011] as observed here. The residual
218 contribution, which is the part of the annual variance that is not explained by the recon-
219 struction (cyan line, Figure 5), is negligible for the AMOC but can reach up to -0.2 PW
220 for the MHT, especially during the austral summer. As observed in Figure 4a, the MHT
221 calculated directly from the model velocities is weak or sometimes negative during austral

222 summer, but these reversals of MHT are hardly featured in the reconstruction (Figure 4a,
223 magenta line). Consequently, the reconstruction produces a higher mean MHT of $0.39 \pm$
224 0.36 PW. These differences may arise because the model velocities contain ageostrophic
225 terms other than Ekman [*Sime et al.*, 2006], non-linearities in the MHT calculation, and
226 unbalanced flow of volume (0.94 ± 3.8 Sv), whose MHT contribution is here estimated
227 at -0.02 ± 0.06 PW (Equation 8), the same mean magnitude of 0.02 PW estimated in
228 *Baringer and Garzoli* [2007].

5.2. XBT observational strategy

229 The AX18 XBT transect, which was designed with the main purpose of monitoring the
230 variability of the upper limb of the AMOC transport, measures temperature sections in
231 the upper ocean between Cape Town and South America quarterly, with a high-density
232 (between 25-50 km) zonal spacing.

233 Observational studies that used AX18 data to estimate meridional volume and heat
234 transports involved several methodological assumptions. The XBTs measure tempera-
235 ture profiles in the upper 800 m depth (e.g. Deep Blue probe type). Because XBTs do
236 not measure salinity, a common method to infer salinity profiles at an XBT deployment
237 location uses a lookup table derived from historical temperature-salinity (T-S) relation-
238 ships [*Thacker*, 2008]. Below 800 m, the temperature and salinity profiles are extended
239 down to the bottom of the ocean with their climatological values [*Baringer and Garzoli*,
240 2007; *Dong et al.*, 2009]. The barotropic or external mode is generally estimated by adopt-
241 ing a level of no motion at the depth where the potential density anomaly referenced to
242 2000 dbar assumes the value of 37.09 Kg m^{-3} ($\sigma_2 = 37.09$) [*Ganachaud and Wunsch*,
243 2003; *Baringer and Garzoli*, 2007]. The $\sigma_2 = 37.09$ depth is approximately located at

244 3700 m depth and between two water masses, the North Atlantic Deep Water (NADW)
245 flowing southward between 1500 and 3700 m, and the underlying Antarctic Bottom Water
246 (AABW) flowing northward [*Ganachaud and Wunsch, 2003*]. The Ekman component of
247 the flow is calculated from available zonal wind stress products at the XBT deployment
248 locations.

249 In order to simulate the XBT observations in the model, we make the same assumptions
250 as used in the observational studies: i) the model temperature data are used above 800 m,
251 ii) a quadratic least squares fit between the annual mean temperature and salinity obtained
252 from the model is specified for each depth, calculated using 1 degree boxes along 34°S, iii)
253 the monthly climatology of temperature and salinity at a 1 degree longitudinal resolution
254 is padded below 800 m to extend the pseudo-observations to the bottom of the ocean, and
255 iv) a reference level for the geostrophic velocity calculation is chosen. Constructing the
256 T-S relationships from the model instead of using, for example, the World Ocean Atlas
257 (WOA) climatology is necessary, since the model's own internal biases relative to the
258 observations could potentially bring spurious T-S discontinuities. The WOA climatology
259 is subject to biases in regional coverage, such as below 2000 m (the parking depth of
260 Argo floats), along coastal areas, and historically in the South Atlantic. Here, we do not
261 account for imperfect sampling although its effects can be sizeable in producing additional
262 seasonal biases.

263 The RMS error between the model salinity and the salinity estimated from the lookup
264 table is shown in Figure 6. In the top 200 m, salinity errors are on the order of 0.1 psu.
265 Higher differences (~ 0.4 psu) are found in the western side of the basin in the upper 100
266 m, where there is a fresh water inflow from river runoff. Below 200 m the RMS difference

267 is generally lower than 0.1 psu, with higher values located around 500 m and decreasing
268 to near zero below 1000 m. These error values are on the same order of magnitude of the
269 RMS of the salinity annual cycle and, therefore, are highly driven by the seasonal variation
270 of T-S relationships, which is not captured by the annual mean T-S relationships.

5.3. AMOC and MHT uncertainties due to the XBT transect observational sampling

271 In this section we investigate the meridional transport uncertainties associated with
272 the observational sampling. We will explore two main sources of uncertainty, that relate
273 to: i) the temporal resolution and ii) the horizontal resolution. We apply each of the
274 two assumptions individually in order to quantify their uncertainties, which will allow
275 recommending improvements in the AX18 transect design and implementation.

276 5.3.1. Temporal resolution

277 The AX18 transect was originally implemented to be carried out four times a year,
278 and estimates of the geostrophic AMOC transport can only be performed at the time
279 of each AX18 transect realization. The rate of time sampling as well as the year-to-
280 year variability of number of transects may alias the estimates of the annual cycle of the
281 AMOC and meridional heat transport [*Bryden et al.*, 2005]. We simulate in the model
282 uncertainties associated with the transect temporal sampling by randomly selecting points
283 in the timeseries of the geostrophic AMOC and MHT, and use the RMS difference of
284 monthly means of these two quantities as a measure of the uncertainty associated with the
285 temporal sampling. We vary two parameters associated with the temporal sampling of the
286 AX18 transect: The number of realizations per year, from 1 to 20 times per year, and the
287 number of years of data collection, from 1 to 15 years. The random sampling is calculated

288 in three steps. First the original timeseries of the AMOC and MHT are extended by
289 padding up to 100 years. Some small stochastic noise is added to the extended timeseries.
290 Seasonality is maintained in this timeseries by choosing accordingly the beginning of
291 each padded timeseries. Second, a stretch of the 100-year timeseries is chosen with its
292 length defined by the uncertain parameter number of years sampled. Third, according
293 the number of samples per year, random samples are taken from the stretch of the time
294 series. In this step the samples are evenly distributed around the year, for example, with
295 a two sample per year parameter setting, one sample is taken every semester. These
296 steps are reproduced 400 times, which is a number sufficiently high to allow all months
297 to be sampled and the average of all realizations to have the same monthly means as
298 the original model geostrophic AMOC and MHT. Furthermore, the mean monthly RMS
299 difference of the 400 realizations will define a measure of the uncertainty associated with
300 the time sampling. Contour plots showing the sampling error variability of the AMOC
301 and MHT with respect to the number of years measured and the number of samples per
302 year is shown in Figure 7. The time sampling error of the AMOC and MHT show similar
303 behavior, i.e., errors decrease exponentially as more samples are collected during the year
304 or when a higher number of years is sampled. The RMS errors are as low as 0.5 Sv
305 and 0.05 PW when carrying out up to 12 transect realizations per year for 15 years. On
306 the other hand, when transects are carried out twice a year for two years, the errors are
307 above 2.5 Sv and 0.25 PW, respectively. The current number of realizations of the AX18
308 transect along the nominal of 34°S is 18 (Figure 2), which are done approximately on a
309 quarterly basis. This is equivalent to a total sampling period of five years in our considered
310 parameter space. Therefore, according to our model estimates, the associated RMS errors

311 of the AMOC and MHT are 2.3 Sv and 0.23 PW, respectively (stars in Figure 7), close
312 to the most uncertain values in the studies parameter space. Although 12 realizations
313 per year is difficult to achieve operationally, current discussions for increasing the number
314 of transect realizations to five or six per year are underway. This would lower the RMS
315 errors to < 2.0 Sv for the AMOC and < 0.20 PW for the MHT, which may allow a greater
316 improvement over the years.

317 One additional temporal sampling error arises from the non-synopticity of the XBT
318 transect measurements. An AX18 realization takes approximately 10 days to complete
319 the trajectory from South America to Cape Town, which may alias the transport estimates
320 across this transect. We quantify here the errors due to non-synopticity by simulating the
321 same observational assumptions within the model environment. In this experiment, we
322 simulate one AX18 XBT realization for each model day by using 10 bins of meridional
323 velocity values from east to west that correspond to 10 consecutive days of model velocity.
324 The AMOC and MHT are estimated every 7 days from these simulations, using as the
325 time tag the first day of each non-synoptic field. These estimates are compared against
326 the ones from the synoptic model outputs. The errors associated with the non-synopticity
327 of the data for the whole period of the simulation are 0.21 ± 4.1 Sv for the AMOC and
328 0.01 ± 0.25 PW for MHT. The RMS values due to non-synopticity are on the same order
329 as the RMS errors produced by the quarterly sampling. However, since this calculation
330 is performed over model daily values instead of 7-day averages, these RMS values are
331 actually an overestimation in comparison to the other experiments.

332 **5.3.2. Horizontal sampling**

333 The AX18 XBT transect crosses three regions of different dynamic regimes (Figure 1):
334 i) the western (Confluence region), interior (gyre), and eastern (Agulhas leakage) regions.
335 Previous studies suggest that it is critical to account for the variability in all three regions
336 in order to monitor and quantify changes in the AMOC and MHT [Dong *et al.*, 2009]. The
337 current XBT spatial sampling strategy accounts for the different regional characteristics:
338 at a lower density (~ 50 km) in the interior region, and at higher density (~ 25 km) closer
339 to the boundaries, i.e., east of the Walvis Ridge ($\sim 1^\circ\text{W}$) and west of 40°W , outside the
340 continental slope region in South America. This sampling strategy is a heuristic approach
341 to add more spatial resolution to the high energy boundary regions (Figure 1). Here we
342 quantify the sensitivity of the meridional transport changes to the horizontal sampling
343 in these three regions. To accomplish this, we generate an ensemble with 30 members
344 by degrading the longitudinal resolution in each of the three regions at a time, from the
345 original 0.08 degree (~ 7.3 km) model grid up to 5 degrees (~ 460 km) at variable steps,
346 giving more emphasis to the high resolution sampling. We use the RMS error, bias, and
347 correlation as metrics to compare the reconstructions to the original AMOC and MHT
348 strength.

349 Our results show that the AMOC strength and MHT are less sensitive to changes in the
350 spatial resolution in the interior than at the boundary regions (Figure 8). For the AMOC,
351 degrading the resolution in the interior to a 3° degree longitude sampling produces a small
352 negative bias and RMS error of -0.45 ± 1.3 Sv, and a minimum correlation of ~ 0.9 . For a
353 50 km resolution ($\sim 0.6^\circ$), the error is -0.1 ± 1.1 Sv and 0.01 ± 0.06 PW. In the boundary
354 regions, the AMOC and MHT are more sensitive to changes in spatial sampling. The bias
355 and RMS error for a 25 km ($\sim 0.3^\circ$) spacing is of 1.7 ± 2.4 Sv/ 0.03 ± 0.06 PW in the

356 western and 1.0 ± 1.4 Sv/ -0.03 ± 0.04 PW in the eastern boundary. The correlation is
357 about 0.9 at 25 km spacing in the boundaries, and decreases to 0.6 when longitudinal
358 sampling is larger than ~ 90 km (1°). The larger decrease of correlation in the boundaries
359 is partly due to subsampling of strong currents and high mesoscale activity, and also
360 because the shelf transport may not be observed at lower sampling rates. The potentially
361 unresolved volume transports in the continental shelves (above 200 m deep) are $-0.61 \pm$
362 0.77 Sv in the west and 0.15 ± 0.44 Sv in the east of the basin. Both transports on
363 the shelf contribute only a negligible temperature transport ($\sim 10^{-8}$ PW), which agrees
364 with the estimates of *Baringer and Garzoli* [2007]. Therefore, a higher AX18 horizontal
365 sampling is indeed needed in the eastern and western boundaries, especially in the western
366 side of the basin, where the current sampling biases are larger in comparison to the other
367 regions.

368 Interestingly, biases in the MHT have opposite signs and similar magnitudes when
369 comparing the western and eastern boundaries for any given zonal sampling resolution
370 (Figure 8c, f). Therefore, biases in the eastern and western regions may cancel each other
371 to some extent.

5.4. AMOC and MHT uncertainties due to computational methodology

372 In the previous section we analyzed the sensitivity of the AMOC and MHT to strategies
373 for different temporal and spatial sampling of the AX18 XBT transect. In this section,
374 we investigate how methodological assumptions affect the AMOC and MHT estimated
375 at 34° S. First, we will explore the impact of salinity and deep temperature inferences.
376 Additionally, we optimize the choice of the reference level, and propose a method to
377 estimate the barotropic velocities across the transect.

379 To study the impact of salinity and deep temperature inferences on the AMOC and
380 MHT, we perform step changes in the model observational strategy. We compute Ψ_y
381 and MHT using: i) the constructed annual T-S lookup table (Section 5.1) to estimate
382 salinity profiles in the upper 800 m, ii) padding the model T-S monthly climatology in
383 the deep ocean (> 800 m deep), and iii) using both the lookup table in the upper ocean
384 and padding in the deeper ocean.

385 We compare the changes in the geostrophic components of AMOC strength and MHT
386 using these approximations against those calculated using the full model output. The
387 main variability of the AMOC and MHT follow closely the ones from the approximated
388 fields (not shown). The analysis of the residuals relative to the estimates from the full
389 model outputs (Figure 9) show that the T-S lookup approximation drives most of the
390 residual AMOC changes (0.35 ± 2.8 Sv). In addition, the residuals from the T-S lookup
391 approximation are subject to strong seasonality. Biases in AMOC strength can reach -1
392 Sv during austral winter and 1 Sv during summer. This seasonal bias is due to the fact
393 that the T-S relationships are taken from an annual mean.

394 Deep ocean padding biases show only a small seasonality, and AMOC mean biases are
395 small, with magnitude of -0.03 ± 2.4 Sv. For the MHT, performing either padding or
396 TS lookup approximations produce residual changes of -0.02 ± 0.13 PW and 0.04 ± 0.17
397 PW, respectively. These RMS errors calculated here are close to the value of ± 0.15 PW
398 estimated for these approximations using the cumulative transport of the WOCE A10
399 section considered in *Baringer and Garzoli* [2007]. The results of our analysis using a six-
400 year timeseries show that although the errors produced by salinity and deep temperature

401 approximations are similar in value, the seasonal amplitude of the MHT and AMOC
402 residuals using the TS lookup table is the largest (right panels in Figures 9a and 9b).
403 Although these are conservative estimates, given that the model climatology represents
404 well the variability below the surface, the errors caused by deep T-S padding are small in
405 comparison to the other sources. Thus deployment of a whole water column CTD is not
406 essential for a strong reduction of errors in the AX18 XBT transect.

407 **5.4.2. Reference level for absolute geostrophic velocities**

408 The barotropic mode accounts for most of the bias of the overturning circulation con-
409 tribution [Baehr *et al.*, 2004]. As indicated from the model output (Figure 10), variations
410 in bottom topography are the main driver of strong bottom velocities, which increases the
411 barotropic contribution and its potential biases as well. Zonal sections, where boundaries
412 are steeper and more similar to a vertical wall, can reduce the effect of the barotropic
413 contribution [Rayner *et al.*, 2011]. At 34°S, where there are strong bottom velocities,
414 large biases in the barotropic component could be introduced by assuming an inaccurate
415 reference velocity. Here we perform four experiments to estimate the sensitivity of the
416 barotropic AMOC (Ψ_{bar}) to the velocity of the reference level. Similar to observational
417 studies, we use in all experiments the reference depth at the $\sigma_2 = 37.09$. Since the velocity
418 at the depth of $\sigma_2 = 37.09$ is below 3000 m, it is not well constrained by observations.
419 Therefore we perform the following experiments: a) with zero reference velocity, b) with
420 climatological reference velocity at the western boundary, c) with climatological reference
421 velocity at the eastern boundary, and d) with climatological velocity at both western
422 and eastern boundaries. Figure 11 shows the evolution and the time mean barotropic
423 streamfunction (left and right panels, respectively), for the experiments (a–d).

424 The minimum of barotropic streamfunction, which characterizes its strength, is located
425 between 2 and 3 km deep. Using model velocities, the mean Ψ_{bar} strength is estimated
426 as -16.3 Sv. When zero reference velocity is assumed, a much weaker Ψ_{bar} strength value
427 is estimated ($\Psi_{bar} = -10.5$ Sv; Figure 11a), or a mean bias of 5.7 ± 4.4 Sv. Because the
428 barotropic streamfunction is the main balance of the vertical shear component in the model
429 (Figure 3), a weaker Ψ_{bar} acts to increase the MHT by 0.17 ± 0.16 . Adding a climatological
430 reference velocity in the boundaries reduces the uncertainties in the barotropic mode. The
431 derived Ψ_{bar} strength estimates using climatological reference velocities in the boundaries
432 produce positive biases of 4.0 ± 4.5 Sv (0.06 ± 0.16 PW) in the western boundary and
433 2.0 ± 4.3 Sv (0.10 ± 0.14 PW) in the eastern side of the basin (Figures 11b and 11c,
434 respectively). Therefore, the eastern boundary velocity information reduces uncertainties
435 more than in the western boundary. When both eastern and western reference velocities
436 are added (Figure 11d), the mean $\Psi_{bar} = -16.0$ Sv, and the Ψ_{bar} strength is correctly
437 measured at value of 0.3 ± 4.4 Sv (-0.02 ± 0.14 PW). Further adding reference velocity
438 information in the interior does not improve these uncertainty values.

439 Therefore, we show here that the misrepresentation of the reference velocities in the
440 geostrophic calculation yields the highest contribution to the uncertainties in the AMOC
441 and MHT calculations. Knowledge of the reference level velocities at both the western and
442 eastern boundaries is necessary for considerably reducing the mean bias in the barotropic
443 mode. This can be achieved by using climatological values in the boundaries, and this
444 information may be acquired from available Argo float climatologies [e.g., *Goes et al.*,
445 2013b], for example. Although climatological reference velocities produce small mean
446 biases in the AMOC and MHT estimates (0.3 Sv and -0.02 PW, respectively), there is

447 still strong uncertainty in the lower frequency variability of the barotropic transport,
448 given by their rmse, which are ± 4.4 Sv and ± 0.14 PW. To resolve the variability of the
449 barotropic mode, additional available observations can be used. This question is addressed
450 in the next section.

451 **5.4.3. Alternative barotropic velocity estimation using altimetry and hydrog-** 452 **raphy**

453 In order to optimize the information necessary to monitor the AMOC at 34°S, several
454 additional observations could be used to complement the AX18 XBT transect measure-
455 ments. Some complimentary observations are already in place, such as the satellite wind
456 stress measurements used to estimate the Ekman transport.

457 A topic of current research in the AMOC decomposition is the estimation of the
458 barotropic mode. Using a reference level near the bottom of the ocean cannot capture
459 interannual or longer variability due to the presence of deep flows, since in this work cli-
460 matology is assumed below 800 m. Bottom pressure (P_{bot}) recorders are a useful platform
461 to compute the time varying reference level for the meridional geostrophic velocity, and,
462 therefore, estimate the non-steric component of the sea level height (SLH). Such a plat-
463 form requires further investment in an array across the basin, and efforts are underway
464 [*Perez et al.*, 2011; *Meinen et al.*, 2012]. Some recent studies use a blend of altimetry
465 and Argo parking velocity as the reference level or level of known motion to infer abso-
466 lute geostrophic velocities [*Willis and Fu*, 2008; *Mielke et al.*, 2013; *Goes et al.*, 2013b].
467 However, because a large number of Argo floats is necessary to produce a reliable esti-
468 mate, seasonal averages are generally used in an Argo-based reference level. We showed
469 in the previous section that a climatological assumption of the reference velocity in the

470 eastern and western boundaries can reduce the AMOC mean bias considerably. Here
471 we test another method for measuring the barotropic flow by using SLH derived from
472 satellite altimetry in conjunction with hydrographic data. Altimetry captures both steric
473 and non-steric components, whose contributions are variable among different regions of
474 the ocean [Guinehut et al., 2006]. The non-steric contribution generally increases toward
475 higher latitudes due to weaker stratification and stronger Coriolis force. In some regions
476 the non-steric contributions, such as the barotropic component, can account for more than
477 50% of the total sea level variability [Shriver and Hurlburt, 2000].

478 Using the hydrostatic relation, the total sea level can be accurately related to bottom
479 and atmospheric (P_{atm}) pressure, plus the steric contribution [Park and Watts, 2005],
480 respectively $SLH = (P_{bot} - P_{atm} - \rho_0 g H) / \rho_0 g$. In order to estimate the non-steric (P_{bot})
481 component of the sea level, we filter the steric contribution by calculating the residual
482 between SLH and the dynamic height (DH) referenced at a certain level (SLH - DH).
483 The barotropic velocities are calculated using geostrophy on this residual field, and the
484 maximum barotropic streamfunction calculated from these velocities is then compared to
485 the model barotropic streamfunction. Figure 12e shows how well this method represents
486 the barotropic velocities across the basin at a certain instant of time.

487 We consider DH referenced at a certain depth, and estimate the optimal reference depth
488 by varying the reference of DH from 300 m down to 3500 m deep (black curve with circles
489 in Figure 12). According to our results, the structure of the variability of the barotropic
490 velocities can be well captured by the non-steric sea level using this methodology. The
491 strength of the barotropic AMOC show correlations above 0.5 irrespective of the reference
492 level used in the DH estimation (Figure 12)b). High correlations (> 0.9) are found for a

493 DH reference level between 500 m and 1100 m. A low RMS region (< 5 Sv) is found for
494 a reference level between 700-1100 m (Figure 12a), and overlaps with the high correlation
495 region. The minimum RMS error of ~ 2.5 Sv is achieved when DH is referenced at
496 1000 m, where the bias in streamfunction is nearly zero (Figure 12)c), and standard
497 deviation is close to a minimum (Figure 12)d). Below 1000 m, the uncertainties increase
498 because assuming a deeper reference level for DH implies excluding the boundaries and
499 regions where the topography is shallower than the reference depth. Finally, we quantify
500 how much information is gained for the barotropic streamfunction estimation by using
501 altimetry data. We compare the altimetry derived barotropic streamfunction with one
502 calculated using the $\sigma_2 = 37.09$ as (i) a level of no motion or (ii) as the climatological
503 reference velocity in the western and eastern boundaries (red and green curves in Figure
504 12, respectively). The correlation (0.74) and the standard deviation (4.4 Sv) (Figures
505 12b, d) are the same for the cases with a level of no motion or a climatological reference
506 level at $\sigma_2 = 37.09$. Therefore, no gain exists in the variability of the barotropic mode by
507 applying these two different assumptions. The bias, however, as we also found in Figure
508 11, decreases considerably, and is close to zero when applying a climatological reference
509 level in the boundaries (Figure 12c). The bias reduction drives the reduction in RMS
510 from 7.2 Sv to 4.4 Sv between these two cases. Using altimetry and DH referenced at 800
511 m, the maximum depth of an XBT profile, promotes a reduction of approximately 2 Sv in
512 standard deviation and an increase of 0.15 in correlation towards the two approximations
513 for the reference level at $\sigma_2 = 37.09$. Although we did not include measurement errors
514 in these estimates, which would decrease the efficacy of the altimetry derived method,
515 we also did not include any extrapolation for the boundaries, which would increase the

516 efficacy of the method. Therefore, this result is a proof of concept that altimetry and
517 XBT data are complementary platforms for the inference of the long term variability of
518 the AMOC.

6. Conclusions

519 In this study we use a high resolution model assimilation product to assess the observa-
520 tional and computational uncertainties associated with estimating meridional transports
521 using the data from the AX18 XBT transect along 34°S. We analyzed the AMOC and
522 MHT in terms of their vertical shear, barotropic, and Ekman components. These terms
523 are here used to reconstruct the AMOC and MHT. We show that this method is well
524 suited for this type of work. In comparison to the AMOC calculated from the model
525 velocities, the reconstructed AMOC streamfunction is able to represent the main model
526 features, although the reconstruction cannot capture the high frequency reversals of the
527 model AMOC and MHT during austral winter/spring. A key finding obtained here is
528 that XBTs produce acceptable estimates of the AMOC and MHT variability, where the
529 uncertainties obtained by the multiple sources of error are smaller than the signal of the
530 time series variability. Therefore, the AX18 transect is a valuable and longstanding piece
531 of a multiple platform monitoring system for the region, and efforts should be made to
532 maintain and improve it. The results obtained here are summarized in Table 1, and the
533 results of *Baringer and Garzoli* [2007] for MHT is added for comparison. As follows, we
534 make recommendations for optimization of sampling and computational methodologies to
535 improve estimates of the AMOC and meridional MHT:

- 536 • The effect of T-S padding of monthly climatology below 800 m on the AMOC (0.03
537 ± 2.4 Sv) and MHT (-0.02 ± 0.13) estimates is small in comparison to the other error

538 sources. The effect of using salinity from the T-S lookup table in the upper 800 m is also
539 small in comparison to the other components, and is about the same order as the deep
540 ocean padding. However, seasonal biases in the annual climatology can produce AMOC
541 monthly biases of as much as 1 Sv. Salinity from other measurements, such as Argo, can
542 produce monthly climatologies of T-S relationships, which would in principle avoid these
543 seasonal biases.

544 • Current quarterly sampling causes an average RMS error of ± 2.3 Sv and ± 0.23 PW
545 in the climatological AMOC and MHT estimates, respectively. The optimal strategy to
546 reduce this sampling error would be to carry out 12 transects per year, i.e. one per month,
547 which is not feasible due to operational constraints. More realistically, it is desirable to
548 conduct continuous realizations at current quarterly sampling for at least 15 years.

549 • Spatial subsampling in the interior produces small errors in the AMOC and MHT
550 estimates compared to the errors produced at the boundaries. The current AX18 zonal
551 sampling uses 25 km on the boundaries and 50 km in the interior of the basin. This current
552 spatial sampling seems to be adequate to capture most of the variability of the meridional
553 transports, although the western boundary resolution still shows large AMOC bias at the
554 present sampling (1.7 ± 2.4 Sv). An increase in the western boundary sampling to 20 km
555 would improve the accuracy of the current AMOC calculations by ~ 1 Sv.

556 • As described in previous studies [e.g., *Kanzow et al.*, 2007, for 26.5°N], the barotropic
557 mode is likely to be the most significant source of error in the AMOC and MHT calcu-
558 lations due to the extensive continental shelf along 34°S . Errors are on the order of 5.7
559 ± 4.4 Sv for the AMOC and 0.17 ± 0.16 PW for MHT if a level of no motion is used in
560 $\sigma_2 = 37.09 \text{ kgm}^{-3}$. Using at least climatological values as the reference velocities in both

561 boundaries is necessary to reduce the AMOC and MHT mean biases to $\sim 0.3 \pm 4.4$ Sv
562 and 0.02 ± 0.14 PW, respectively.

563 • The use of satellite altimetry observations in conjunction with hydrographic data
564 is a good alternative for barotropic term estimation. We show that barotropic volume
565 transport estimates using the non-steric component of altimetry can improve the RMS
566 error by ~ 3 Sv in comparison to the commonly used level of no motion at $\sigma_2 = 37.09$
567 kgm^{-3} .

568 Finally, this study assesses only one the part of the several platforms that are in place to
569 monitor the variability of the AMOC and MHT in the South Atlantic, XBT and altimetry
570 data. The utility of the other operational platforms, such as moorings and Argo data,
571 has been demonstrated in various other studies [*Dong et al.*, 2011b; *Perez et al.*, 2011].
572 An analysis that includes a blend of several platforms is still necessary to evaluate the
573 optimal observational system for the region.

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References

- 587 Baehr, J., J. Hirschi, J.-O. Beismann, and J. Marotzke (2004), Monitoring the meridional
588 overturning circulation in the North Atlantic: A model-based array design study, *J.*
589 *Mar. Res.*, *62*(3), 283–312, doi:10.1357/0022240041446191.
- 590 Baehr, J., D. McInerney, K. Keller, and J. Marotzke (2008), Optimization of an observing
591 system design for the North Atlantic meridional overturning circulation, *J. Atmosph.*
592 *Ocean. Tech.*, *25*(4), 625–634, doi:10.1175/2007JTECHO535.1.
- 593 Baringer, M., and S. Garzoli (2007), Meridional heat transport determined with expend-
594 able bathythermographs, Part I: Error estimates from model and hydrographic data,
595 *Deep-Sea Res. I*, *54*(8), 1390–1401, doi:10.1016/j.dsr.2007.03.011.
- 596 Beal, L. M., W. P. M. D. Ruijter, A. Biastoch, R. Zahn, and S. 136 (2011), On the role
597 of the Agulhas system in ocean circulation and climate, *Nature*, *472*(7344), 429–436,
598 doi:10.1038/nature09983.
- 599 Biastoch, A., C. W. Böning, F. U. Schwarzkopf, and J. R. E. Lutjeharms (2009), Increase
600 in Agulhas leakage due to poleward shift in the southern hemisphere westerlies, *Nature*,
601 *462*, 495–498, doi:10.1038/nature08519.
- 602 Bryden, H. L., H. R. Longworth, and S. A. Cunningham (2005), Slowing of the
603 Atlantic meridional overturning circulation at 25°N, *Nature*, *438*, 655–657, doi:
604 10.1038/nature04385.

605 Chassignet, E., H. Hurlburt, E. Metzger, O. Smedstad, J. Cummings, G. Halliwell,
606 R. Bleck, R. Baraille, A. Wallcraft, C. Lozano, H. Tolman, A. Srinivasan, S. Han-
607 kin, P. Cornillon, R. Weisberg, A. Barth, R. He, F. Werner, and J. Wilkin (2009), U.S.
608 GODAE: Global ocean prediction with the hybrid coordinate ocean model (HYCOM),
609 *Oceanography*, *22*(2), 64–75, doi:10.5670/oceanog.2009.39.

610 Cummings, J. A. (2005), Operational multivariate ocean data assimilation, *Quart. J.*
611 *Royal Met. Soc., Part C*, *131*(613), 3583–3604, doi:10.1256/qj.05.105.

612 Dong, B.-W., and R. T. Sutton (2007), Enhancement of El Nino-Southern Oscillation
613 ENSO variability by a weakened Atlantic thermohaline circulation in a coupled GCM,
614 *J. Clim.*, *20*, 4920–4939, doi:10.1016/j.dsr2.2010.10.069.

615 Dong, S., S. L. Garzoli, M. O. Baringer, C. S. Meinen, and G. J. Goni (2009), Interannual
616 variations in the Atlantic meridional overturning circulation and its relationship with the
617 net northward heat transport in the South Atlantic, *Geophys. Res. Lett.*, *36*, L20,606,
618 doi:10.1029/2009GL039356.

619 Dong, S., S. Garzoli, and M. Baringer (2011a), The role of interocean exchanges on decadal
620 variations of the meridional heat transport in the South Atlantic, *J. Phys. Oceanogr.*,
621 *41*, 1498–1511, doi:10.1175/2011JPO4549.1.

622 Dong, S., M. Baringer, G. Goni, and S. Garzoli (2011b), Importance of the assimilation
623 of Argo float measurements on the meridional overturning circulation in the South
624 Atlantic, *Geophys. Res. Lett.*, *38*, L18,603, doi:10.1029/2011GL048982.

625 Donners, J., and S. S. Drijfhout (2004), The lagrangian view of South Atlantic intero-
626 cean exchange in a global ocean model compared with inverse model results, *J. Phys.*
627 *Oceanogr.*, *34*, 1019–1035, doi:10.1175/1520-0485(2004)034<1019:TLVOSA>2.0.CO;2.

628 Ducet, N., P.-Y. L. Traon, and G. Reverdin (2000), Global high-resolution mapping of
629 ocean circulation from Topex/Poseidon and ERS-1 and -2, *J. Geophys. Res.*, *105* (C8),
630 19,477–19,498, doi:10.1029/2000JC900063.

631 Enfield, D. B., A. M. Mestas-Nuez, and P. J. Trimble (2001), The Atlantic Multidecadal
632 Oscillation and its relation to rainfall and river flows in the continental U.S., *Geophysical*
633 *Research Letters*, *28*(10), 2077–2080, doi:10.1029/2000GL012745.

634 Fox, D., W. J. Teague, C. N. Barron, M. R. Carnes, and C. M. Lee (2002), The modular
635 ocean data assimilation system (MODAS), *J. Atmos. Ocean. Technol.*, *19*, 240–252,
636 doi:10.1175/1520-0426(2002)019<0240:TMODAS>2.0.CO;2.

637 Ganachaud, A., and C. Wunsch (2003), Large scale ocean heat and freshwater trans-
638 ports during the World Ocean Circulation Experiment, *J. Climate*, *16*, 696–705, doi:
639 10.1175/1520-0442(2003)016<0696:LSOHAF>2.0.CO;2.

640 Garzoli, S. (1993), Geostrophic velocities and transport variability in the Brazil/Malvinas
641 confluence, *Deep-Sea Res.*, *40*, 1379–1403, doi:10.1016/0967-0637(93)90118-M.

642 Garzoli, S., and M. Baringer (2007), Meridional heat transport determined with expend-
643 able bathythermographs. Part II: South Atlantic transport, *Deep-Sea Res. I*, *54*, 1402–
644 1420, doi:10.1016/j.dsr.2007.04.013.

645 Garzoli, S., M. Baringer, S. Dong, R. Perez, and Q. Yao (2013), South Atlantic meridional
646 fluxes, *Deep-Sea Res. I*, *71*, 21–32, doi:10.1016/j.dsr.2012.09.003.

647 Garzoli, S. L., and R. Matano (2011), The South Atlantic and the Atlantic merid-
648 ional overturning circulation, *Deep-Sea Res. Part II*, *58*(17–18), 1837–1847, doi:
649 10.1016/j.dsr2.2010.10.063.

650 Goes, M., N. M. Urban, R. Tonkonojenkov, M. Haran, A. Schmittner, and K. Keller
651 (2010), What is the skill of ocean tracers in reducing uncertainties about ocean diapycnal
652 mixing and projections of the atlantic meridional overturning circulation?, *J. Geophys.*
653 *Res.*, *115*, C12,006, doi:10.1029/2010JC006407.

654 Goes, M., G. Goni, and K. Keller (2013a), Reducing biases in XBT measurements by
655 including discrete information from pressure switches, *J. Atmos. Oceanic Technol.*, *30*,
656 810–824, doi:10.1175/JTECH-D-12-00126.1.

657 Goes, M., G. Goni, V. Hormann, and R. Perez (2013b), Variability of the Atlantic off-
658 equatorial eastward currents during 1993-2010 using a synthetic method, *J. Geophys.*
659 *Res.-Oceans*, *118*(6), 3026 – 3045, doi:10.1002/jgrc.20186.

660 Goni, G., and I. Wainer (2001), Investigation of the Brazil Current front variability from
661 altimeter data, *J. Geophys. Res.*, *106*, 31,117–31,128, doi:10.1029/2000JC000396.

662 Goni, G., S. Garzoli, A. Roubicek, D. Olson, and O. Brown (1997), Agulhas ring dynamics
663 from TOPEX/POSEIDON satellite altimeter data, *J. Mar. Res.*, *55*(5), 861–883, doi:
664 10.1357/00222409732224175.

665 Goni, G., F. Bringas, and P. D. Nezio (2011), Observed low frequency variability of the
666 Brazil Current front, *J. Geophys. Res.*, *116*, C10,037, doi:10.1029/2011JC007198.

667 Gordon, A. (1986), Interocean exchange of thermocline water, *J. Geophys. Res.*, *91*, 5037–
668 5046, doi:10.1029/JC091iC04p05037.

669 Griffies, S. M., M. J. Harrison, R. C. Pacanowski, and A. Rosati (2004), A technical guide
670 to MOM4, GFDL Ocean Group, *Tech. Rep. 5*, NOAA/GFDL, Princeton, NJ.

671 Guinehut, S., P.-Y. L. Traon, and G. Larnicol (2006), What can we learn from
672 global altimetry/hydrography comparisons?, *Geophys. Res. Lett.*, *33*, L10,604, doi:

673 10.1029/2005GL0255551.

674 Hall, M. M., and H. L. Bryden (1982), Direct estimates and mechanisms of ocean heat
675 transport, *Deep-Sea Res.*, *29*(3), 339–359, doi:10.1016/0198-0149(82)90099-1.

676 Hatun, H., A.-B. Sandø, H. Drange, B. Hansen, and H. Valdimarsson (2005), Influence
677 of the atlantic subpolar gyre on the thermohaline circulation, *Science*, *309*, 1841–1844,
678 doi:10.1126/science.1114777.

679 Hawkings, E., R. S. Smith, L. C. Allison, J. M. Gregory, T. J. Woollings, H. Pohlmann,
680 and B. de Cuevas (2011), Bistability of the Atlantic overturning circulation in a global
681 climate model and links to ocean freshwater transport, *Geophys Res Lett.*, *38*, L10,605,
682 doi:10.1029/2011GL047208.

683 Hirschi, J., J. Baehr, J. Marotzke, J. Stark, S. Cunningham, and J.-O. Beismann (2003),
684 A monitoring design for the Atlantic meridional overturning circulation, *Geophys. Res.*
685 *Lett.*, *30*, 1413, doi:10.1029/2002GL016776.

686 Hu, A., G. A. Meehl, W. Han, and J. Yin (2011), Effect of the potential melting of the
687 Greenland ice sheet on the meridional overturning circulation and global climate in the
688 future, *Deep-Sea Res. II*, *58*, 1914–1926, doi:10.1029/2000GL012745.

689 Jayne, S. R., and J. Marotzke (2001), The dynamics of ocean heat transport variability,
690 *Rev. Geophys.*, *39*, 385–411, doi:10.1029/2000RG000084.

691 Kanzow, T., S. A. Cunningham, D. Rayner, J. J.-M. Hirschi, W. E. Johns, M. O. Baringer,
692 H. L. Bryden, L. M. Beal, C. S. Meinen, and J. Marotzke (2007), Observed flow compen-
693 sation associated with the MOC at 26.5 degrees N in the Atlantic, *Science*, *317*(5840),
694 938–941, doi:10.1126/science.1141293.

695 Lee, T., and J. Marotzke (1998), Seasonal cycles of meridional overturning and heat
696 transport of the Indian Ocean, *J. Phys. Oceanogr.*, *28*, 923–943, doi:10.1175/1520-
697 0485(1998)028<0923:SCOMOA>2.0.CO;2.

698 Lentini, C., G. Goni, and D. Olson (2006), Investigation of Brazil Current rings in the
699 confluence region, *J. Geophys. Res.*, *111*(C06013), doi:10.1029/2005JC002988.

700 Levermann, A., A. Griesel, M. Hofmann, M. Montoya, and S. Rahmstorf (2005), Dynamic
701 sea level changes following changes in the thermohaline circulation, *Climate Dyn.*, *24*,
702 347–354, doi:10.1007/s00382-004-0505-y.

703 Locarnini, R. A., A. V. Mishonov, J. I. Antonov, T. P. Boyer, and H. E. Garcia (2006),
704 World Ocean Atlas 2005, *Tech. Rep. V. 1: Temperature*, NOAA Atlas NESDIS 61, U.S.
705 Government Printing Office, Washington, D.C.

706 Lohmann, K., H. Drange, and M. Bentsen (2009), A possible mechanism for the strong
707 weakening of the north atlantic subpolar gyre in the mid-1990s, *Geophys. Res. Lett.*,
708 *36*, L15,602, doi:1029/2009GL039166.

709 Marshall, J., and F. Schott (1999), Open-ocean convection: Observations, theory and
710 models, *Rev. Geophys.*, *37*, 1–64, doi:10.1029/98RG02739.

711 Meinen, C. S., A. R. Piola, R. C. Perez, and S. L. Garzoli (2012), Deep Western Boundary
712 Current transport variability in the South Atlantic: preliminary results from a pilot
713 array at 34.5° S, *Ocean Sci. Discuss.*, *9*, 977–1008, doi:10.5194/osd-9-977-2012.

714 Mello, R. L., A. C. N. Freitas, L. Russo, J. F. Oliveira, C. A. S. Tanajura, and J. B. R.
715 Alvarenga (2013), Ocean forecasts in the southwestern Atlantic: Impact of different
716 sources of sea surface height in data assimilation, *Rev. Bras. de Geóscica*, *31*(2), 243–
717 255.

718 Mielke, C., E. Frajka-Williams, and J. Baehr (2013), Observed and simulated variabil-
719 ity of the AMOC at 26°N and 41°N, *Geophys. Res. Lett.*, *40*(6), 1159–1164, doi:
720 10.1002/grl.50233.

721 Montgomery, R. B. (1974), Comments on Seasonal variability of the Florida current, by
722 Niiler and Richardson, *J. Mar. Res.*, *32*, 533–535.

723 Park, J.-H., and D. R. Watts (2005), Response of the southwestern Japan/East Sea to the
724 atmospheric pressure, *Deep-Sea Res. II*, *52*, 1671–1683, doi:10.1016/j.dsr2.2003.08.007.

725 Perez, R. C., S. L. Garzoli, C. Meinen, and R. P. Matano (2011), Geostrophic velocity
726 measurement techniques for the meridional overturning circulation and meridional heat
727 transport in the South Atlantic, *J. Atmos. and Ocean. Tech.*, *28*(11), 1504–1521, doi:
728 10.1175/JTECH-D-11-00058.1.

729 Pond, S., and G. Pickard (1983), *Introductory Dynamical Oceanography*, Pergamon in-
730 ternational library of science, technology, engineering and social studies, Butterworth-
731 Heinemann.

732 Rahmstorf, S. (1996), On the freshwater forcing and transport of the Atlantic thermoha-
733 line circulation, *Clim. Dyn.*, *12*, 799–811, doi:10.1007/s003820050144.

734 Rayner, D., J. J.-M. Hirschi, T. Kanzow, W. E. Johns, P. G. Wright, E. Frajka-Williams,
735 H. L. Bryden, C. S. Meinen, M. O. Baringer, J. Marotzke, L. M. Beal, and S. A.
736 Cunningham (2011), Monitoring the Atlantic meridional overturning circulation, *Deep-*
737 *Sea Res. II*, *58*(17–18), 1744–1753, doi:10.1016/j.dsr2.2010.10.056.

738 Richardson, P., and S. Garzoli (2003), Characteristics of intermediate water flow in the
739 Benguela Current as measured with RAFOS floats, *Deep-Sea Res.*, *50*, 87–118, doi:
740 10.1016/S0967-0645(02)00380-6.

741 Sabine, C., R. Feely, N. Gruber, R. Key, K. Lee, J. Bullister, R. Wanninkhof, C. Wong,
742 D. Wallace, B. Tilbrook, et al. (2004), The oceanic sink for anthropogenic CO₂, *Science*,
743 *305*, 367–371, doi:10.1126/science.1097403.

744 Shriver, J. F., and H. E. Hurlburt (2000), The effect of upper ocean eddies on the non-
745 steric contribution to the barotropic mode, *Geophys. Res. Lett.*, *27*, 2713–2716, doi:
746 10.1029/1999GL011105.

747 Sime, L. C., D. P. Stevens, K. J. Heywood, and K. I. Oliver (2006), A decomposition
748 of the Atlantic meridional overturning, *J. Phys. Oceanogr.*, *36*(12), 2253–2270, doi:
749 10.1175/JPO2974.1.

750 Stramma, L., and M. England (1999), On the water masses and mean circulation
751 of the South Atlantic Ocean, *J. Geophys. Res.*, *104*((C9)), 20,863–20,883, doi:
752 10.1029/1999JC900139.

753 Sutton, R. T., and D. L. R. Hodson (2005), Atlantic Ocean forcing of North American
754 and European summer climate, *Science*, *309*, 115–118, doi:10.1126/science.1109496.

755 Thacker, W. C. (2008), Estimating salinity between 25° and 45°S in the At-
756 lantic ocean using local regression, *J. Atmos. Ocean. Tech.*, *25*, 114–130, doi:
757 10.1175/2007JTECHO530.1.

758 Timmermann, A., Y. Okumura, S.-I. An, A. Clement, B. Dong, E. Guilyardi, A. Hu, J. H.
759 Jungclaus, M. Renold, T. F. Stocker, R. J. Stouffer, R. Sutton, S.-P. Xie, and J. Yin
760 (2007), The influence of a weakening of the Atlantic meridional overturning circulation
761 on ENSO, *J. Climate*, *20*, 4899–4919, doi:10.1175/JCLI4283.1.

762 Treguier, A. M., M. England, S. R. Rintoul, G. Madec, J. L. Sommer, and J.-M. Molines
763 (2007), Southern Ocean overturning across streamlines in an eddy simulation of the

764 Antarctic circumpolar current, *Ocean Sci.*, *3*, 491–507, doi:10.5194/os-3-491-2007.

765 Wainer, I., P. Gent, and G. Goni (2000), Annual cycle of the Brazil-Malvinas conflu-
766 ence region in the National Center for Atmospheric Research climate system model, *J.*
767 *Geophys. Res.*, *05*((C11)), 26,167–26,177, doi:10.1029/1999JC000134.

768 Weijer, W., W. P. M. D. Ruijter, H. A. Dijkstra, and P. J. van Leeuwen (1999), Impact
769 of interbasin exchange on the Atlantic overturning circulation, *J. Phys. Oceanogr.*, *29*,
770 2266–2284.

771 Willis, J., and L.-L. Fu (2008), Combining altimeter and subsurface float data to estimate
772 the time-averaged circulation in the upper ocean, *J. Geophys. Res.*, *113*(C12), 2156–
773 2202, doi:10.1029/2007JC004690.

774 Woollings, T., J. M. Gregory, J. G. Pinto, M. Reyers, and D. J. Brayshaw (2012), Re-
775 sponse of the North Atlantic storm track to climate change shaped by ocean-atmosphere
776 coupling, *Nat. Geosci.*, *5*, 313–317, doi:10.1038/ngeo1438.

777 Zhang, R., and T. L. Delworth (2006), Impact of Atlantic multidecadal oscillations on
778 India/Sahel rainfall and Atlantic hurricanes, *Geophys. Res. Lett.*, *33*, L17,712, doi:
779 10.1029/2006GL026267.

Table 1. Bias \pm RMS error of the AMOC (Sv) and MHT (PW) introduced by each source of error associated with the AX18 XBT transect observational assumptions estimated in the present study. Last column shows the error estimates of *Baringer and Garzoli* [2007], Table 3.

Source	AMOC (Sv)		Meridional Heat Transport (PW)
	Present	Present	B&G
Upper ocean salinity	0.35 ± 2.8	0.04 ± 0.17	0.03
Deep climatology below 800 m	-0.03 ± 2.4	-0.02 ± 0.13	0.15
Mass imbalance	0.9 ± 3.8	-0.02 ± 0.06	0.02
Non-synopticity	0.2 ± 4.1	0.01 ± 0.25	–
Quarterly sampling	± 2.3	± 0.23	–
Unresolved western shelf transport	-0.6 ± 0.8	10^{-8}	0.01
Unresolved eastern shelf transport	0.15 ± 0.4	10^{-8}	0.01
Western Horizontal resolution (25 km)	1.7 ± 2.4	0.03 ± 0.06	–
Eastern Horizontal resolution (25 km)	1.0 ± 1.4	-0.03 ± 0.04	–
Interior Horizontal resolution(50 km)	-0.1 ± 1.1	0.01 ± 0.06	–
Western Reference level	4.0 ± 4.5	0.06 ± 0.16	0.05
Eastern Reference level	2.0 ± 4.3	0.10 ± 0.14	0.05

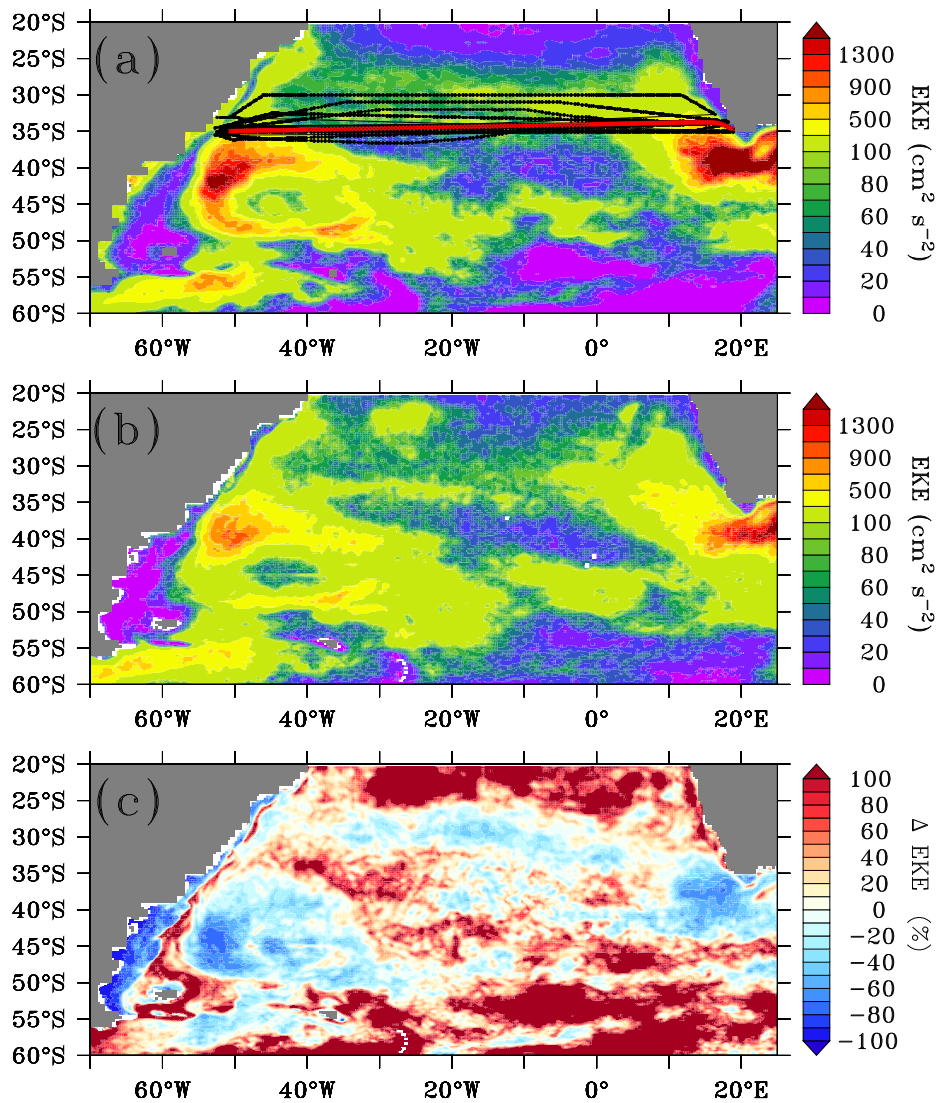


Figure 1. Eddy kinetic energy ($\text{cm}^2 \text{s}^{-2}$) calculated from sea level anomalies for the period between 2007 and 2013. (a) AVISO observations, (b) HYCOM model, and (c) HYCOM minus observations (in percentage changes). The black lines in Figure 1a are the locations of the 18 selected AX18 transects between 2002 and 2012, overlaid by the mean AX18 transect location in red.

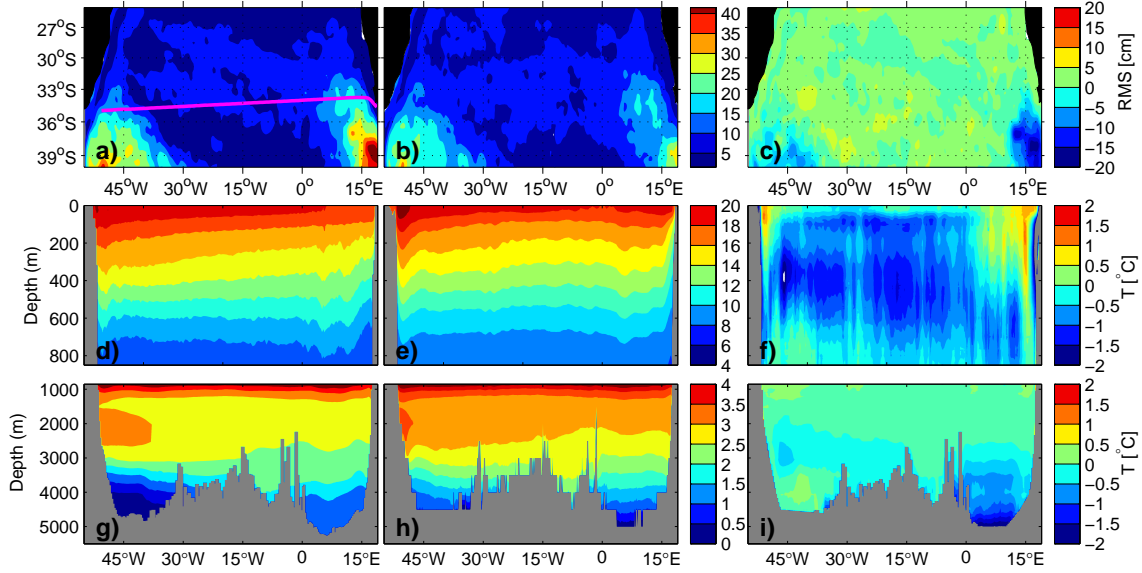


Figure 2. (a) – (c) Sea level anomaly (SLA) root-mean-square (RMS) contours (in cm) for: (a) AVISO overlaid by the mean AX18 transect (magenta line); (b) HYCOM/NCODA; (c) HYCOM/NCODA minus AVISO. (d)–(i): Mean temperature sections contours (in °C) for: (d, g) observations, with AX18 data for the upper 850 m (d) and WOA05 for 850 m to bottom (g); (e, h) HYCOM/NCODA model; (f, i) HYCOM/NCODA minus observations.

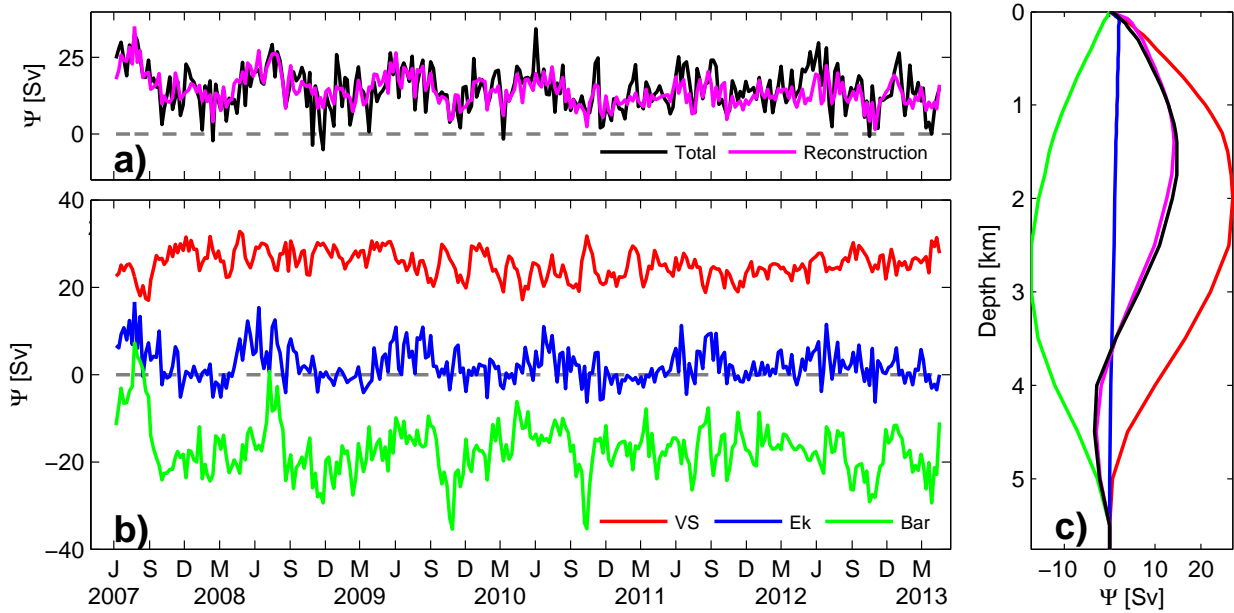


Figure 3. (a) Maximum volume transport streamfunction (AMOC) using model velocities (black) and the reconstruction (magenta). (b) AMOC decomposition into vertical shear (red), Ekman (blue), and barotropic (green) components. (c) Time mean meridional transport streamfunction for the model velocities (black), reconstruction (magenta), Ekman (blue), vertical shear (red) and barotropic (green).

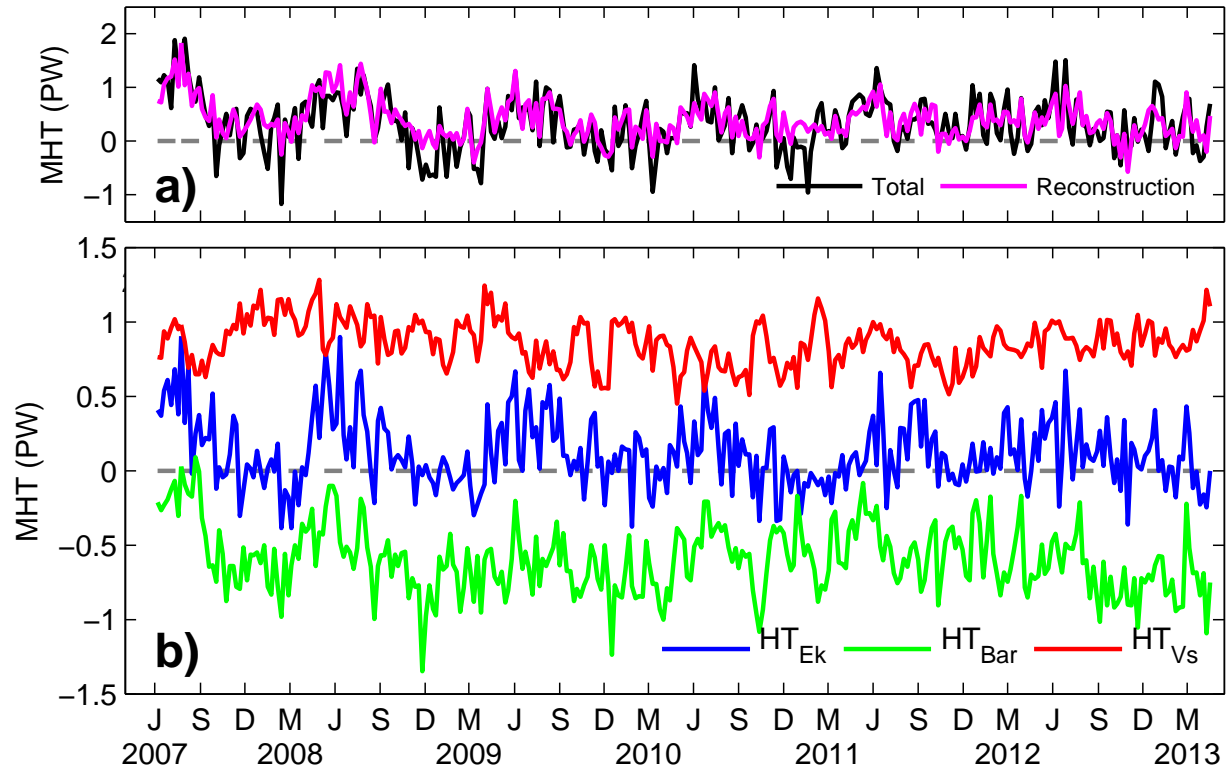


Figure 4. (a) Heat transport (MHT in PW) using model velocities (black) and reconstruction (magenta). (b) MHT decomposition into vertical shear (red), Ekman (blue), and barotropic (green) components.

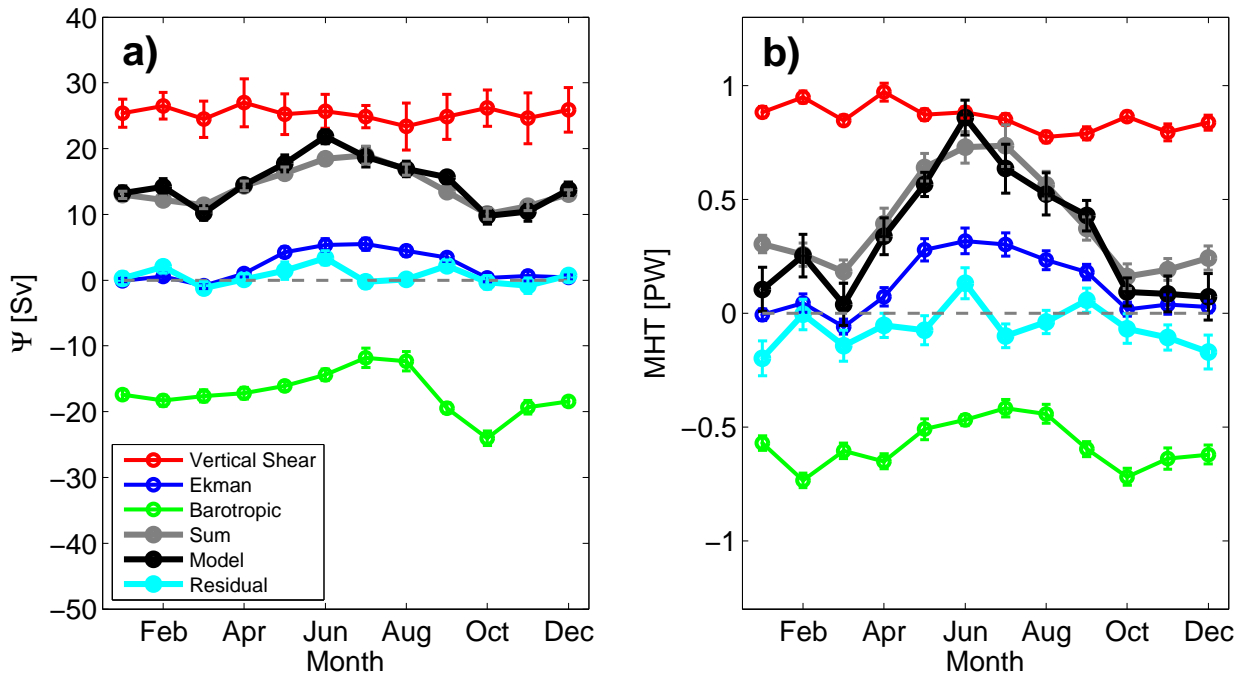


Figure 5. Monthly means of the (a) AMOC and (b) MHT components: vertical shear (red), Ekman (blue) and barotropic (green). The level of reference is assumed to be on the ocean bottom using the model bottom velocities as the reference. The sum of the transport components (gray) is comparable to the total transport from the original model velocities (black).

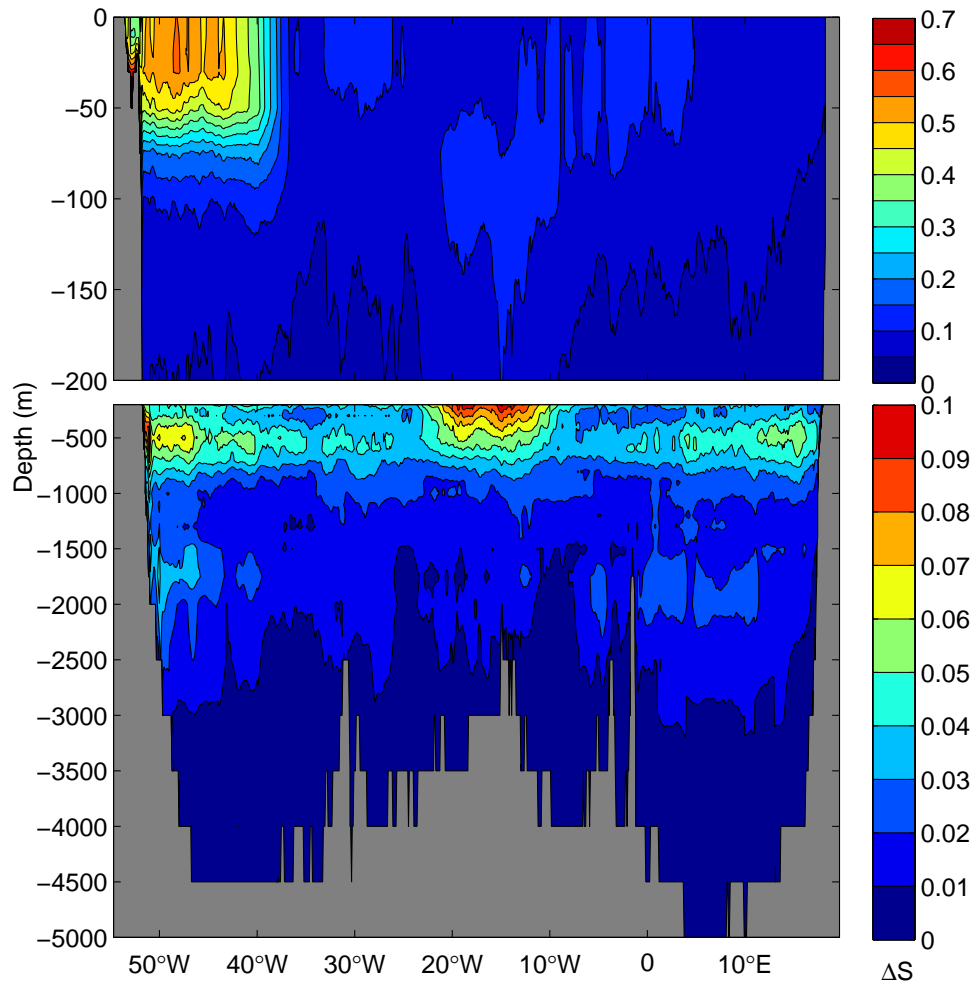


Figure 6. RMS error (psu) between the estimated salinity using climatological T-S relationships and the model salinity along the 34.5°S section.

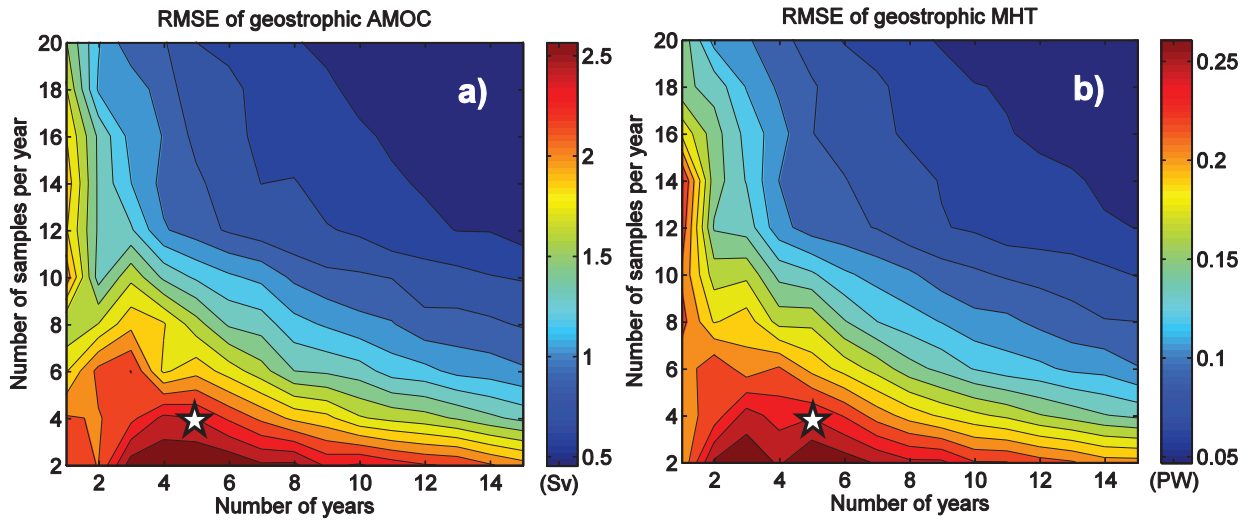


Figure 7. RMS error of geostrophic AMOC (a) and MHT (b) associated with different time samplings, i.e., the number of samples per year (y-axis) and the number of year (x-axis). The RMS error is calculated from the difference between the reconstructed time series using a different time sampling and the reconstructed time series using the original model sampling. The number of samples per year is randomly selected, and this process is realized 400 times to average the random realizations. The stars in (a) and (b) correspond to the current location of the AX18 sampling in the time sampling parameter space.

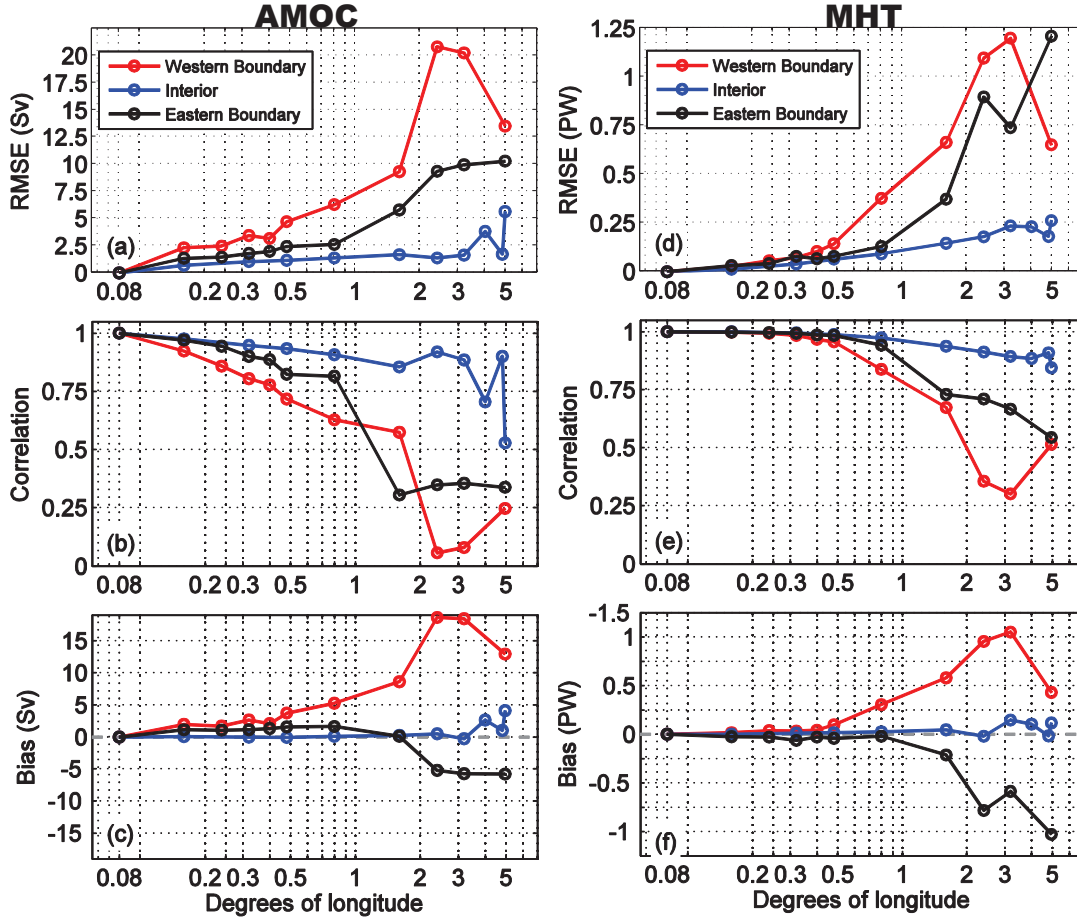


Figure 8. RMS error, correlation, and bias of the AMOC (a, b, c) and MHT (d, e, f) with respect to the simulated longitudinal resolution (in degrees) of the AX18 transect. The transect horizontal resolution varies individually for three regions, western boundary (red), interior (blue) and eastern boundary (black). The x-axis is shown in logarithmic scale.

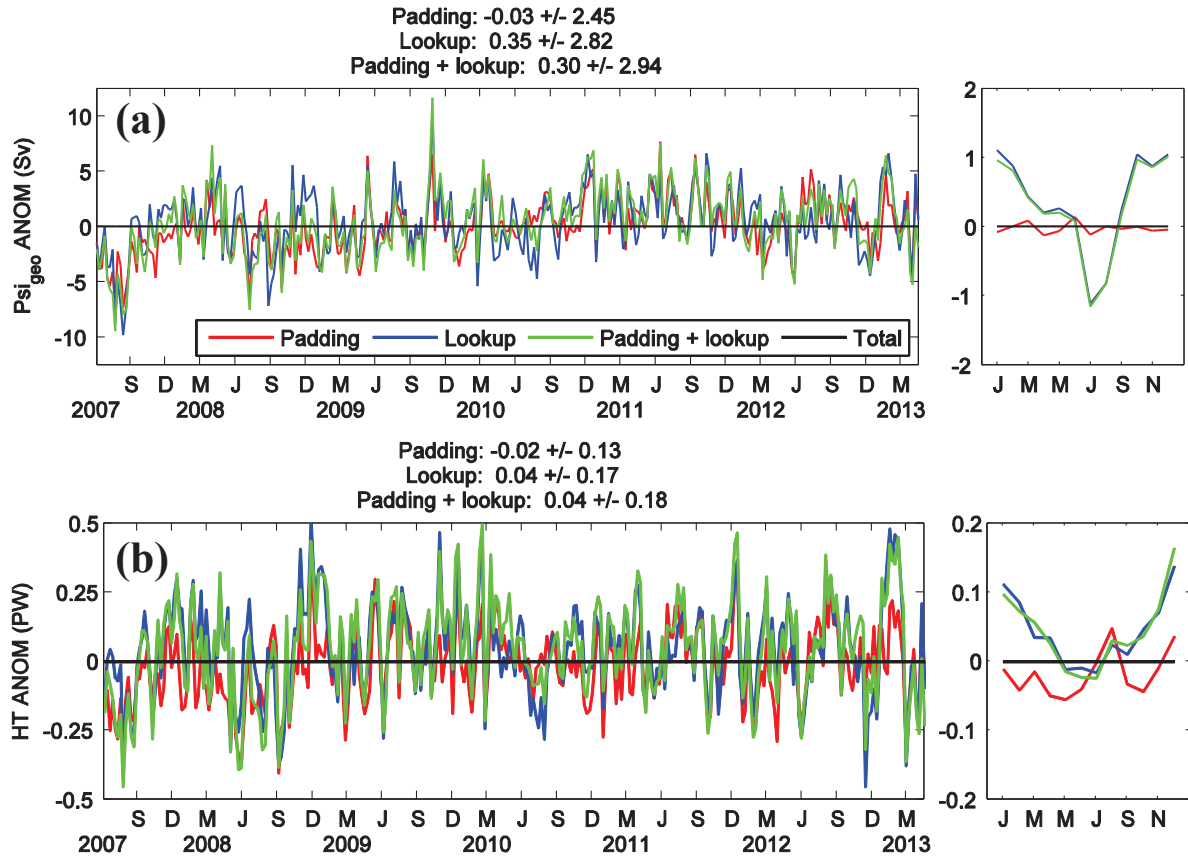


Figure 9. Anomalies relative to the total model field time series of (a) geostrophic AMOC and (b) MHT, and respective monthly averages (right panels). The total field anomalies are defined as having zero value (black), and the colored time series assume a bottom T-S climatology padding (red), salinity inference from lookup table in the top 800 m (blue), padding plus T-S lookup (green), and the total (black).

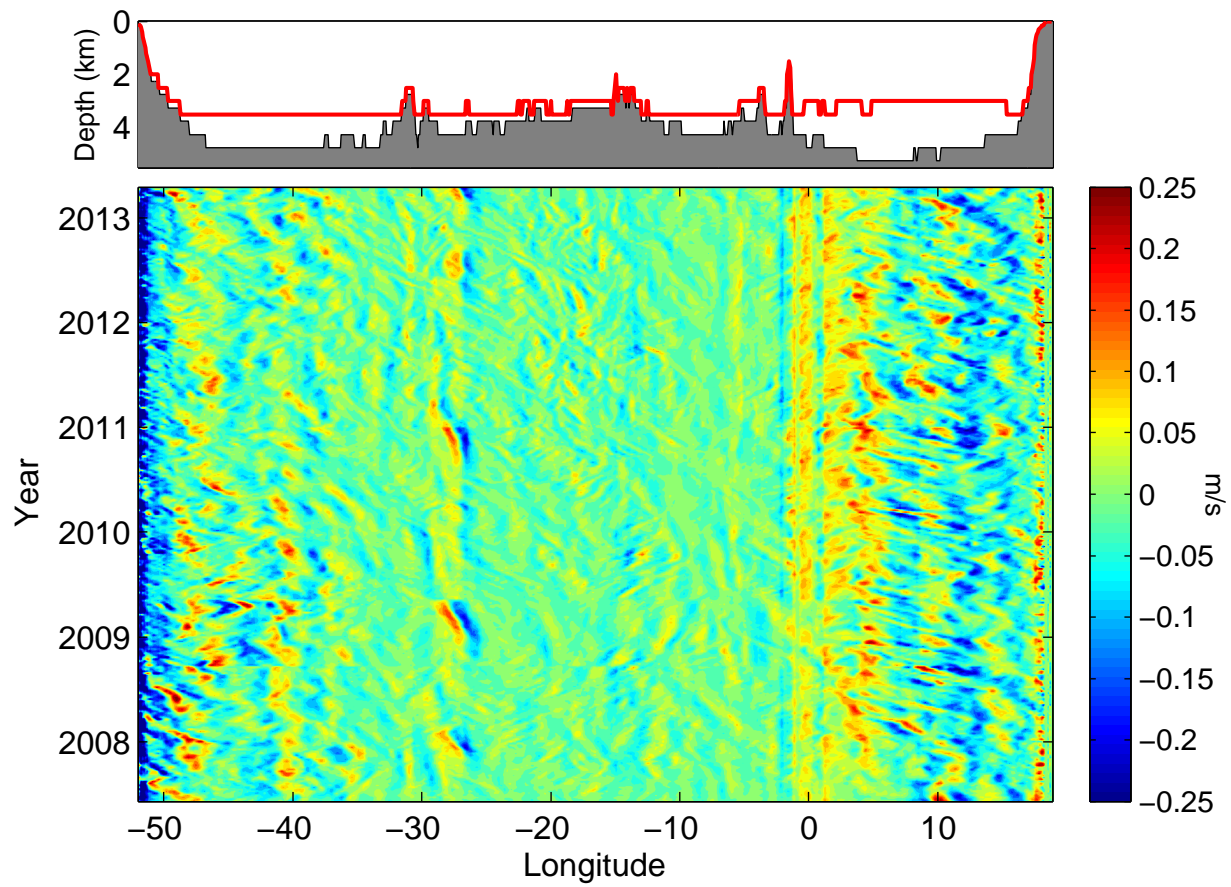


Figure 10. Barotropic velocities at 34.5°S estimated from the model velocities. The top panel shows the average depth of the $\sigma_2 = 37.9$ (red line) overlaid on model bathymetry

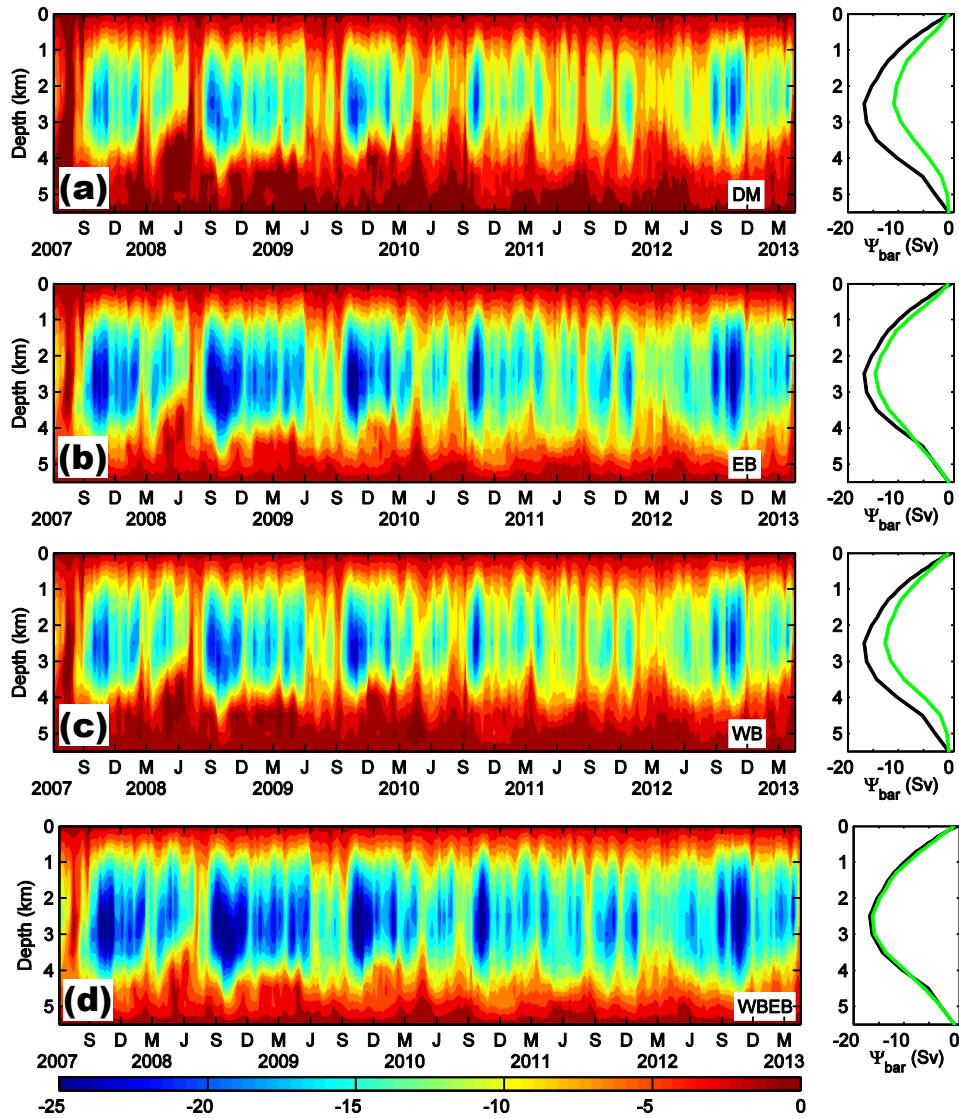


Figure 11. Changes in the barotropic streamfunction (Sv) due to the knowledge of a climatological reference velocity at $\sigma_2 = 37.09$. (a) Zero reference velocity, (b) eastern boundary, (c) western boundary, and (d) western plus eastern boundaries. Left panels: time evolution of the barotropic streamfunction. Right panels: green line is the time average of the barotropic streamfunction shown on the left panels, and black line is the time average of the original model barotropic streamfunction.

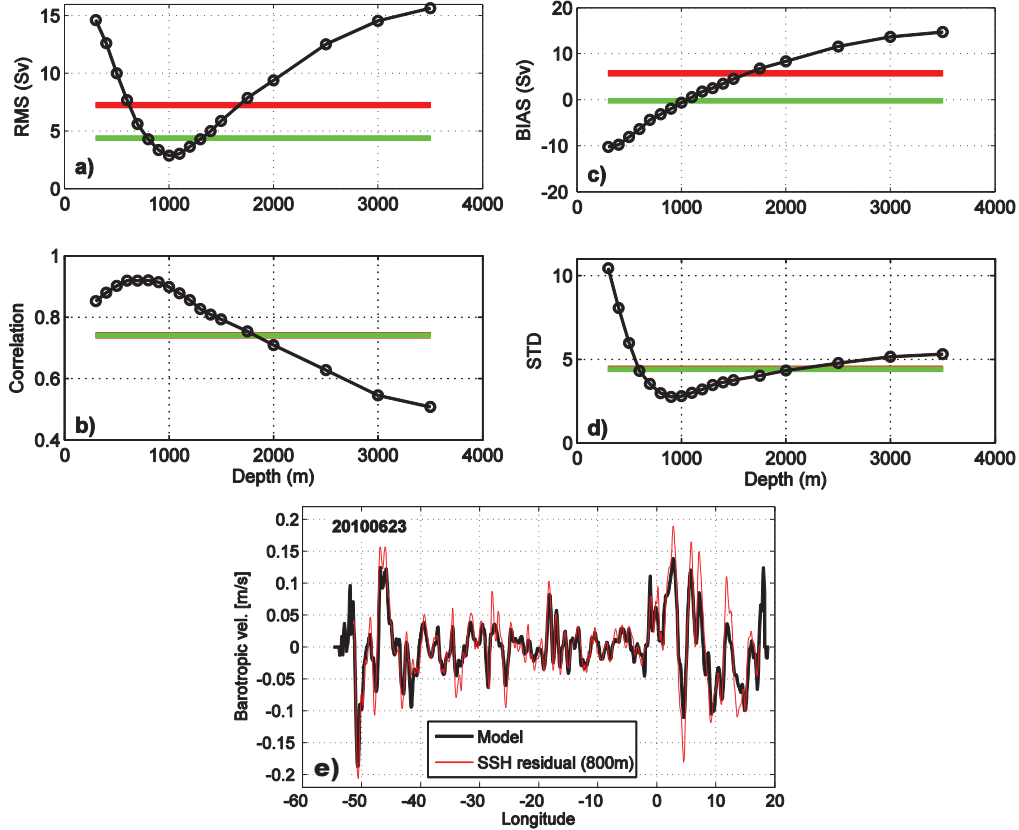


Figure 12. a) RMS error (Sv), (b) correlation, (c) bias (Sv) and (d) standard deviation (Sv) between the barotropic streamfunction strength for the barotropic velocities calculated from the SLH-DH residual with a variable reference level (x-axis) from 300 m to 3500 m depth (black line with open dots). The respective values of the barotropic streamfunction strength calculated using geostrophic velocities referenced to a level of no motion at $\sigma_2 = 37.09 \text{ kg m}^{-3}$ (red curve), and using the climatological model velocity values on the boundaries at $\sigma_2 = 37.09 \text{ kg m}^{-3}$ (green curve). (e) Comparison of a snapshot between the barotropic velocities (m/s) calculated from model velocities (black) and using the SSH-DH residual