
Diagnosing Vertical Motion in the Equatorial Atlantic

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(Météo-France/CNRM/GAME)

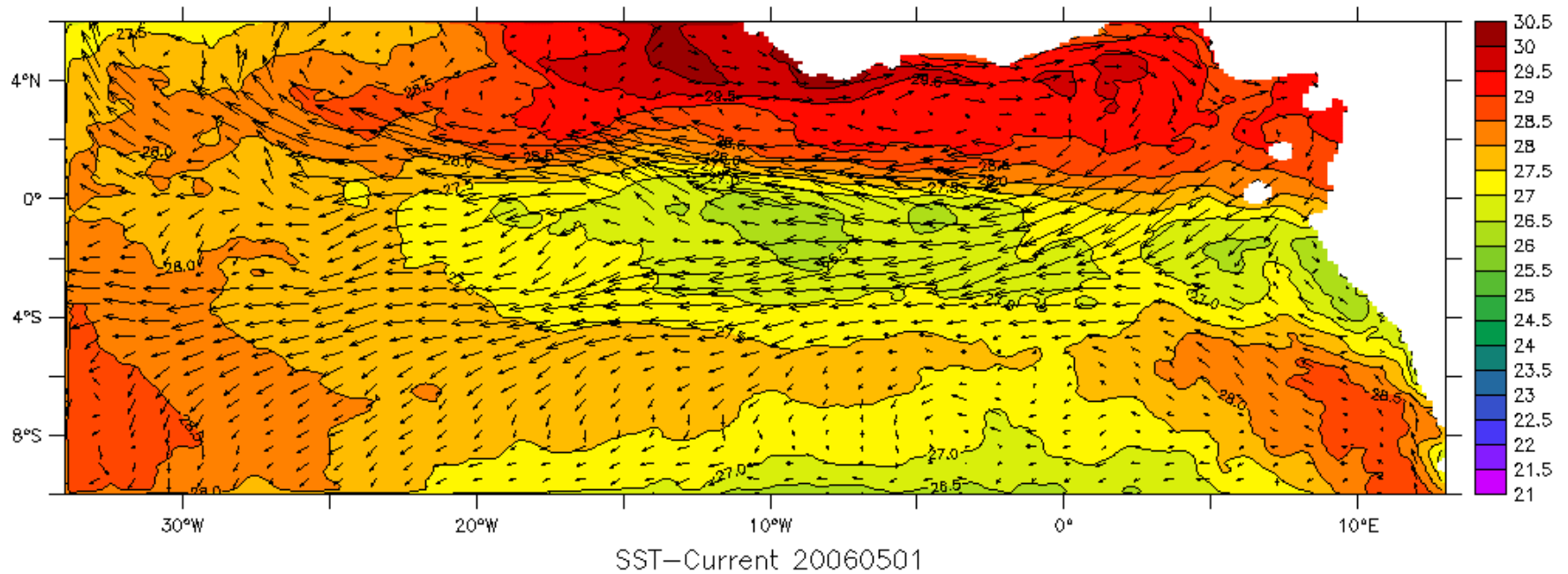
The Regional Model

(Giordani et al., 2005a,b)

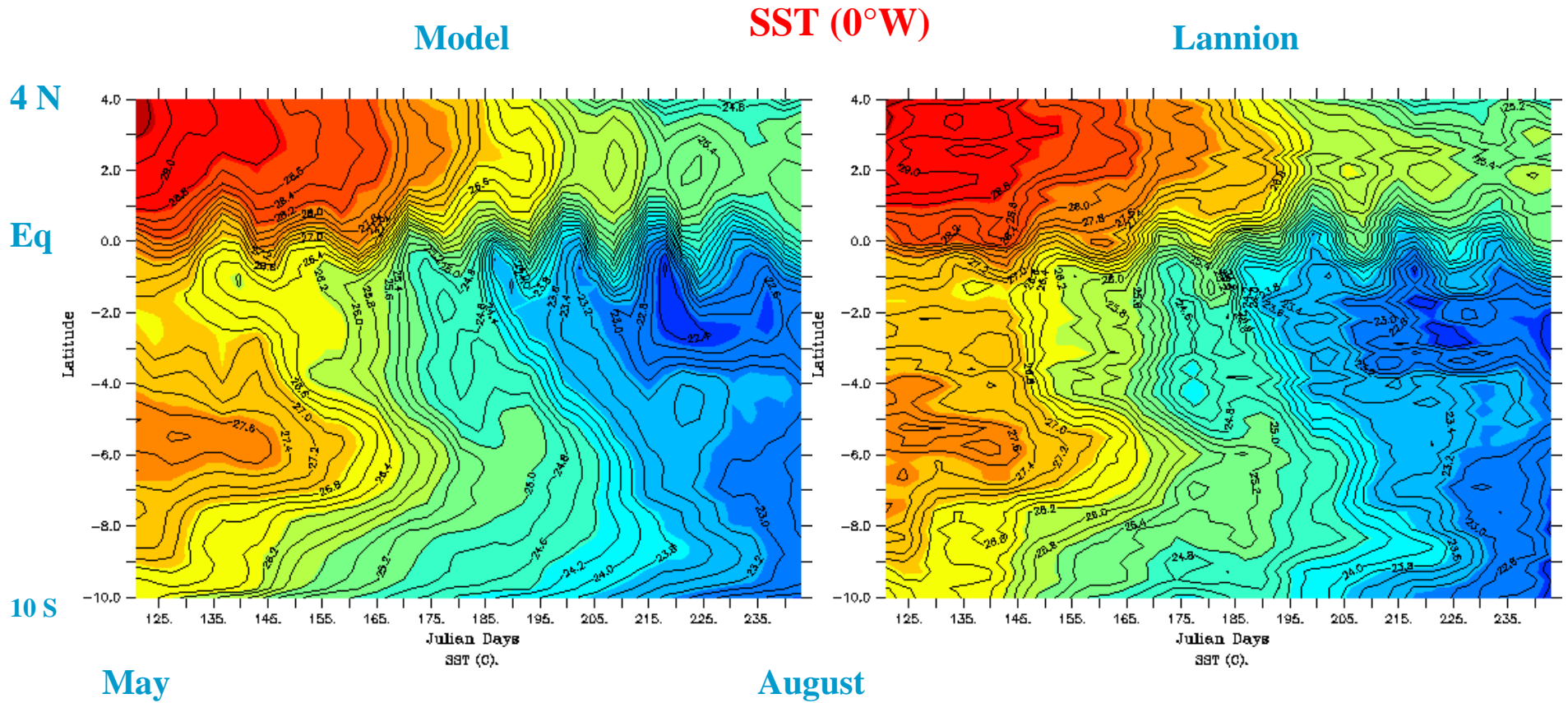
- Primitive Equation Model implemented in the Atlantic Equatorial region
- Atlantic Cold Tongue development during EGEE-3
- Processes studies \Rightarrow How works the Equatorial upwelling ?

Simulation: MJJA 2006

AMMA/EGEE P3D Model (Herve Giordani)



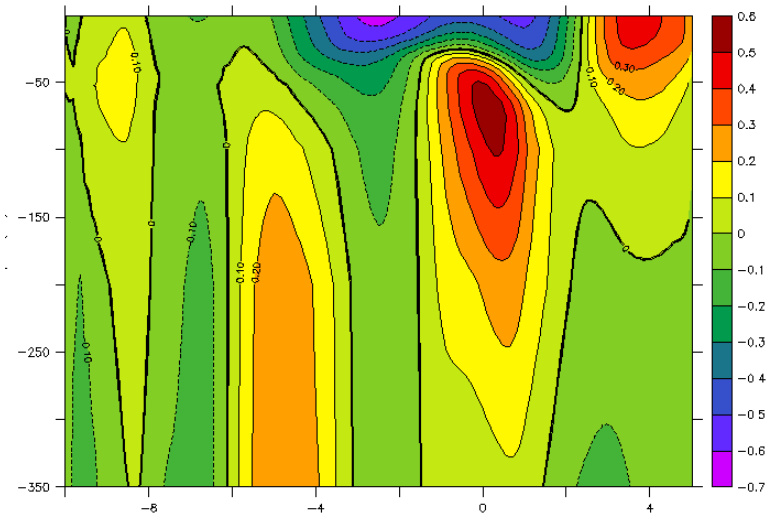
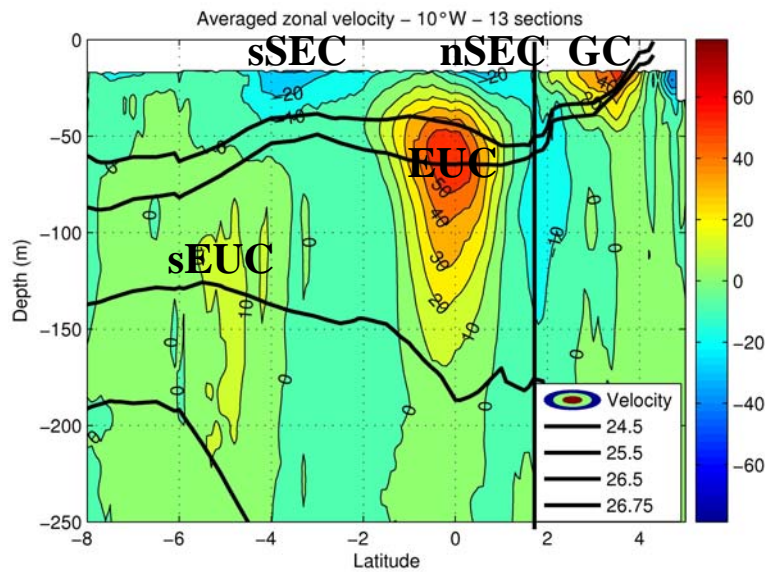
Validation



Validation

Observation-Mean EUC at 10°W
Courtesy B. Bourlès

Model



How to identify the sources of vertical velocity ?

Ocean β -plan slab model
(Zebiak and Cane, 1987)

$$\begin{cases} ru_s - \beta y v_s = \frac{\tau_x}{\rho_0 H} \\ \beta y u_s + r v_s = \frac{\tau_y}{\rho_0 H} \end{cases}$$

$r = \frac{1}{T}$ Adjustment frequency
of the Newtonian damping

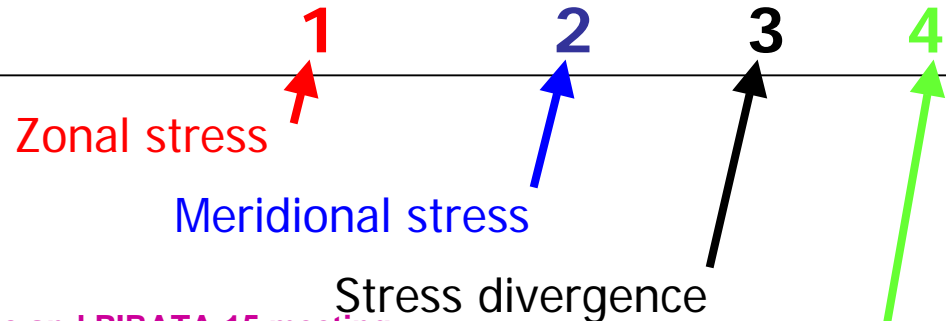
Ekman Transport

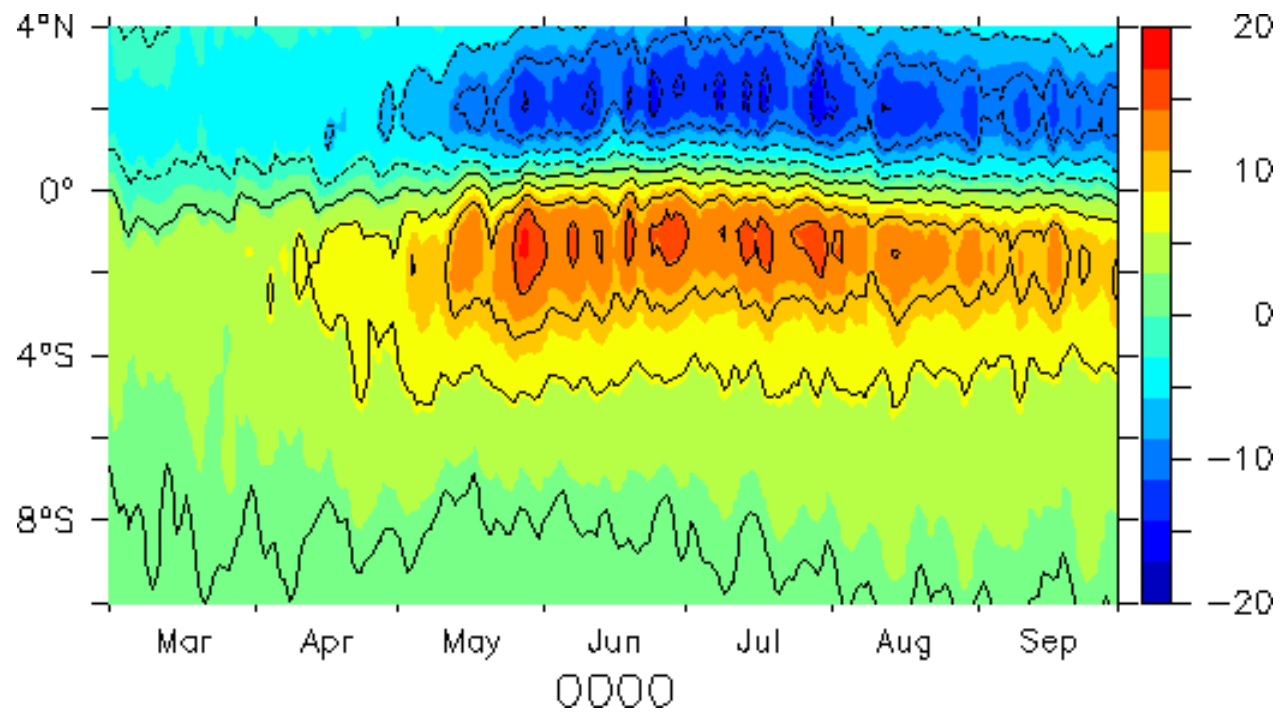
$$\begin{cases} u_s = \frac{1}{\rho_0 H} \frac{r\tau_x + \beta y \tau_y}{r^2 + \beta^2 y^2} \\ v_s = \frac{1}{\rho_0 H} \frac{r\tau_y - \beta y \tau_x}{r^2 + \beta^2 y^2} \end{cases}$$

Current only induced by the surface stress τ
No vertical shear of the current

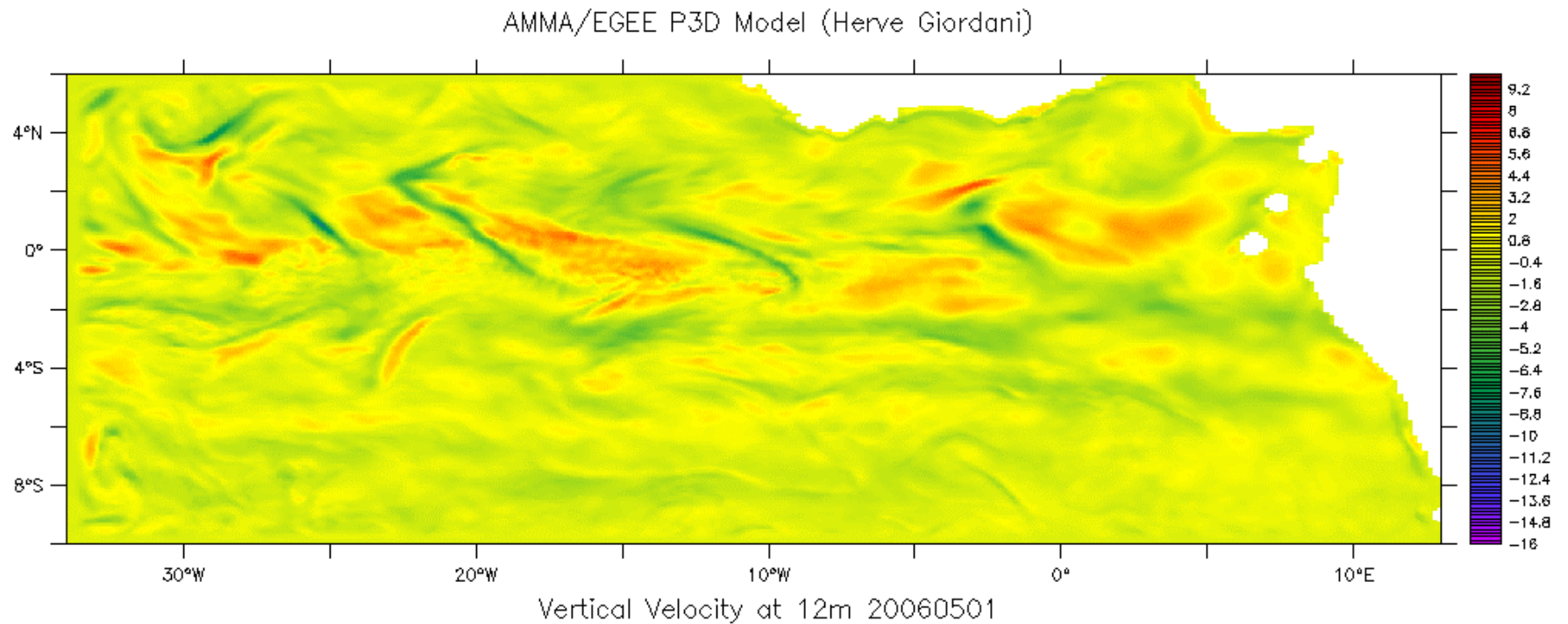
Ekman pumping

$$w(-H) = \frac{1}{\rho_0 (r^2 + \beta^2 y^2)} \left\{ \frac{\beta(\beta^2 y^2 - r^2)}{r^2 + \beta^2 y^2} \tau_x + \frac{-2\beta^2 y r}{r^2 + \beta^2 y^2} \tau_y + r \nabla \cdot \tau + \beta y \nabla \wedge \tau \right\}$$





Simulation: MJJA 2006

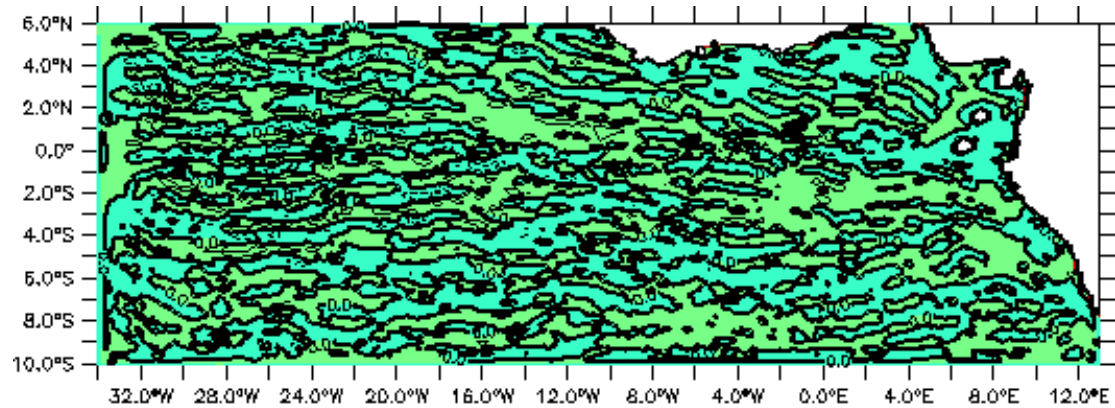


How to identify the sources of vertical velocity in the primitive equation system ?

$$\frac{\partial D}{\partial t} = f\xi - \beta u - \frac{1}{\rho} \nabla^2 P + \vec{\nabla} \cdot \left(\frac{\partial \vec{\tau}}{\partial z} \right) + Adv + Baro + Def$$

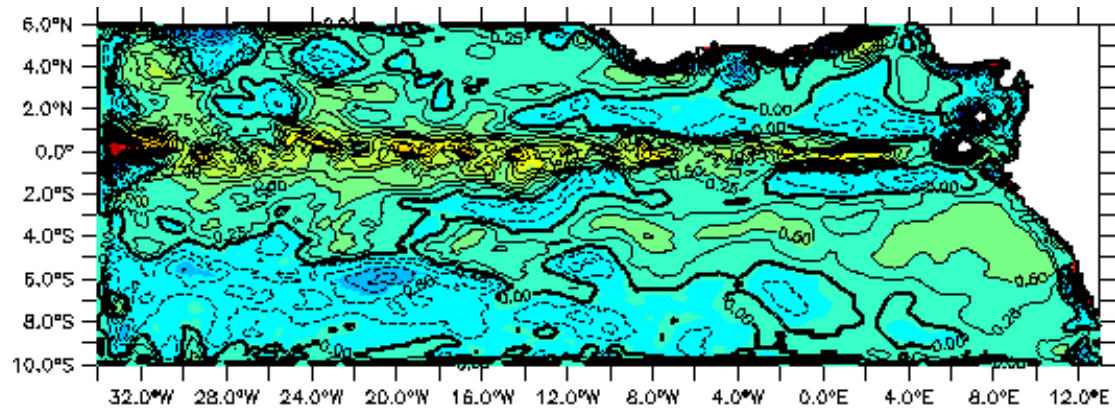
$$w(z) = \int_t \int_z \frac{\partial D}{\partial t} dz dt \Rightarrow \underbrace{w(H) = \frac{\partial D}{\partial t} \frac{H}{r}}_{Zebiak \text{ and } Cane. (1987). approach}$$

OUPS?



DW MODEL (mm/s)

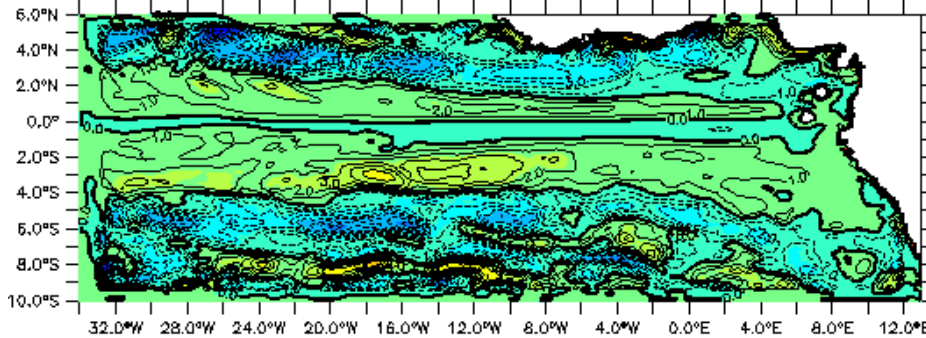
W - May 2006



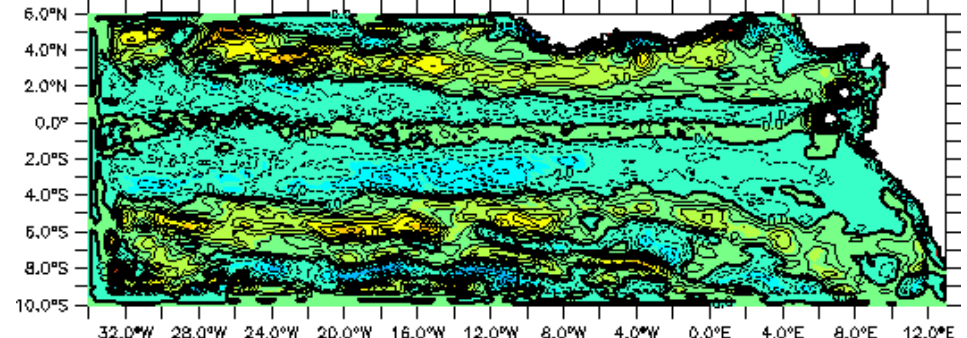
W MODEL (mm/s)

Is there an Equatorial balance?

$$\frac{\partial D}{\partial t} = \underbrace{f\xi - \beta u}_{\text{left}} - \underbrace{1/\rho \nabla^2 P}_{\text{right}} + \dots$$



WZETA+WETAU (mm/s)



WLAP (mm/s)

Yes !

The Linear Equatorial Balance

$$\frac{1}{\rho} \nabla^2 P = f\xi - \beta u$$

$$\frac{\partial \xi}{\partial t} = -\beta v$$

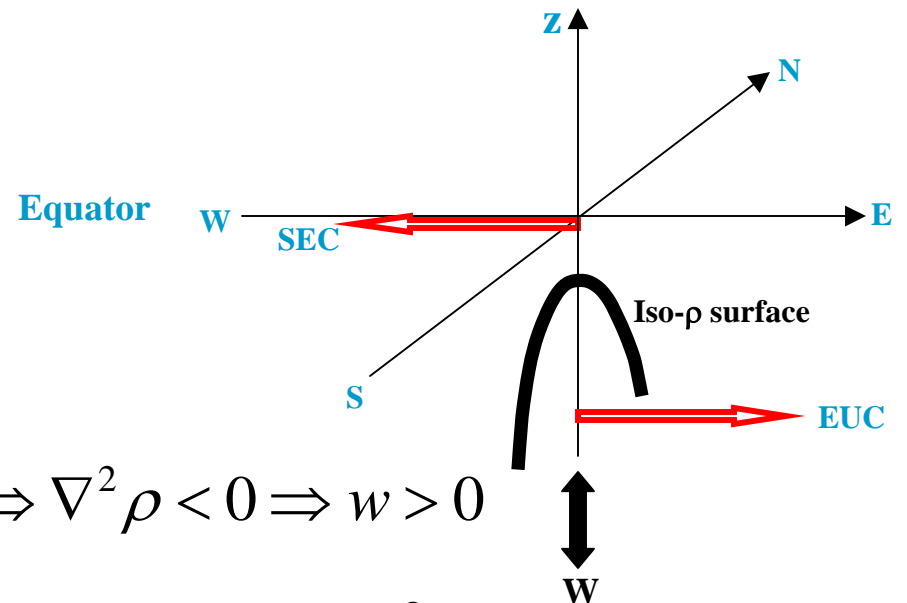
$$\frac{\partial P}{\partial z} = -\rho g$$

$$\frac{1}{\rho} \nabla^2 \rho = \beta \frac{\partial u}{\partial z} + \beta f \frac{\partial v}{\partial z} \Delta t$$

Vertical velocity inferred from the linear balance equation

$$\frac{1}{\rho} \nabla^2 \rho = \beta \frac{\partial u}{\partial z} + \beta f \frac{\partial v}{\partial z} \Delta t - \frac{1}{h^2} \vec{\nabla} \cdot \vec{\tau}_s$$

Upwelling Conditions:

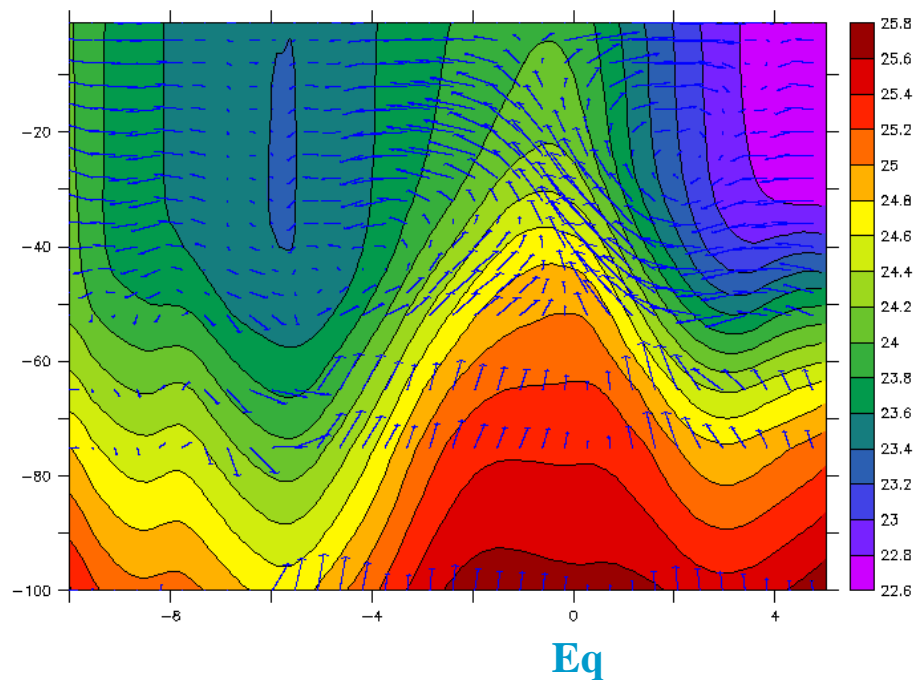


Easterly Wind Pulse: $\tau_x < 0 \Rightarrow \beta \frac{\partial u}{\partial z} < 0 \Rightarrow \nabla^2 \rho < 0 \Rightarrow w > 0$

Southerly Wind Pulse in the South Hemisphere: $\tau_y > 0 \Rightarrow \beta f \frac{\partial v}{\partial z} < 0 \Rightarrow w > 0$

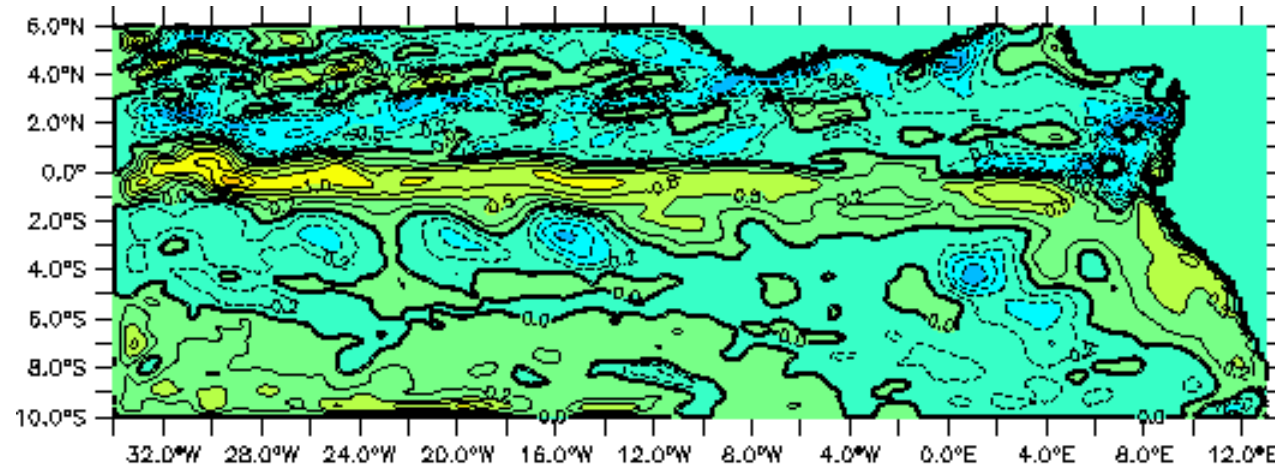
Divergent Surface Stress: $\vec{\nabla} \cdot \vec{\tau} > 0 \Rightarrow w > 0$

w readjusts the density/pressure field to the circulation

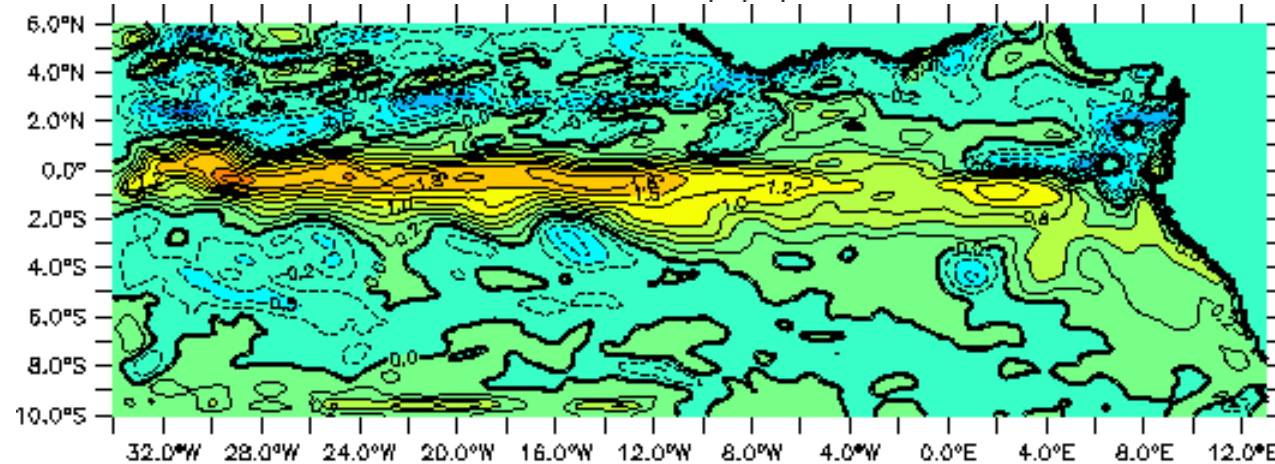


The vertical velocity around the Equator restores the negative concavity of the density/pressure fields in order to sustain the vertical shear of zonal current

BINGO !



WTOT (m/d)



WMODEL (m/d)

Generalized Vertical Velocity Equation

$$\begin{aligned}
 & N^2 \nabla^2 w + f(\xi + f) \frac{\partial^2 w}{\partial z^2} + \frac{1}{T^2} \frac{\partial^2 w}{\partial z^2} + \beta \frac{\partial u}{\partial z} \frac{\partial w}{\partial z} + \left(\nabla^2 N^2 + \beta \frac{\partial^2 u}{\partial z^2} - f \frac{\partial^2 \xi}{\partial z^2} \right) w = \\
 & - \frac{\beta}{\rho} \frac{\partial}{\partial z} \left(\frac{\partial P}{\partial x} \right) - \frac{g}{\rho} \nabla^2 [Advh(\rho)] + \frac{g}{\rho} \nabla^2 \left(\frac{\partial F_\rho}{\partial z} \right) - f \frac{\partial Advh(\xi)}{\partial z} + \beta \frac{\partial Advh(u)}{\partial z} \\
 & + 2\beta f \frac{\partial v}{\partial z} + \beta \frac{\partial^2 \tau_x}{\partial z^2} - f \vec{k} \Lambda \vec{\nabla} \left(\frac{\partial^2 \vec{\tau}}{\partial z^2} \right) - \frac{\partial}{\partial t} \left[\vec{\nabla} \left(\frac{\partial^2 \vec{\tau}}{\partial z^2} \right) \right] \\
 & - f \frac{\partial}{\partial z} [Baro(\xi) + def(\xi)] - \frac{\partial^2}{\partial t \partial z} [Adv(D) + Baro(D) + Def(D)] + \frac{\partial^3 D}{\partial t^2 \partial z}
 \end{aligned}$$

The ω -Response Function: An Elliptic Operator

$$\Gamma(w) = F \quad \Gamma \Leftrightarrow r = 1/T$$

$$\Gamma = \left[N^2 \nabla^2 + \nabla^2 N^2 \right] + \left[f(\xi + f) \frac{\partial^2}{\partial z^2} - f \frac{\partial^2 \xi}{\partial z^2} \right] + \left[\beta \frac{\partial u}{\partial z} \frac{\partial}{\partial z} + \beta \frac{\partial^2 u}{\partial z^2} \right]$$

↓

Pressure/Density

↓

Vorticity

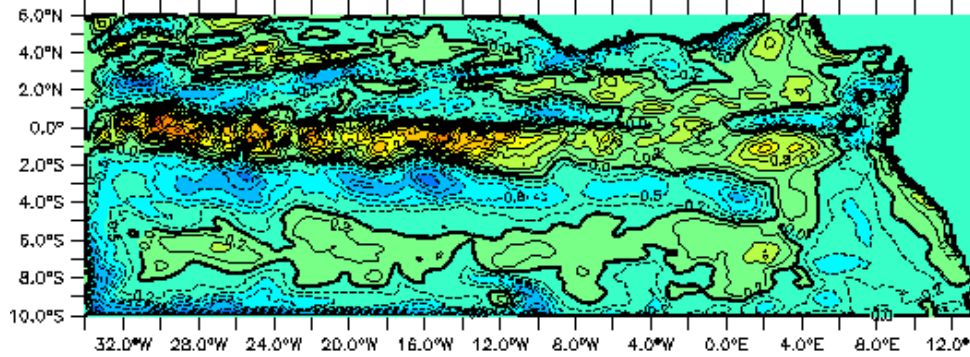
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Zonal Current

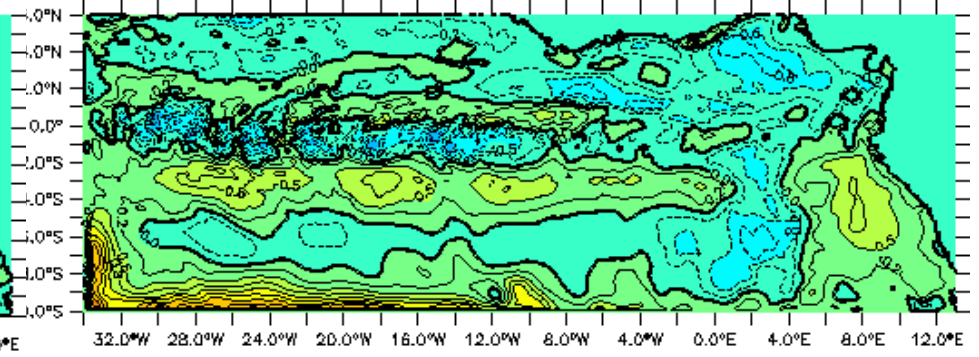
The forcing associated with w works to balance its sources

$$\Gamma(w) = F \Rightarrow w = \Gamma^{-1}(F)$$

Thermodynamical

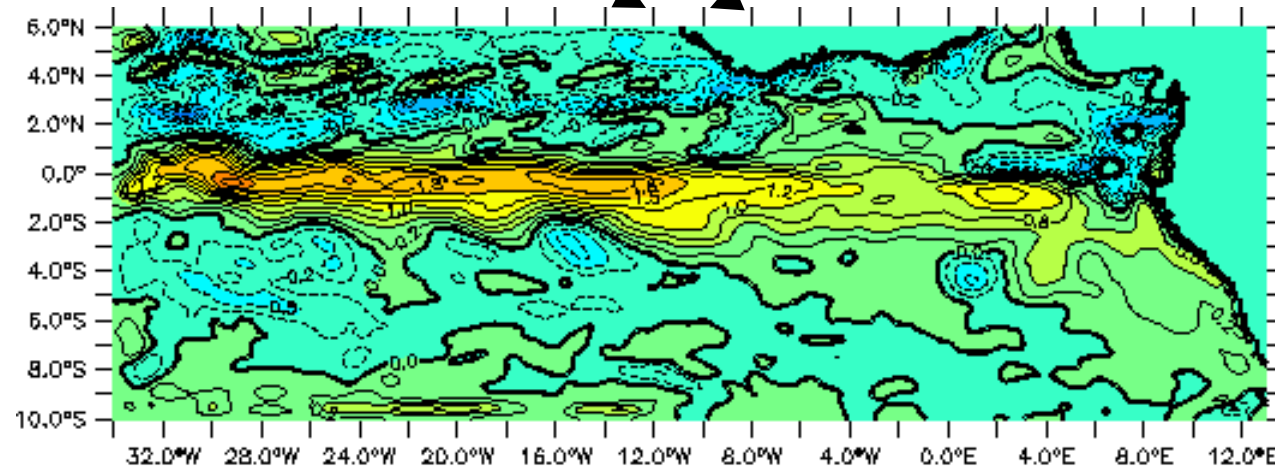


Dynamical



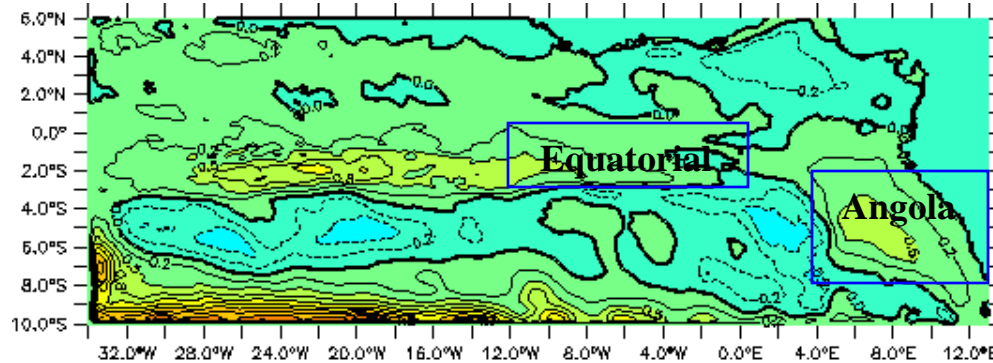
WPRESSURE (m/d)

WDYN (m/d)



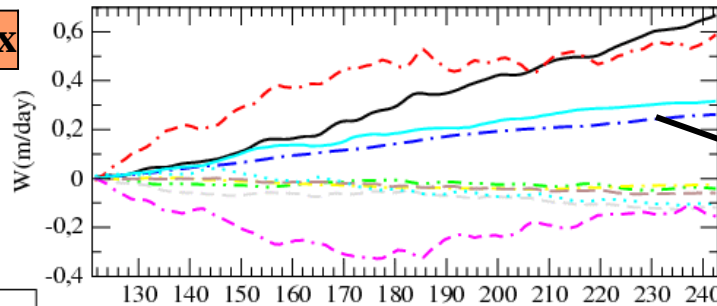
WMODEL (m/d)

Curl of the momentum stress



Equatorial & Angola Boxes

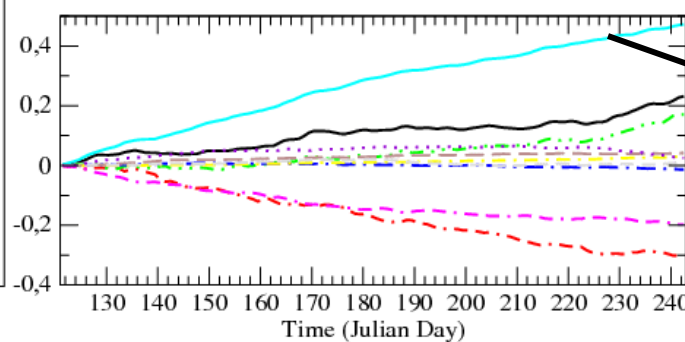
Equatorial box



Transport of ζ

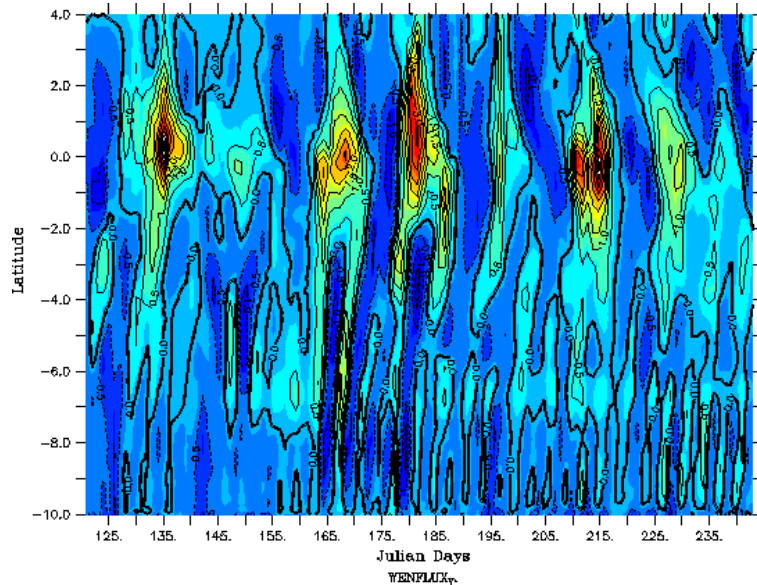
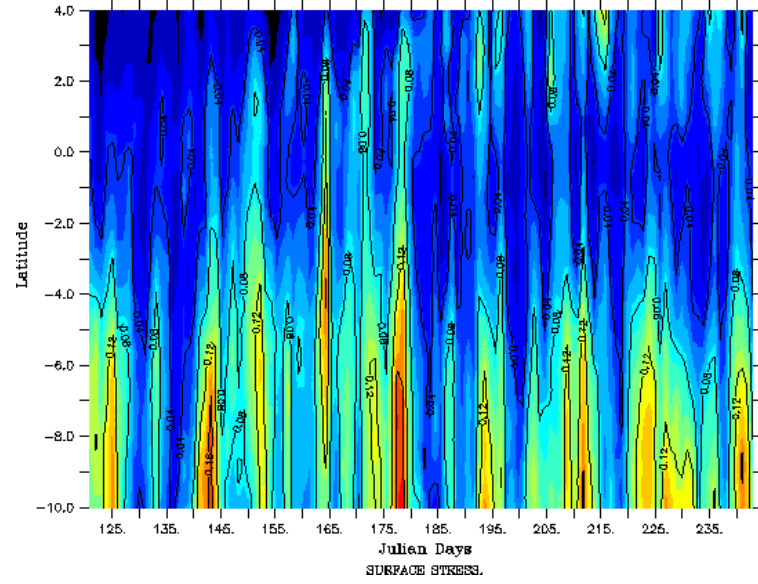
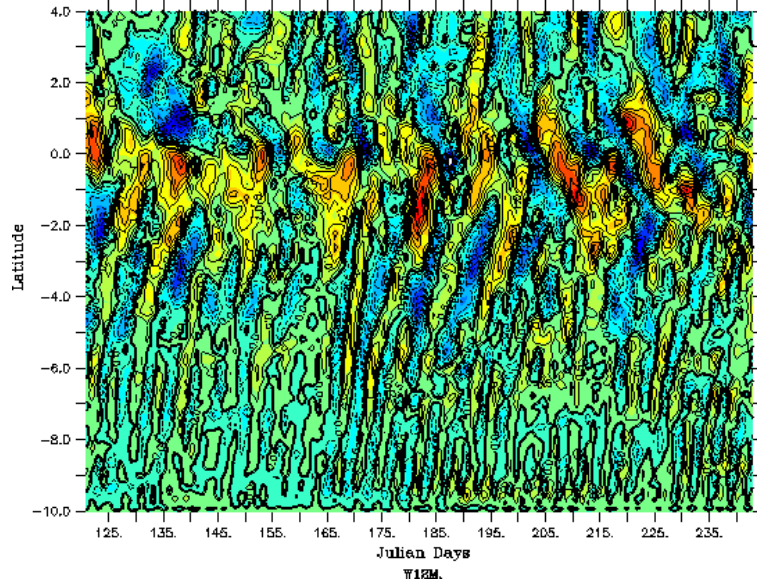
Angola box

- W_{tot}
- - - W_{pres}
- · - W_v
- · - $W_{advzeta}$
- · - W_{advu}
- · - $W_{defzeta}$
- · - W_{defD}
- · - W_{taux}
- · - W_{rotau}
- · - W_{divtau}



Wind-Stress Curl

Vertical Velocity Hovmuller at 10°W



Conclusion

1. The generalized ω -equation:
 - The vertical velocity set up in order to restore the balance equation
 - It includes the Ekman theory (Zebiak and Cane, 1987)
 - Identification of the w -sources in the PE system
2. Equatorial upwelling adjusts the density/pressure fields to the sheared currents system
⇒ Biases in OGCMs and OA coupled models ?
3. ω -equation: Indirect oceanic response to surface wind stress $\vec{\tau}$
Ekman model: Direct response to $\vec{\tau}$
4. Upwelling of Angola results from the curl of momentum stress
5. Transport of vorticity: **Connecting process** between the Equatorial & Angola upwellings